

Use the straight-line approximation to sketch the Bode (both magnitude & phase) plots for:
 {label all values on both the x and y axis}

+2 tried

Standard form: $H(s) = \frac{1 \times 10^9}{(s+100)(s+1k)^2}$

$$H(s) = \frac{1 \times 10^9}{(s+100)(s+1k)^2}$$

$$\frac{1 \times 10^9}{(100)(1k)(1k)^2} \left(\frac{s}{100} + 1 \right) \left(\frac{s}{1k} + 1 \right)^2$$

Poles: $\omega = 100, 1k, 1k \text{ rad s}^{-1}$

No zeros.

Starting point = $20 \log_{10}(10) = 20 \text{ dB}$

Mag:

Start at 20dB w/ 0 slope.

@ $\omega = 100 \text{ rad s}^{-1} \rightarrow -20 \text{ dB/dec}$

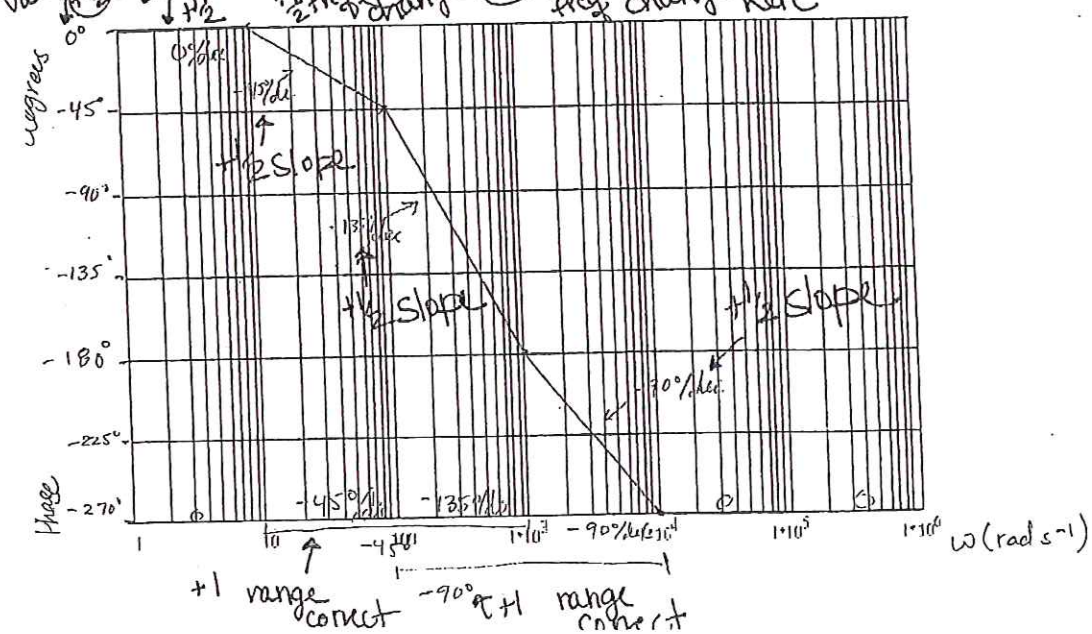
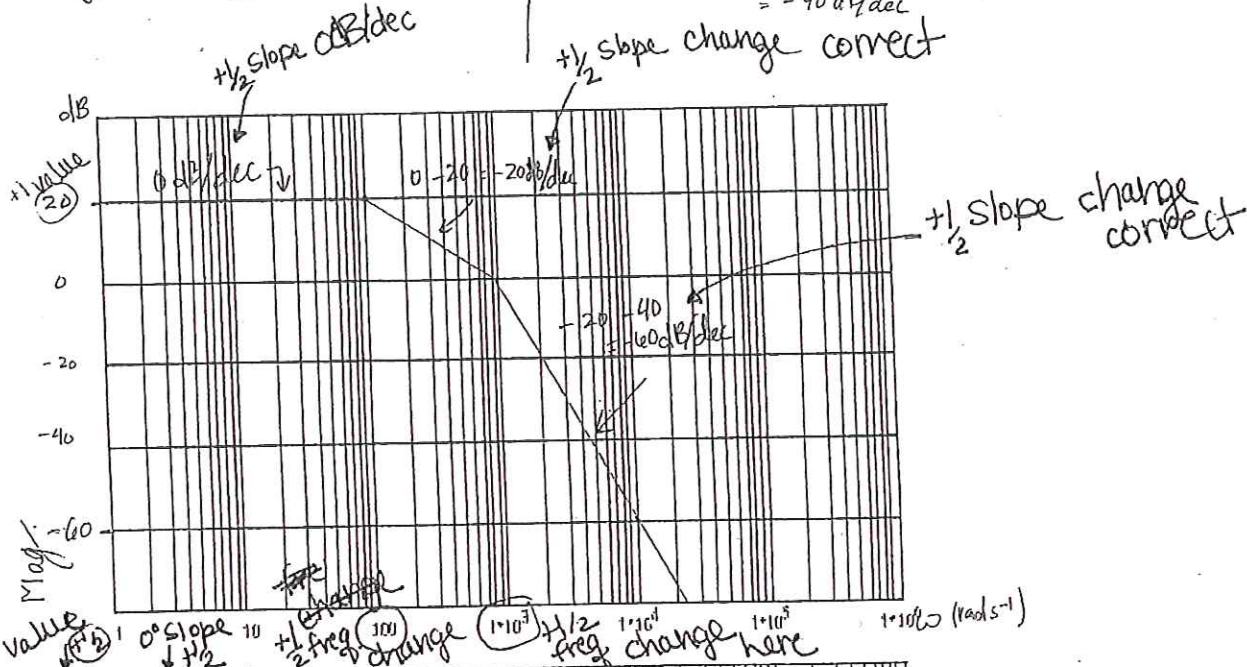
@ $\omega = 1k \text{ rad s}^{-1} \rightarrow 2(-20) \text{ dB/dec}$
 $= -40 \text{ dB/dec}$

