

Web Pages

Specifications section, **Lecture 10**



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CS 6110, U of Utah

6 February 2020

Quantifier elimination

Equality

$$x + y = y + x$$

Integer

$$n \mid x$$

Arrays

$$F(i) \rightarrow G(a[i])$$

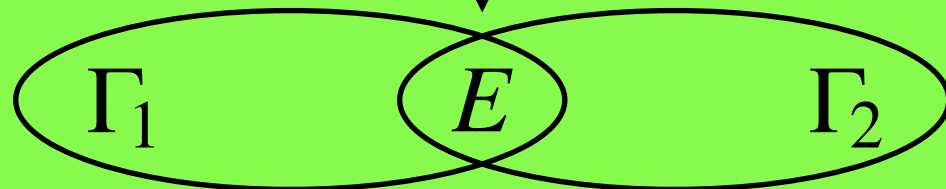
First-order

Unquantified
Input

Tseitin

Nelson-Oppen

Γ
↓

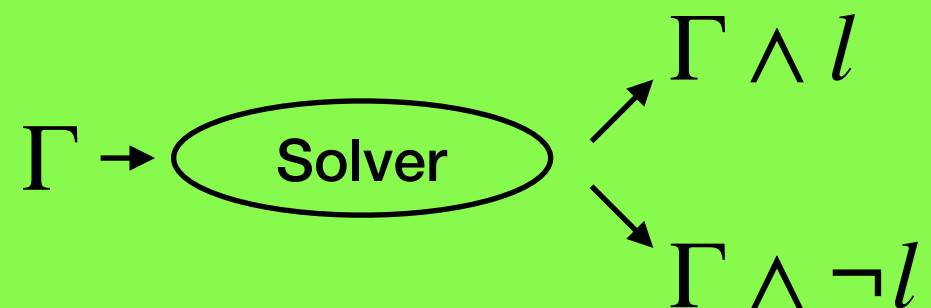


Integer

Array

Conjunctive
Form

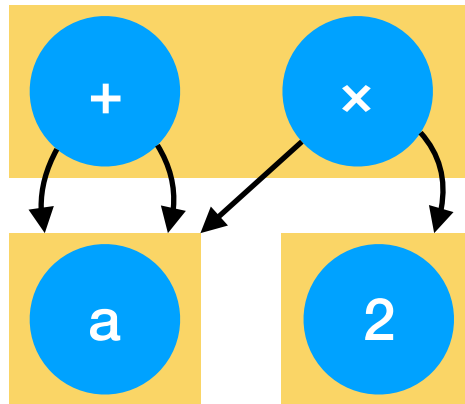
DPLL(T)



Per-Theory
Queries

Domain Reasoning

Equality



Model building
Term database
Equivalence classes

Integers

$$\begin{array}{l} x + 2y \leq z \\ z \leq 2x - y \\ \downarrow \\ x + 2y \leq 2x - y \end{array}$$

Matrix form
Variable elimination
Complexity of integers

Arrays

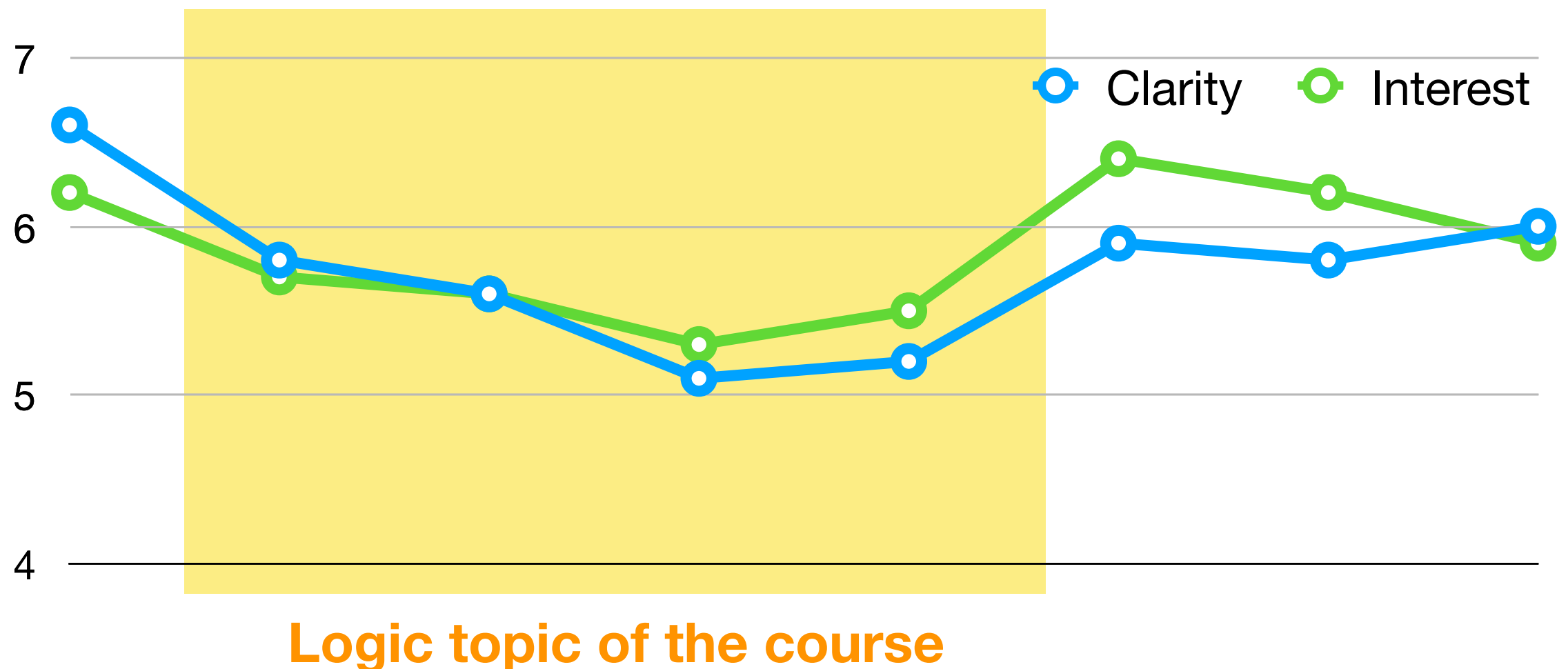
$$\begin{array}{l} a[k := 2] = b \\ \downarrow \\ b[k] = 2 \\ a =_k b \end{array}$$

