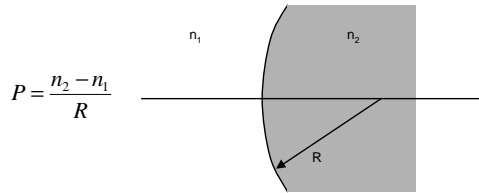


### Refractive Power of a Surface

- The refractive power  $P$  is measured in diopters when the radius is expressed in meters.
- $n_1$  and  $n_2$  are the refractive indices of the two media.



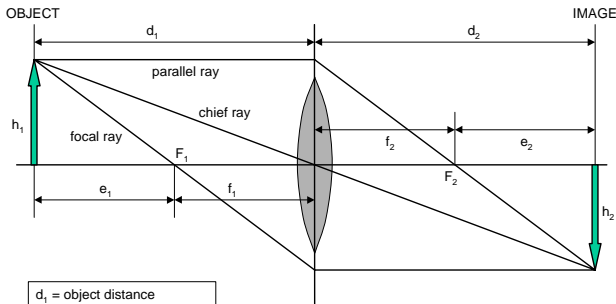
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### EE-527: MicroFabrication

#### Exposure and Imaging

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### Thin Lenses



$d_1$  = object distance  
 $d_2$  = image distance  
 $f_1, f_2$  = focal lengths  
 $e_1, e_2$  = extrafocal distances  
 $h_1, h_2$  = object/image heights

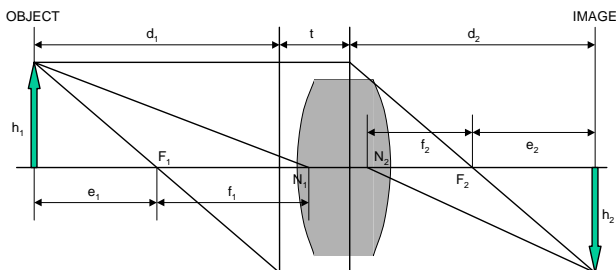
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### Exposure Sources

- Photons
  - white light
  - Hg arc lamp
  - filtered Hg arc lamp
  - excimer laser
  - x-rays from synchrotron
- Electrons
  - focused electron beam direct write
- Ions
  - focused ion beam direct write

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### Thick Lenses

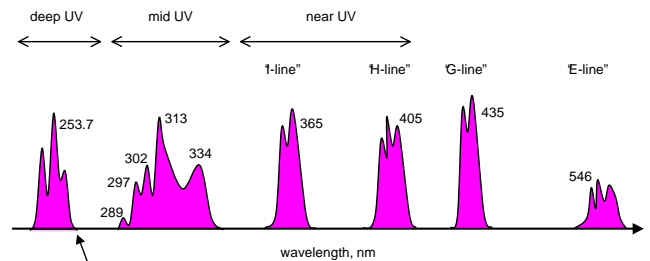


$d_1$  = object distance  
 $d_2$  = image distance  
 $f_1, f_2$  = focal lengths  
 $e_1, e_2$  = extrafocal distances  
 $h_1, h_2$  = object/image heights

Cardinal Points of a Lens:  
 Focal Points:  $F_1, F_2$   
 Nodal Points:  $N_1, N_2$   
 Principal Points:  $H_1, H_2$

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### High Pressure Hg Arc Lamp Spectrum



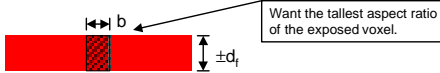
spectral reference;  
 also used for sterilization

The I-line at 365 nm is the strongest.

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## Projection Lithography Requirements

- $b$  = minimum feature size (spot or line)
- $2b$  = minimum period of line-space pattern
- $\lambda$  = exposure wavelength
- Using  $b = f \theta_{\min}$ , obtain that  $b \approx \lambda/2NA$ .
- The depth of focus can be shown to be  $d_f = \pm \lambda/2(NA)^2$
- A "voxel" is a volume pixel.
- For highest resolution lithography, desire the tallest aspect ratio voxel.
- Thus, wish to maximize the ratio  $d_f/b = 1/NA$ .
- SO: it all depends upon the NA of the lens!