Phase

Constant $> 0 \therefore$ Start at 0°

$10 < \omega < 1k \text{ rad s}^{-1} \rightarrow -45^\circ/\text{dec}$

$100 < \omega < 10k \text{ rad s}^{-1} \rightarrow 2(-45^\circ)/\text{dec}$
 $= -90^\circ/\text{dec}$



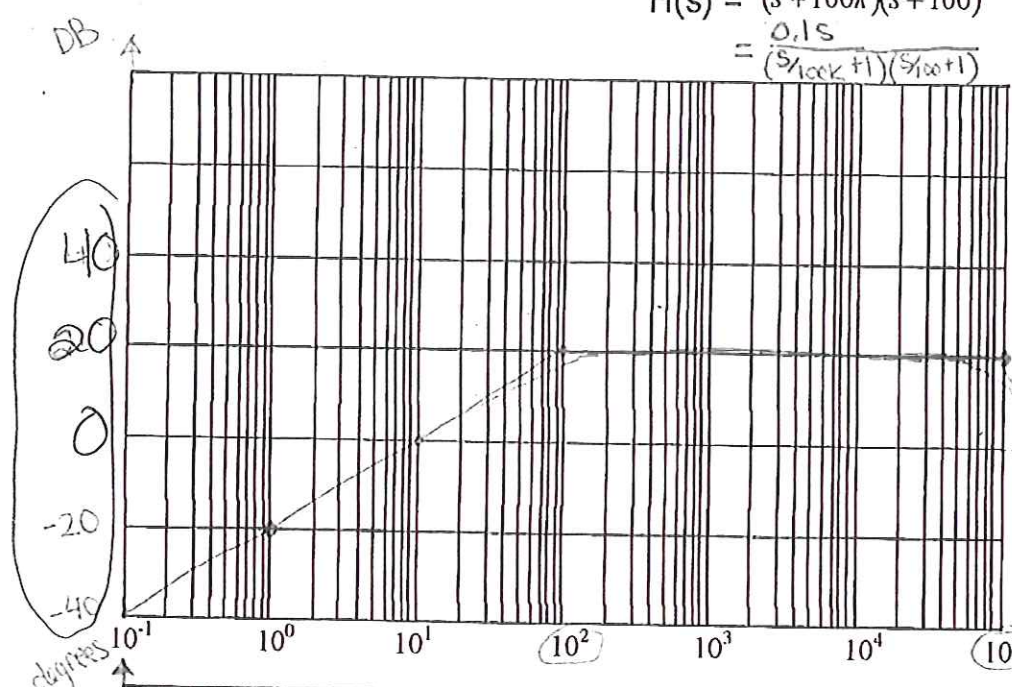
Use the straight-line approximation to sketch the Bode (both magnitude & phase) plot for: {label your axis}