Mutation graph
Backward propagation
Translation to theory

Theory or Practice

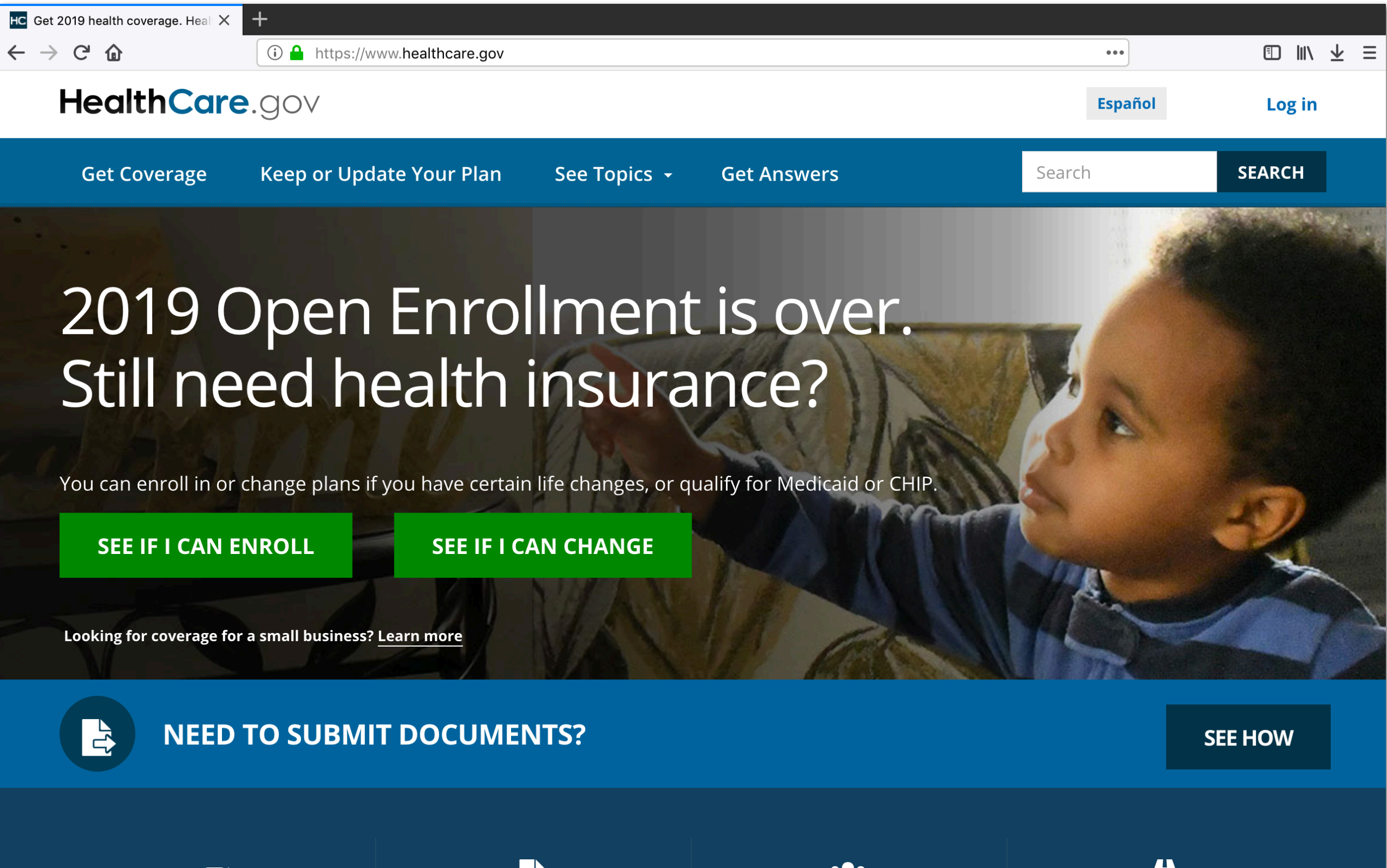
Stoked to move onto more algorithmic related material.

Don't listen to theory haters. I wanna freebase the theory stuff.



Web Page Reasoning

My Research on Web Page Accessibility



2019 Open Enrollment is over. Still need health insurance?

You can enroll in or change plans if you have certain life changes, or qualify for Medicaid or CHIP.