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## Lens-Maker's Formula

$$\frac{n_1}{d_1} + \frac{n_2}{d_2} = \frac{n - n_1}{R_1} + \frac{n - n_2}{R_2}$$

If  $n_1 = n_2 = 1$ , then

$$\frac{1}{d_1} + \frac{1}{d_2} = (n - 1) \left( \frac{1}{R_1} + \frac{1}{R_2} \right) = P = \frac{1}{f}$$

This can also be expressed as:  $(d_1 - f)(d_2 - f) = f^2$

or:  $e_1 e_2 = f^2$

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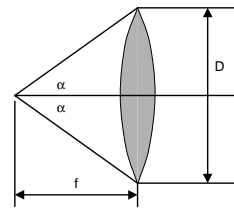
## Sample Calculation

- Primary reduction camera in WTC-MFL uses a projection lens with  $f/6.8$  and  $f = 9.5$  in. = 241.3 mm.
- Lens diameter is  $D = 241.3 \text{ mm}/6.8 = 35.5 \text{ mm} = 1.40$  in.
- The numerical aperture is  $NA = 1/2 * 6.8 = 0.074$ .
- For exposure in the middle green,  $\lambda = 550$  nm.
- Thus, the minimum feature size is  $b = 550 \text{ nm}/2 * 0.074 = 3.72 \mu\text{m}$  for a line, or  $1.220 * 3.72 \mu\text{m} = 4.56 \mu\text{m}$  for a spot.
- The tightest grating pitch that could be printed using this lens is therefore  $2b = 7.44 \mu\text{m}$ .

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## Lens Apertures

- The f-number of a lens ( $f/\#$ ) is the focal length divided by the diameter. It is a measure of the light gathering ability.
- The numerical aperture (NA) of a lens is  $n \sin \alpha$ , where  $\alpha$  is the half-angle of the largest cone of light entering the lens.



$$f/\# = \frac{f}{D}$$

$$NA = n \sin \alpha$$

$$NA = \frac{\frac{1}{2} D}{\sqrt{\frac{1}{4} D^2 + f^2}} \approx \frac{D}{2f} = \frac{1}{2 \cdot f/\#}$$

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## Lens Aberrations

- Chromatic aberration
  - Dispersion: change of refractive index with wavelength
- Monochromatic aberrations
  - transverse focal shift
  - longitudinal focal shift
  - spherical aberration
  - coma
  - astigmatism
  - field curvature
  - distortion

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## Resolving Power of a Lens

- Rayleigh criterion:
  - Minimum angular ray separation to resolve two spots from one is:  $\sin \theta_{\min} = 1.220 \lambda/D$ .
  - Since  $\theta_{\min}$  is small,  $\theta_{\min} \approx 1.220 \lambda/D$ .
  - $D$  is the diameter of a circular aperture.
  - 1.220 is the first zero of the Bessel function  $J_m(x)$ .
  - An Airy function results from Fraunhofer diffraction from a circular aperture.
- Straight line pattern:
  - Minimum angular ray separation to resolve two lines from one is:  $\sin \theta_{\min} = \lambda/D$ , or approximately  $\theta_{\min} \approx \lambda/D$ .

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## Standing Waves - 2

- Standing waves are enhanced by reflective wafer surfaces.
- If the wafer or substrate is transparent, reflections from the aligner chuck can create standing wave patterns, also.
  - This can be eliminated by using:
    - a flat black chuck (anodized aluminum)
    - an optical absorber under the wafer (lint free black paper)
    - a transparent glass chuck (used on Karl Suss MJB3)
- Exposures can be greatly miscalculated by the presence of standing waves and reflective wafers or chucks.

