

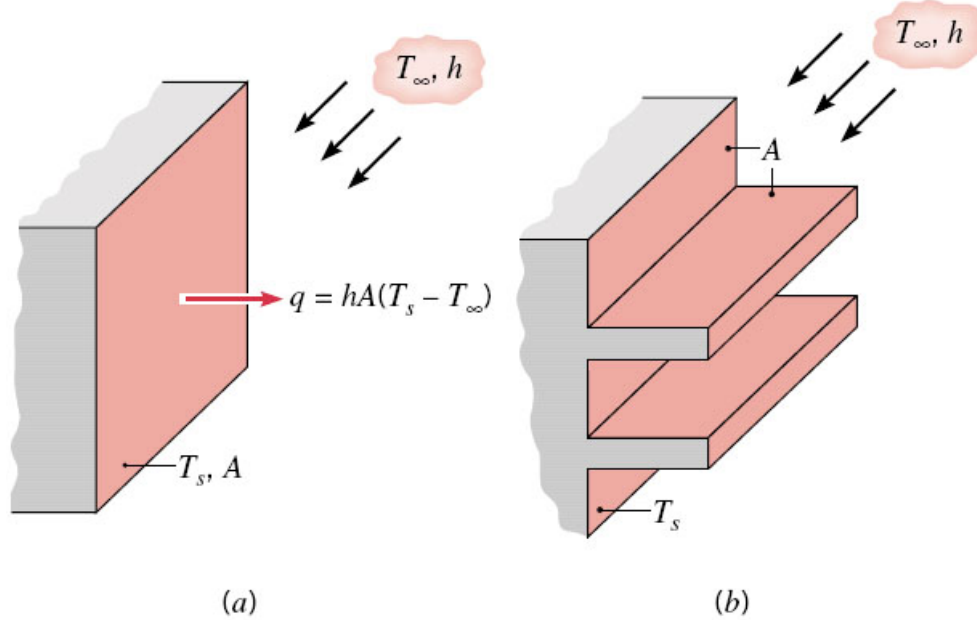
**CH EN 3453 – Heat Transfer**

**Heat Transfer from  
Extended Surfaces  
Part 1**

**Reminders...**

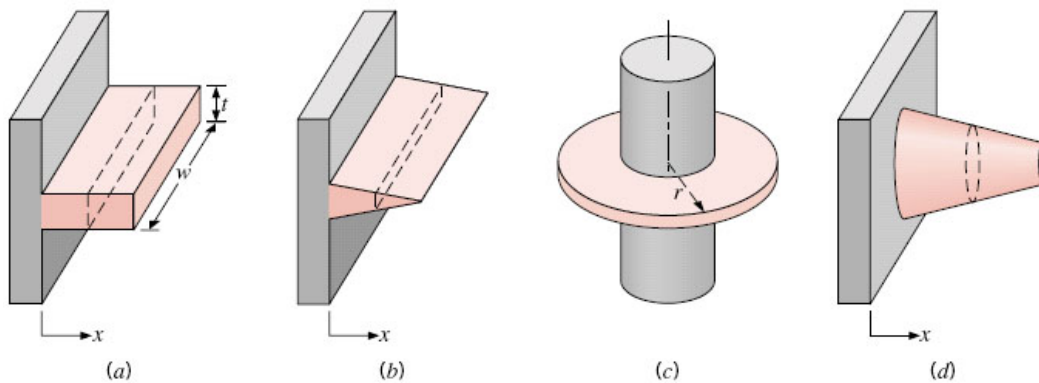
- Homework #3 due Friday
- Help session this afternoon, 4:30 pm in MEB 2325
- Exam #1 in three weeks
  - Covers all assigned reading material in Chapters 1, 2, 3, 4, 5