SEE IF I CAN ENROLL

SEE IF I CAN CHANGE

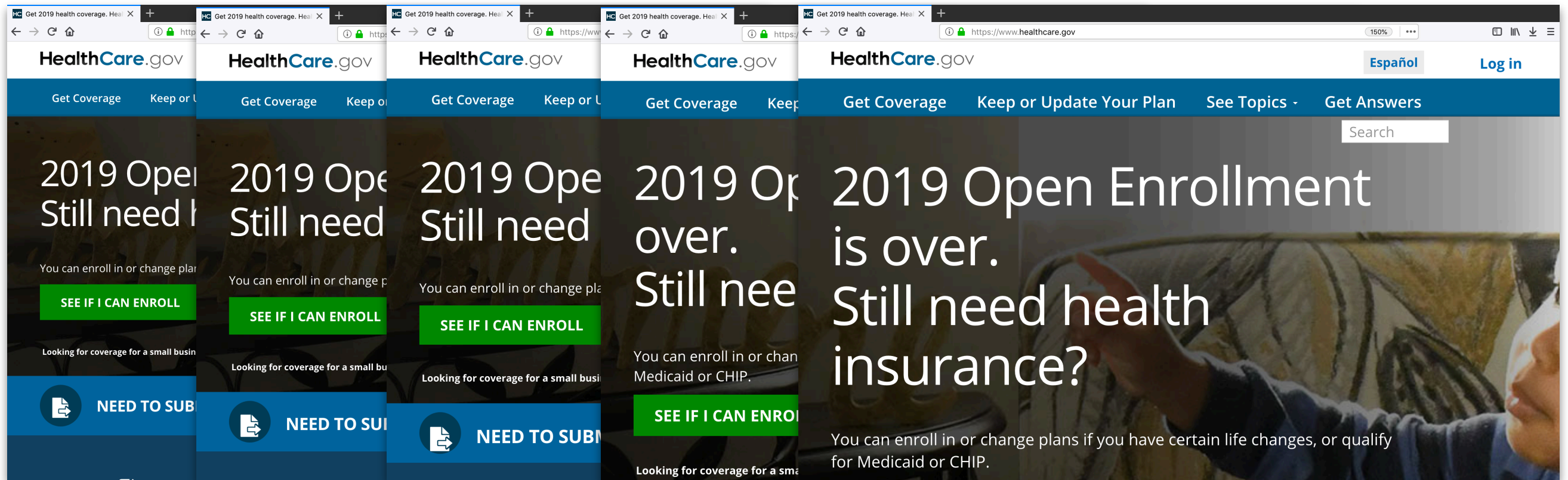
Looking for coverage for a small business? [Learn more](#)



NEED TO SUBMIT DOCUMENTS?

SEE HOW

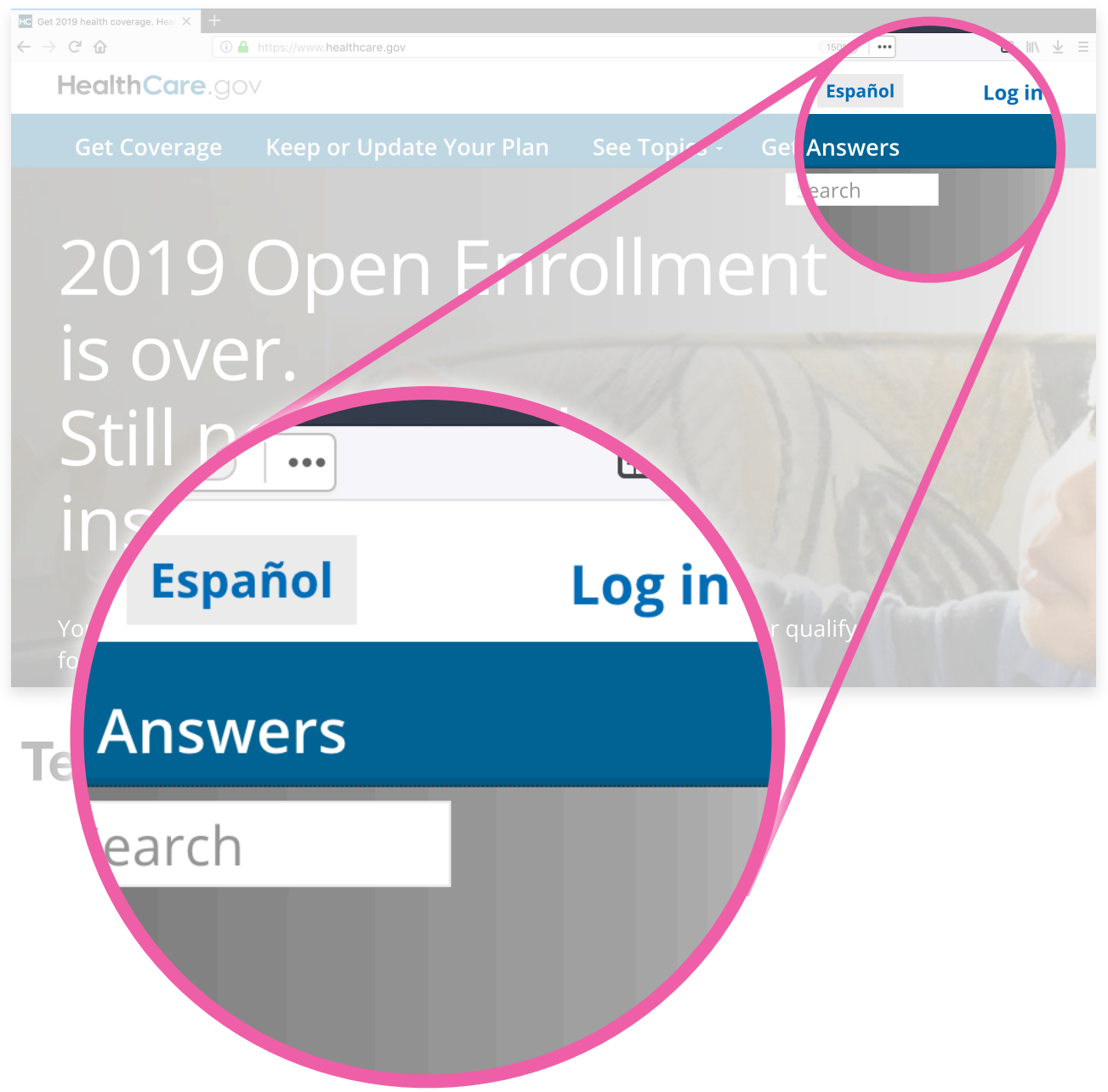
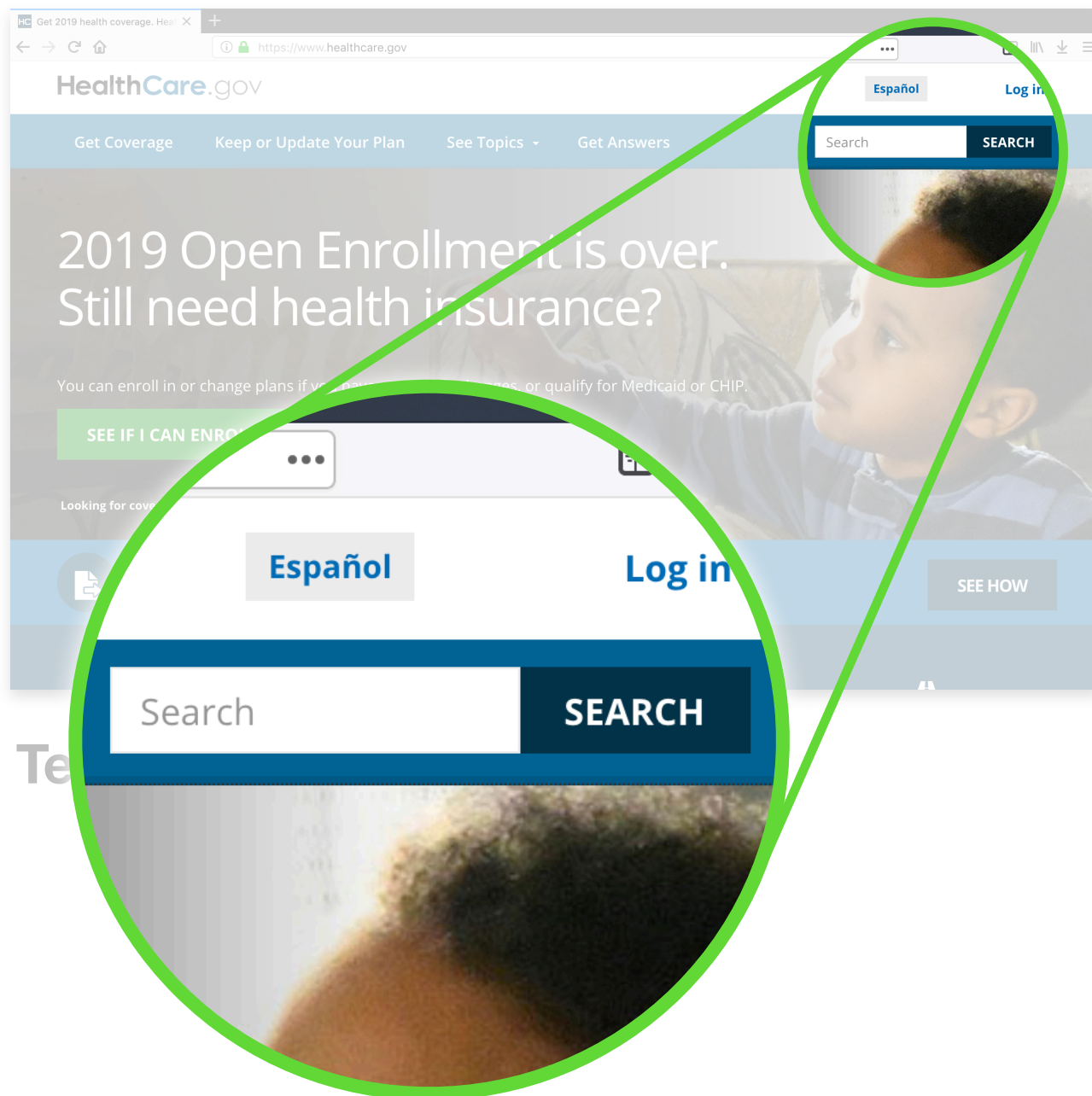
Text Zoom