$$H(s) = \frac{1 \times 10^6 s}{(s + 100k)(s + 100)} = \frac{1 \times 10^6 s}{(100k)(100) \left(\frac{s}{100k} + 1\right) \left(\frac{s}{100} + 1\right)}$$

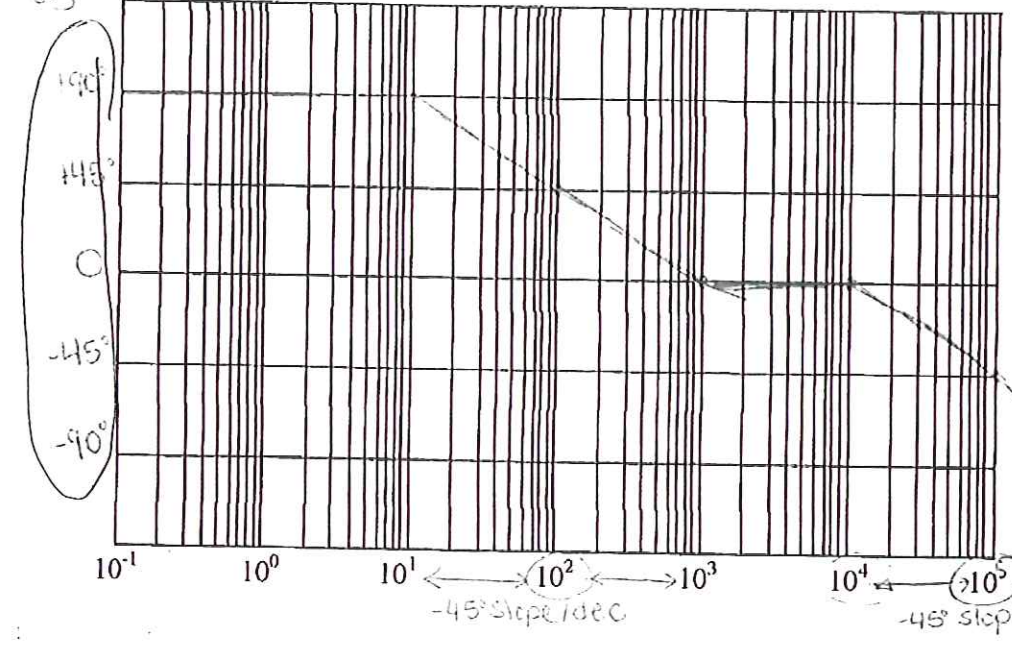
$$= \frac{0.1s}{\left(\frac{s}{100k} + 1\right) \left(\frac{s}{100} + 1\right)}$$