# Extended Surfaces (fins)



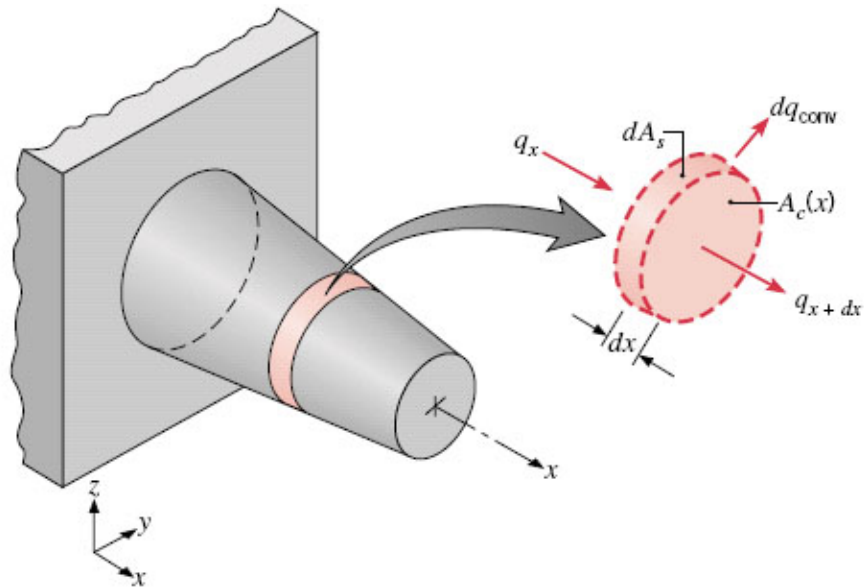
**Figure 3.12** Use of fins to enhance heat transfer from a plane wall. (a) Bare surface. (b) Finned surface.

# Types of Fins



**FIGURE 3.14** Fin configurations. (a) Straight fin of uniform cross section. (b) Straight fin of nonuniform cross section. (c) Annular fin. (d) Pin fin.

# A Fin



**FIGURE 3.15** Energy balance for an extended surface.

## Energy Equation for Extended Surface

General Form:

$$\frac{d^2T}{dx^2} + \left( \frac{1}{A_c} \frac{dA_c}{dx} \right) \frac{dT}{dx} - \left( \frac{1}{A_c} \frac{h dA_s}{k dx} \right) (T - T_\infty) = 0 \quad \begin{array}{l} \text{Eq. 3.66} \\ \text{Page 158} \end{array}$$

...where  $A_c$  is the cross-sectional area of the pin  
 $A_s$  is the external surface area on the sides of the pin

For a straight fin of constant cross-sectional area:

$$\frac{d^2T}{dx^2} - \frac{hP}{kA_c} (T - T_\infty) = 0 \quad \begin{array}{l} \text{Eq. 3.67} \\ \text{Page 158} \end{array}$$

...where  $P$  is the perimeter (meters) of the pin

# Four Scenarios for Treating Pin Tips

**TABLE 3.4** Temperature distribution and heat loss for fins of uniform cross section

Case	Tip Condition ( $x = L$ )	Temperature Distribution $\theta/\theta_b$	Fin Heat Transfer Rate $q_f$
A	Convection heat transfer: $h\theta(L) = -k d\theta/dx _{x=L}$	$\frac{\cosh m(L-x) + (h/mk) \sinh m(L-x)}{\cosh mL + (h/mk) \sinh mL}$ (3.70)	$M \frac{\sinh mL + (h/mk) \cosh mL}{\cosh mL + (h/mk) \sinh mL}$ (3.72)
B	Adiabatic $d\theta/dx _{x=L} = 0$	$\frac{\cosh m(L-x)}{\cosh mL}$ (3.75)	$M \tanh mL$ (3.76)
C	Prescribed temperature: $\theta(L) = \theta_L$	$\frac{(\theta_L/\theta_b) \sinh mx + \sinh m(L-x)}{\sinh mL}$ (3.77)	$M \frac{(\cosh mL - \theta_L/\theta_b)}{\sinh mL}$ (3.78)
D	Infinite fin ( $L \rightarrow \infty$ ): $\theta(L) = 0$	$e^{-mx}$ (3.79)	$M$ (3.80)

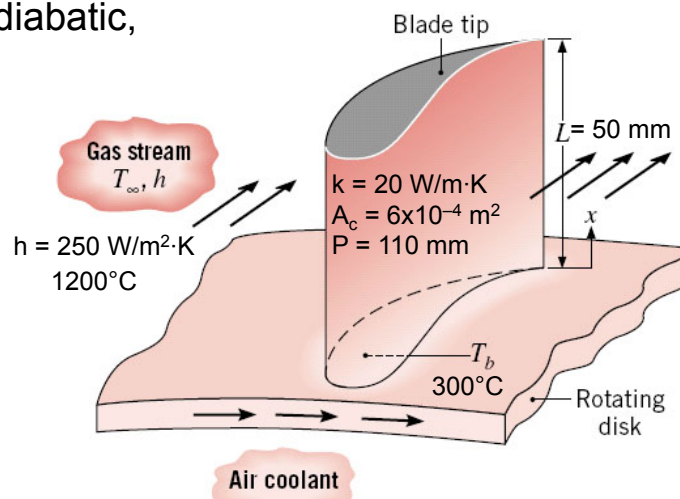
$\theta \equiv T - T_\infty$        $m^2 \equiv hP/kA_c$   
 $\theta_b = \theta(0) = T_b - T_\infty$        $M \equiv \sqrt{hPkA_c} \theta_b$