Text zoom: 100%

Text zoom: 150%

Text-zoom Bug



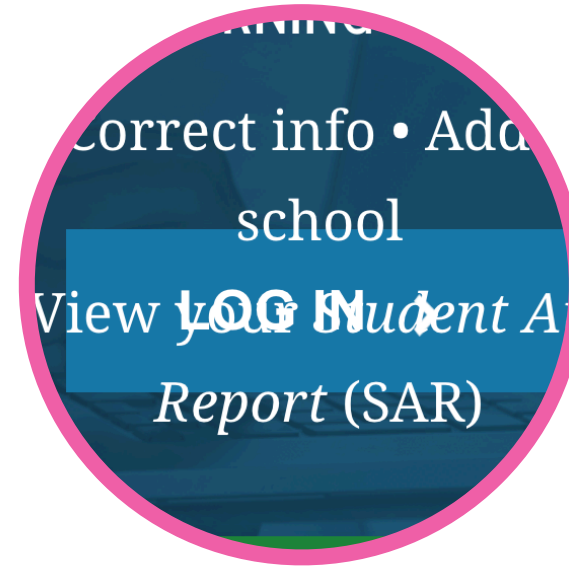
Layout Bugs are Endemic



HealthCare.gov
Missing button



Bank of America
Hidden text



FAFSA
Overlapping text



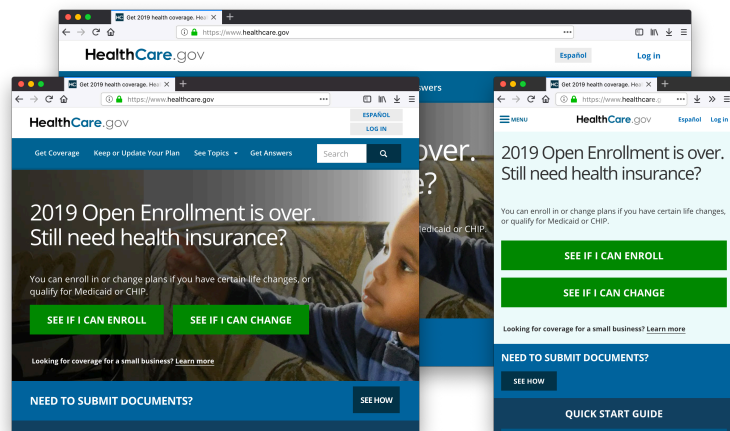
Walgreens
Hidden tabs

12% of Americans have disabilities

Accommodation legally required (under ADA)