Find starting value \Rightarrow
 use $\omega = 1$ (< 100 & $100k$)

magnitude:
 $\frac{0.1(1)}{\left(\sqrt{\frac{1^2}{(100k)^2} + 1}\right) \left(\sqrt{\frac{1^2}{100^2} + 1}\right)} = 0.1$
 $20 \log(0.1) = -20 \text{ dB}$
 Since there is an s in numerator \Rightarrow starts with slope = $(+1) / (20 \text{ dB})$ and -90°



changes: (magnitude)
 $\omega = 100 \Rightarrow -20 \text{ dB/dec}$
 $\omega = 100k \Rightarrow -20 \text{ dB/dec}$
 (phase)
 $\omega = 10$ to $\omega = 1k \Rightarrow -45^\circ \text{ slope/dec}$
 $\omega = 10k$ to $\omega = 1 \times 10^6 \Rightarrow -45^\circ \text{ slope/dec}$



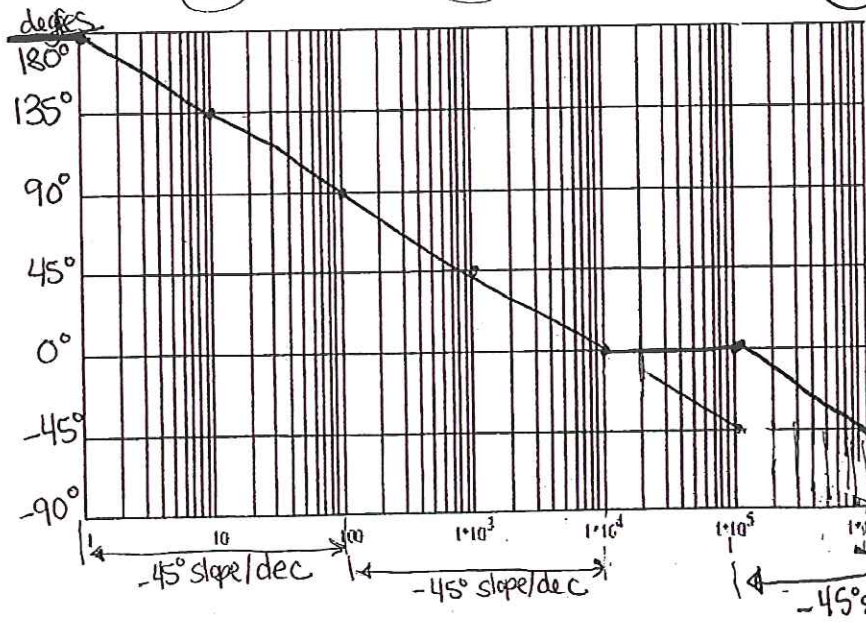
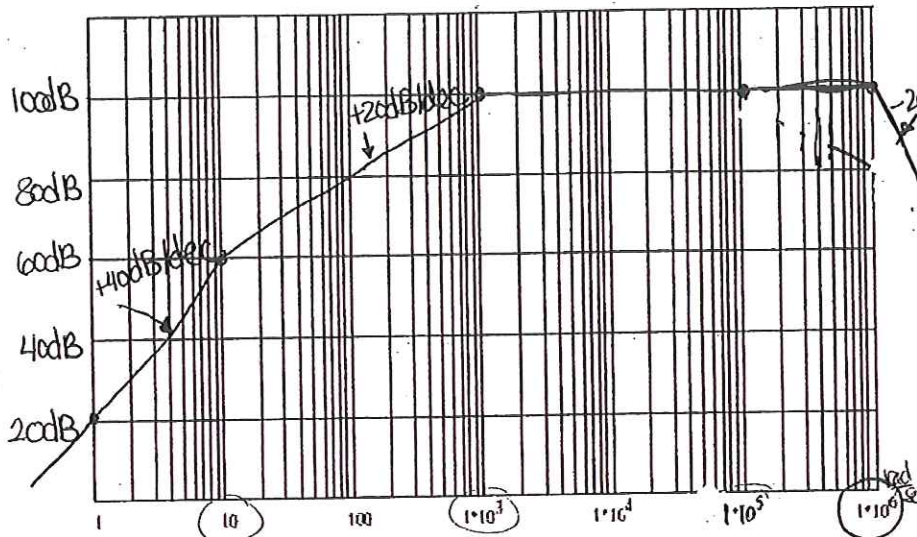
Use the straight-line approximation to sketch the Bode (both magnitude & phase) plots for:
 {label all values on both the x and y axis}