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## Projection Optics

- It is exceedingly difficult to make large NA refractive optics due to aberration limits.
  - The best lenses used in projection lithography have NA = 0.3 - 0.4
  - A lens with NA = 0.50 is a f/1.00 lens: its focal length and effective diameter are the same!
  - The largest NA lenses ever made were a NA = 0.54 and a NA = 0.60 by Nikon.
- Reflective optics are better suited for large NA applications.
  - But they are physically larger, and usually require close temperature stability to keep their proper contours and alignment.
- Combinations (catadioptric) systems are also used.
  - This is very common in DSW (stepper) lithography equipment.

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## Photographic Exposure Equation

$$T = \frac{f^2}{SB}$$

$T$  = exposure time in seconds  
 $f$  = f-number of projection lens  
 $S$  = ASA or ISO film speed  
 $B$  = scene brightness in candles/ft<sup>2</sup>

American Standards Association (ASA) film speed is the dose required to produce an optical density of 0.1 in a film media.

German DIN film speed is:  
 $DIN = 10 \log_{10}(ASA) + 1$   
 100 ASA = 21 DIN

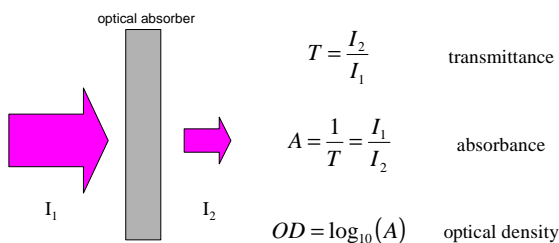
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## Contact and Proximity Lithography Resolution

- $\lambda$  = exposure wavelength
- $d$  = resist thickness
- $2b$  = minimum pitch of line-space pattern
- $s$  = spacing between the mask and the resist
- Contact Printing:
 
$$2b = 3\sqrt{0.5\lambda d}$$
  - At  $\lambda = 400$  nm,  $d = 1$   $\mu$ m, obtain  $b = 0.7$   $\mu$ m linewidth
- Proximity Printing:
 
$$2b = 3\sqrt{\lambda(s + 0.5d)}$$
  - At  $\lambda = 400$  nm,  $s = 10$   $\mu$ m,  $d = 1$   $\mu$ m, obtain  $b = 3.0$   $\mu$ m linewidth

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## Optical Absorbance and Density

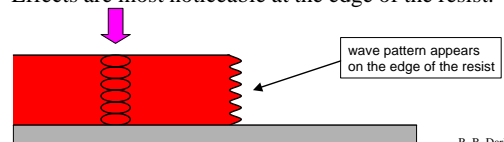


Typical optical densities:  
 xerox transparency: OD = 1  
 photographic emulsion plate: OD = 2-3  
 chrome photomask: OD = 5-6

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## Standing Waves - 1

- Short exposure wavelengths can create standing waves in a layer of photoresist. Regions of constructive interference create increased exposure.
- These can impair the structure of the resist, but can be eliminated by:
  - use of multiple wavelength sources
  - postbaking
- Effects are most noticeable at the edge of the resist.



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## Optical Modulation

$I$  = optical intensity, W/cm<sup>2</sup>  
 $M$  = optical modulation within a scene or image  
 $MT$  = modulation transfer factor for an optical element

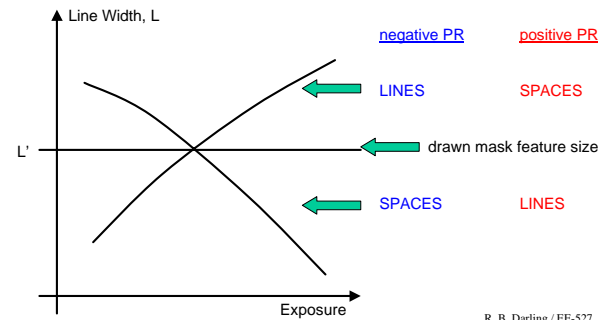
$$M = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} \quad M \rightarrow 1 \text{ when } I_{\min} \rightarrow 0.$$

$$MT = \frac{M_{\text{out}}}{M_{\text{in}}}$$

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## Exposure Latitude

Dimensional Latitude:  
 (typically want less than 0.05)  $\delta = \left| \frac{L' - L}{L'} \right|$