How We Find Layout Bugs

Industry standard:
Manual Testing



Manual review
of renderings

Manual selection
of configurations

State of the Art:
Automated Tests



Auto-comparison
of renderings

Random test array
of configurations

My Work:
Verification



Formal specification
for valid renderings

Automated proof
for all configurations

How It Works

Formalize

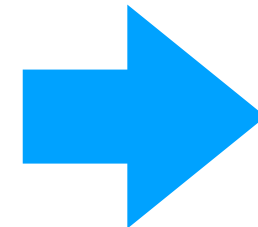
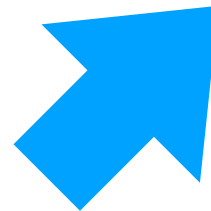
Solve

Scale Up

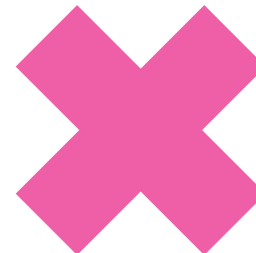
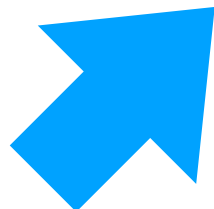
Accessibility



Equations



Web Page



How It Works

Formalize

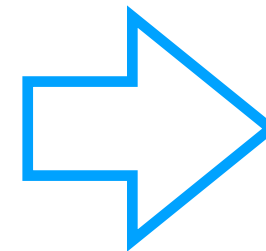
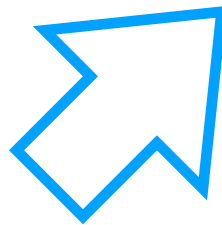
Solve

Scale Up

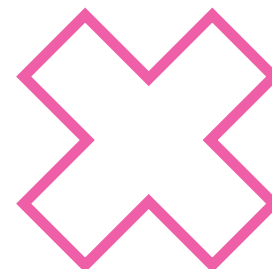
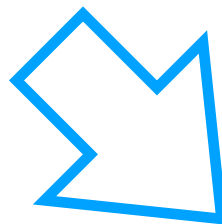
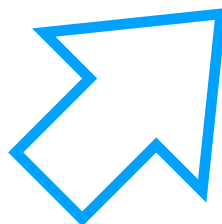
Accessibility



Equations

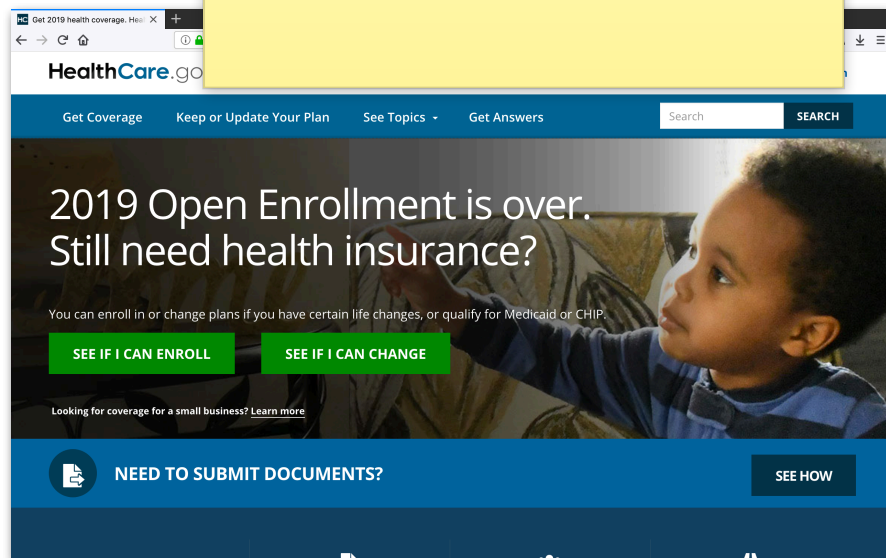


Web Page



Web Pages

JS is “interaction” not behavior



HTML + CSS + JS

Attractive

Easy to Use

Mobile Friendly

Accessible

Simple

Accessibility Guidelines

Developed by
accessibility researchers

Select page elements

Constrain geometry

All handled by VizAssert

DO NOT EDIT

Size & position guidelines

- Text is at least 14px tall
- Lines are at most 80 chars
- Text doesn't overlap

Screen-reader assistance

- Screen-reader text is offscreen
- Header hierarchy matches sizes

Functionality guidelines

- Text zoom up to 200%
- Scrolling in only one dimension

Accessibility Guidelines

Guideline

Text zoom up to 200%
with same functionality



Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Formal Specifications

Behavior

CSS Selector

div[role=banner] [type]

geometry.within

#header + div + div

text.zoom \leq 200%

Geometric primitive

CSS Selector

Inequality



HealthCare.gov
Missing button

Formal Specifications

Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Visual Logic

all elements matching

`div[role=banner] [type]`

are `geometry.within`

the `#header + div + div`

when `text.zoom $\leq 200\%$`
`window.width ≥ 800`

Formalize
→

Only on desktop

Specification to Equations

Visual Logic

all elements matching

div[role=header] [type]

are geometry.within

the #header + div + div

when text.zoom ≤ 200%

window.width ≥ 800

within(B, A) :=

$B.\text{left} \geq A.\text{left} \wedge \dots$

Sizes & positions

$\langle \text{assertion} \rangle ::= \forall b_1, \dots \in \mathcal{B} : \langle \text{cond} \rangle$ **Quantifiers**