## Example – Book Problem 3.116

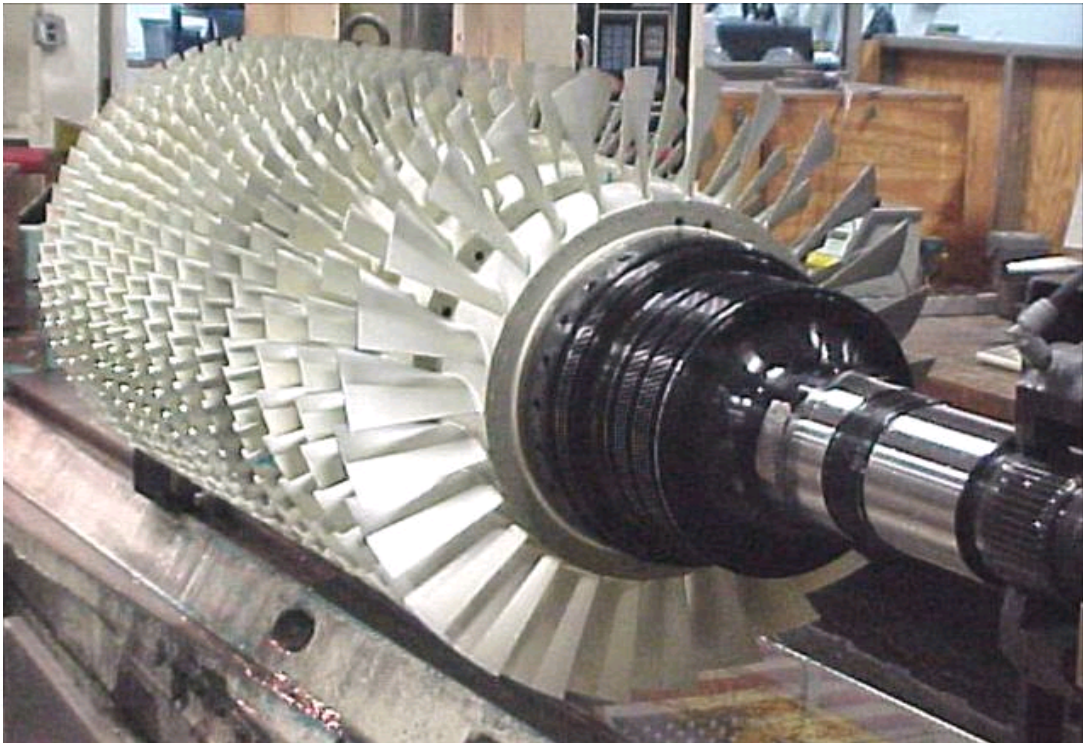
Turbine blade mounted on proposed air-cooled rotating disc ( $T_b = 300^\circ\text{C}$ ) in a gas turbine with gas stream at  $T_\infty = 1200^\circ\text{C}$ .

- (a) If max allowable blade temperature is  $1050^\circ\text{C}$  and blade tip is assumed to be adiabatic, will the air cooling approach work?

- (b) What is the rate of heat transfer from blade to coolant?



# Gas Turbine Blade



8. (20 pts) The case covering the back of my cell phone is soft vulcanized rubber 1/8 inch thick. On the front I have a screen protector of 1/16-inch thick soda lime glass. The phone itself is 2.3 inches wide, 4.5 inches tall and 0.4 inches thick. Each Friday night I watch Star Wars on my phone, which results in heat production of 10 Watts. I notice that the front of the phone (between the phone and glass) is 3°C cooler than the back of the phone (between the phone and rubber). If the air temperature on my windy back porch is 28°C and the convective heat transfer coefficient is 150 W/m<sup>2</sup>·K, what are the temperatures at (a) the phone-rubber interface and (b) the phone-glass interface? Ignore any heat loss through the edges of the phone (i.e., consider only heat loss through the front and back).