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## Modulation Transfer Function

The modulation transfer function (MTF) is the modulus of the Fourier transform of the linespread function:

$$MTF(f) = \left| \int_{-\infty}^{\infty} L(x) e^{-2\pi i f x} dx \right|$$

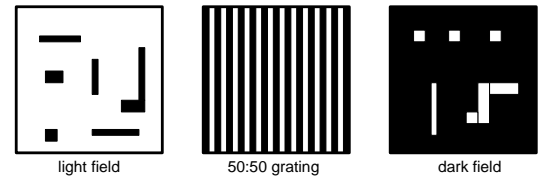
$f$  is the spatial frequency

Optics obeys linear system theory:

$$MTF(\text{system}) = MTF(\text{element}_1) \times MTF(\text{element}_2) \times MTF(\text{element}_3) \times \dots$$

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## Proximity Exposure Effect - 1



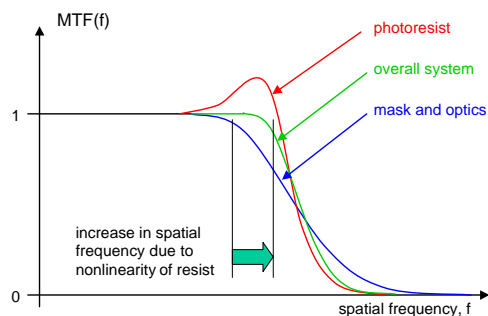
Optimum exposure depends upon the pattern!!!

Adjacent clear (bright) regions add additional exposure to a given region because of overlap from Gaussian tail of the linespread function.

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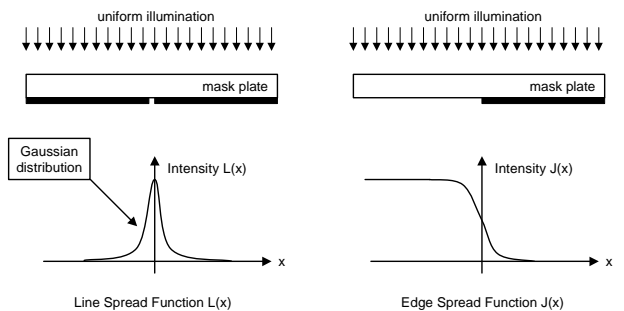
## Modulation Transfer Function in Photolithography

$$MTF(\text{system}) = MTF(\text{mask}) \times MTF(\text{optics}) \times MTF(\text{resist})$$



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## Spread Functions

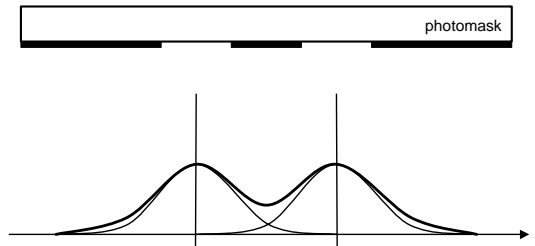


$$L(x) = \frac{dJ(x)}{dx}$$

$$J(x) = \int_{-\infty}^x L(x') dx'$$

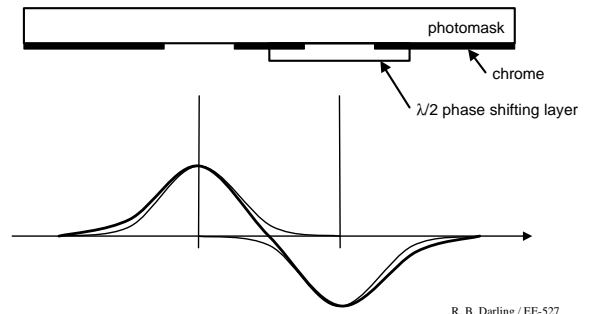
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## Proximity Exposure Effect - 2



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## Phase Shifting Masks



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