$\langle \text{cond} \rangle ::= \langle \text{cond} \rangle \wedge \langle \text{cond} \rangle \mid \neg \langle \text{cond} \rangle \mid \langle \text{cond} \rangle \vee \langle \text{cond} \rangle$
| $\langle \text{real} \rangle = \langle \text{real} \rangle \mid \langle \text{real} \rangle < \langle \text{real} \rangle \mid \langle \text{real} \rangle > \langle \text{real} \rangle$
| $\langle \text{box} \rangle = \langle \text{box} \rangle \mid \langle \text{box} \rangle.\text{type} = \langle \text{type} \rangle \mid \langle \text{box} \rangle.\text{whitespace}$

$\langle \text{real} \rangle ::= \mathbb{R} \mid \langle \text{real} \rangle + \langle \text{real} \rangle \mid \langle \text{real} \rangle - \langle \text{real} \rangle \mid \mathbb{R} \times \langle \text{real} \rangle$
| $\langle \text{box} \rangle.\langle \text{dir} \rangle \mid \langle \text{color} \rangle.r \mid \langle \text{color} \rangle.g \mid \langle \text{color} \rangle.b$

$\langle \text{color} \rangle ::= \text{transparent} \mid \text{rgb}(\langle \text{real} \rangle, \langle \text{real} \rangle, \langle \text{real} \rangle)$
| $\langle \text{box} \rangle.\text{fg} \mid \langle \text{box} \rangle.\text{bg} \mid \gamma(\langle \text{box} \rangle.\text{fg}) \mid \gamma(\langle \text{box} \rangle.\text{bg})$

$\langle \text{box} \rangle ::= b_i \mid \text{root} \mid \text{null} \mid \langle \text{box} \rangle.\text{ancestor}(\langle \text{cond}^* \rangle)$
| $\langle \text{box} \rangle.\text{parent} \mid \langle \text{box} \rangle.\text{first-child} \mid \langle \text{box} \rangle.\text{last-child}$
| $\langle \text{box} \rangle.\text{next} \mid \langle \text{box} \rangle.\text{prev}$

$\langle \text{type} \rangle ::= \text{window} \mid \text{inline} \mid \text{line} \mid \text{text} \mid \text{block}$

$\langle \text{dir} \rangle ::= \text{top} \mid \text{right} \mid \text{bottom} \mid \text{left}$

Booleans + **Linear Real Arithmetic**
+ **Equality** + **Domain concepts**

How It Works

Formalize

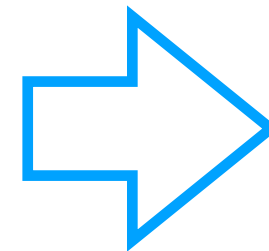
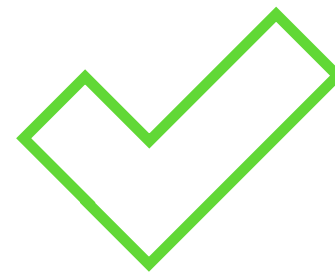
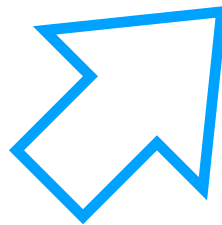
Solve

Scale Up

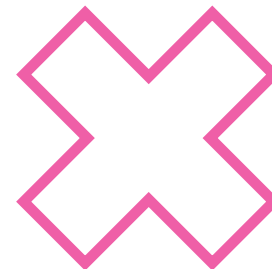
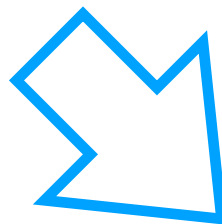
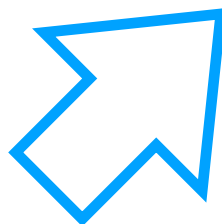
Accessibility



Equations



Web Page



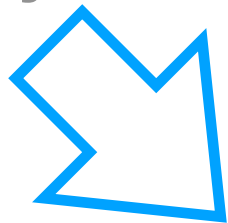
How It Works

Formalize

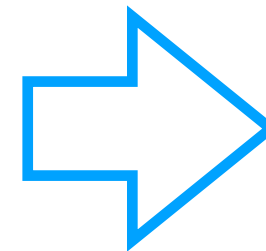
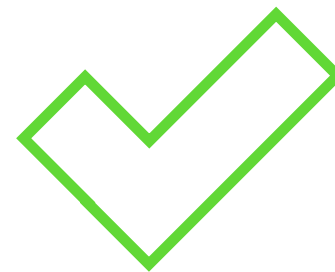
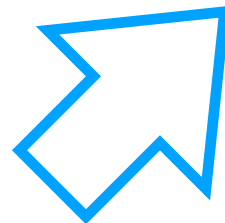
Solve

Scale Up

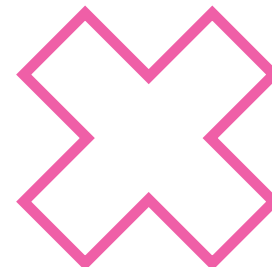
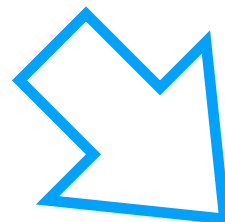
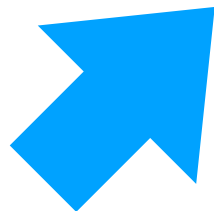
Accessibility