$$H(s) = \frac{1 \times 10^6 s^2}{(s+10)(s+1k) \left(\frac{s}{100k} + 10 \right)}$$

standard form: $\frac{1 \times 10^6 s^2}{(10)(1k)(10) \left(\frac{s}{10} + 1 \right) \left(\frac{s}{1k} + 1 \right) \left(\frac{s}{100k} + 10 \right)} = \frac{10(s^2)}{\left(\frac{s}{10} + 1 \right) \left(\frac{s}{1k} + 1 \right) \left(\frac{s}{1M} + 1 \right)}$

at $\omega=1: (s=j\omega)$
 $\frac{10(1)^2}{\sqrt{\left(\frac{1}{10}\right)^2+1^2} \sqrt{\left(\frac{1}{1k}\right)^2+1^2} \sqrt{\left(\frac{1}{1M}\right)^2+1^2}}$
 ≈ 10
 $20 \log(10) = 20dB$

magnitude:
 2 zero at origin: +40dB/dec
 $\omega=10: -20dB/dec$
 $\omega=1k: -20dB/dec$
 $\omega=1M: -20dB/dec$
phase: +180° starting value
 $1 < \omega < 100: -45^\circ \text{ slope/dec}$
 $100 < \omega < 1k: "$
 $100k < \omega < 10M: "$



- a) Sketch the Bode (both magnitude & phase) plot for: {label as many y values as possible for both magnitude and phase and/or each slope along with showing all your work}

$$H(s) = \frac{-2 \times 10^6 (s+10)^2}{s \cdot (s+1k)(s+10k)} = \frac{-2 \times 10^6 (10)^2 \left(\frac{s}{10} + 1\right)^2}{s(1k)(10k) \left(\frac{s}{1k} + 1\right) \left(\frac{s}{10k} + 1\right)}$$

$$H(s) = \frac{-20 \left(\frac{s}{10} + 1\right)^2}{\left(\frac{s}{1k} + 1\right) \left(\frac{s}{10k} + 1\right)}$$

- b) What is the estimated or actual magnitude value at $\omega=10k$ rad/sec (in dB):

cutoff freq. so $46\text{dB} - 3\text{dB} = \underline{\underline{43\text{dB}}}$

- c) What range of frequency will this circuit operate correctly:

$$\omega = 1k \text{ to } \omega = 10k$$

1 pole at origin \Rightarrow magnitude slope -20dB/dec
phase is -90

negative is $-180 \rightarrow$ start phase $= -180 - 90 = -270^\circ$

starting magnitude value: $\omega=1$: $20 \log \left[\frac{20 \sqrt{(1/10)^2 + 1^2} \cdot \sqrt{(1/10)^2 + 1^2}}{\sqrt{(1/1k)^2 + 1^2} \cdot \sqrt{(1/10k)^2 + 1^2}} \right]$
 $= 26\text{dB}$

magnitude:

(zero) 2 at $\omega=10$: $2(+20\text{dB/dec}) = +40\text{dB/dec}$

$\omega=1k$ (pole): -20dB/dec

$\omega=10k$ (pole): -20dB/dec

phase:

(zero) $1 < \omega < 100$: $2(+45^\circ \text{ slope/dec}) = +90^\circ \text{ slope/dec}$

(pole) $100 < \omega < 10k$: $-45^\circ \text{ slope/dec}$

(pole) $1k < \omega < 100k$: $-45^\circ \text{ slope/dec}$

$$H(s) = \frac{-2 \times 10^6 (s+10)^2}{s \cdot (s+1k)(s+10k)}$$