Equations



Web Page



Web Browser

Web Page

HTML + CSS

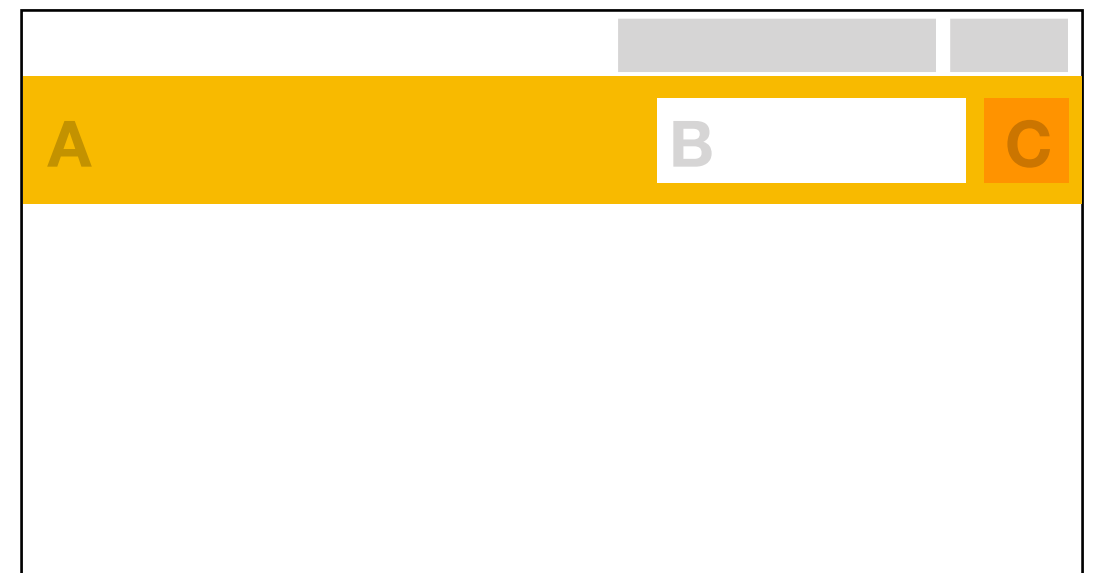
Configuration

Size: 1920×1280

Text zoom: 1.5×



Rendering



Web Browser

Modern Web Browsers:

Millions of lines of code

Decades of development

Dozens of developers

Rendering



Web Browser

Web Page

HTML + CSS

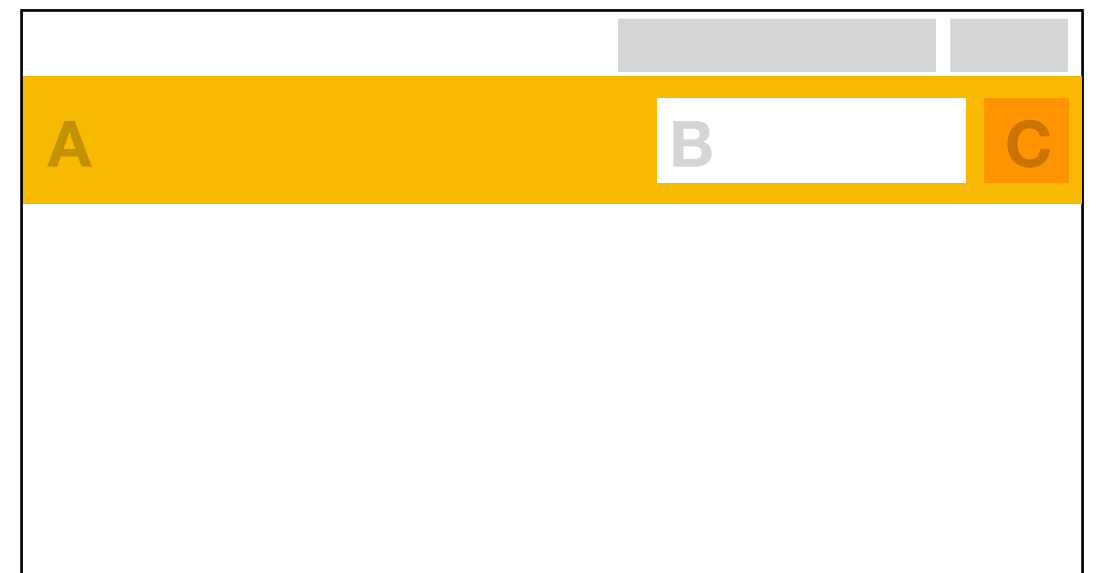
Configuration

Size: 1920×1280

Text zoom: 1.5×



Rendering



Web Browser

Web Page

HTML + CSS

Configuration

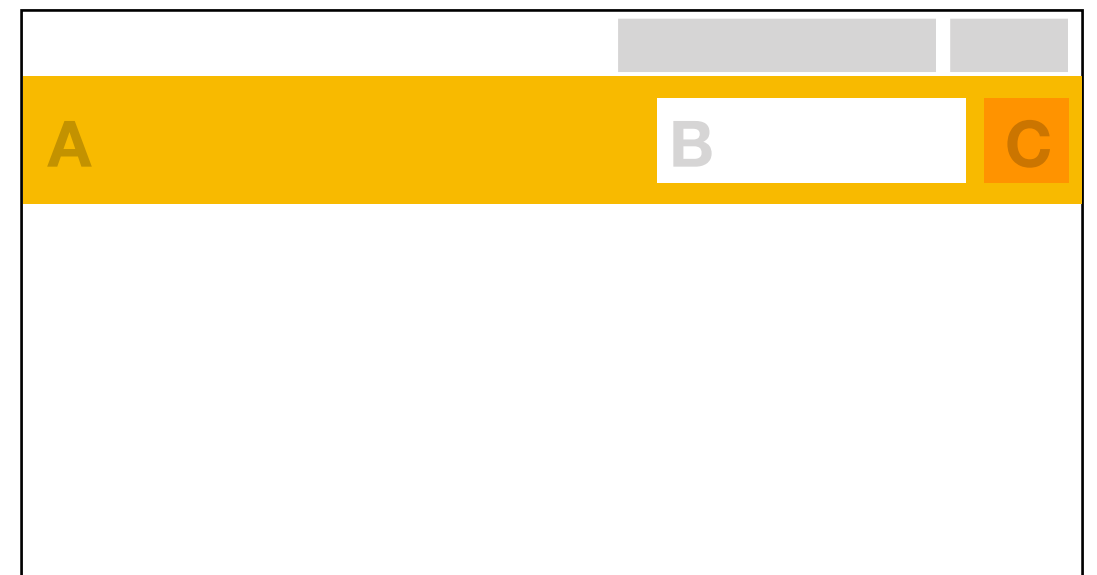
Size: $W \times H$

Text zoom: $Z\times$

Symbolic

Browser

Rendering



Symbolic Web Browser

Web Page

HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$

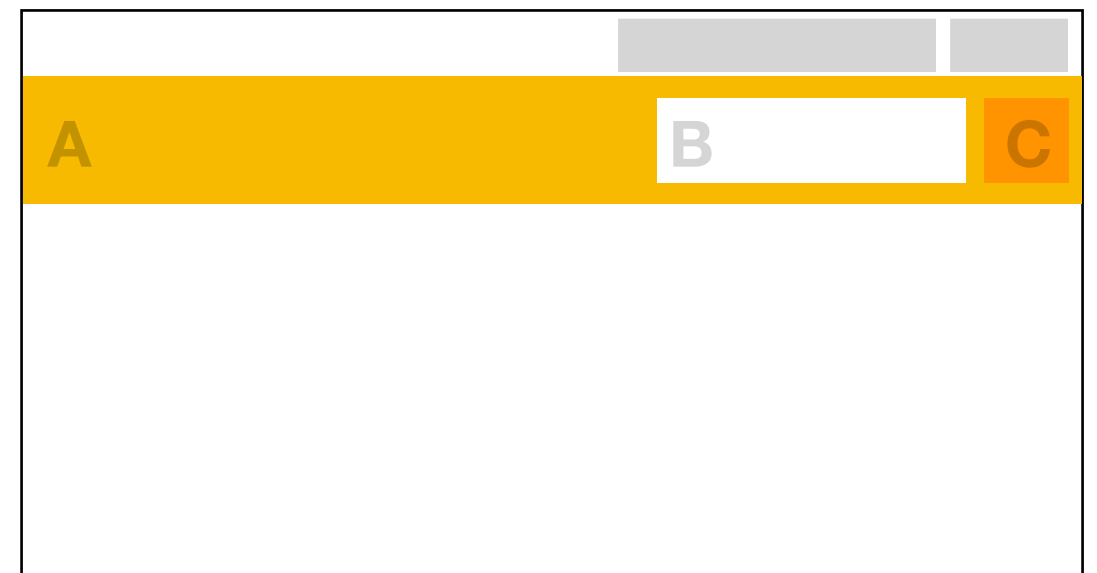
Symbolic

Symbolic

Browser

Rendering

Symbolic



Sizes & positions
depend on W, H, Z

Symbolic Web Browser

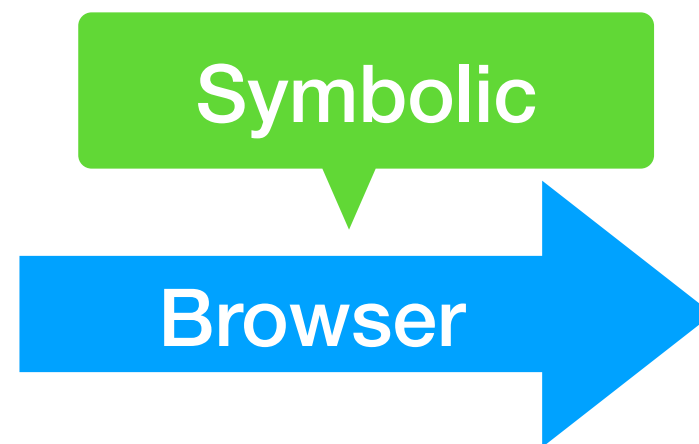
Web Page

HTML + CSS

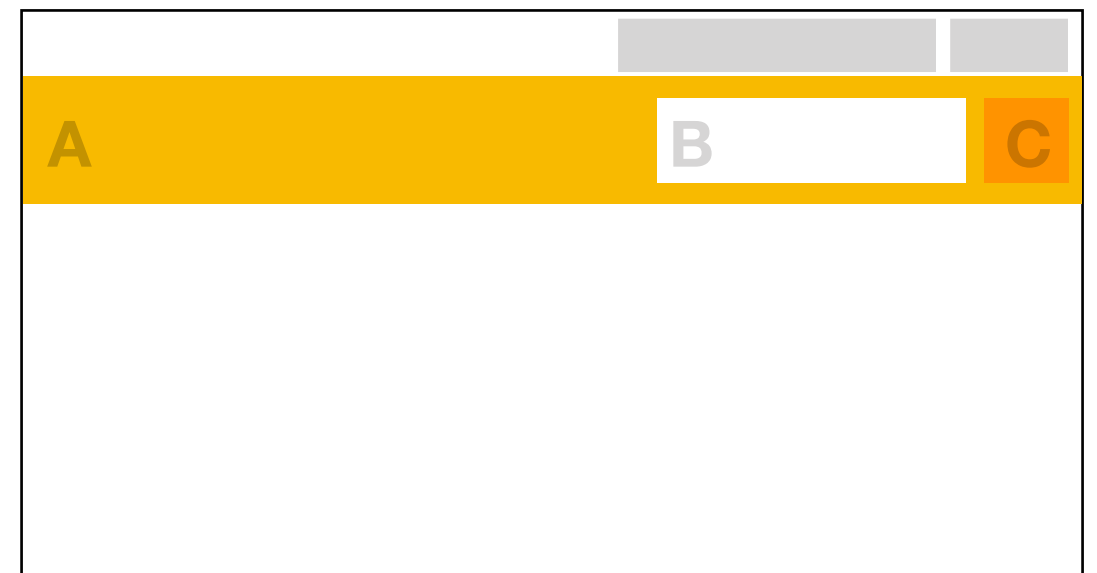
Configuration

Size: $W \times H$

Text zoom: $Z\times$



Rendering



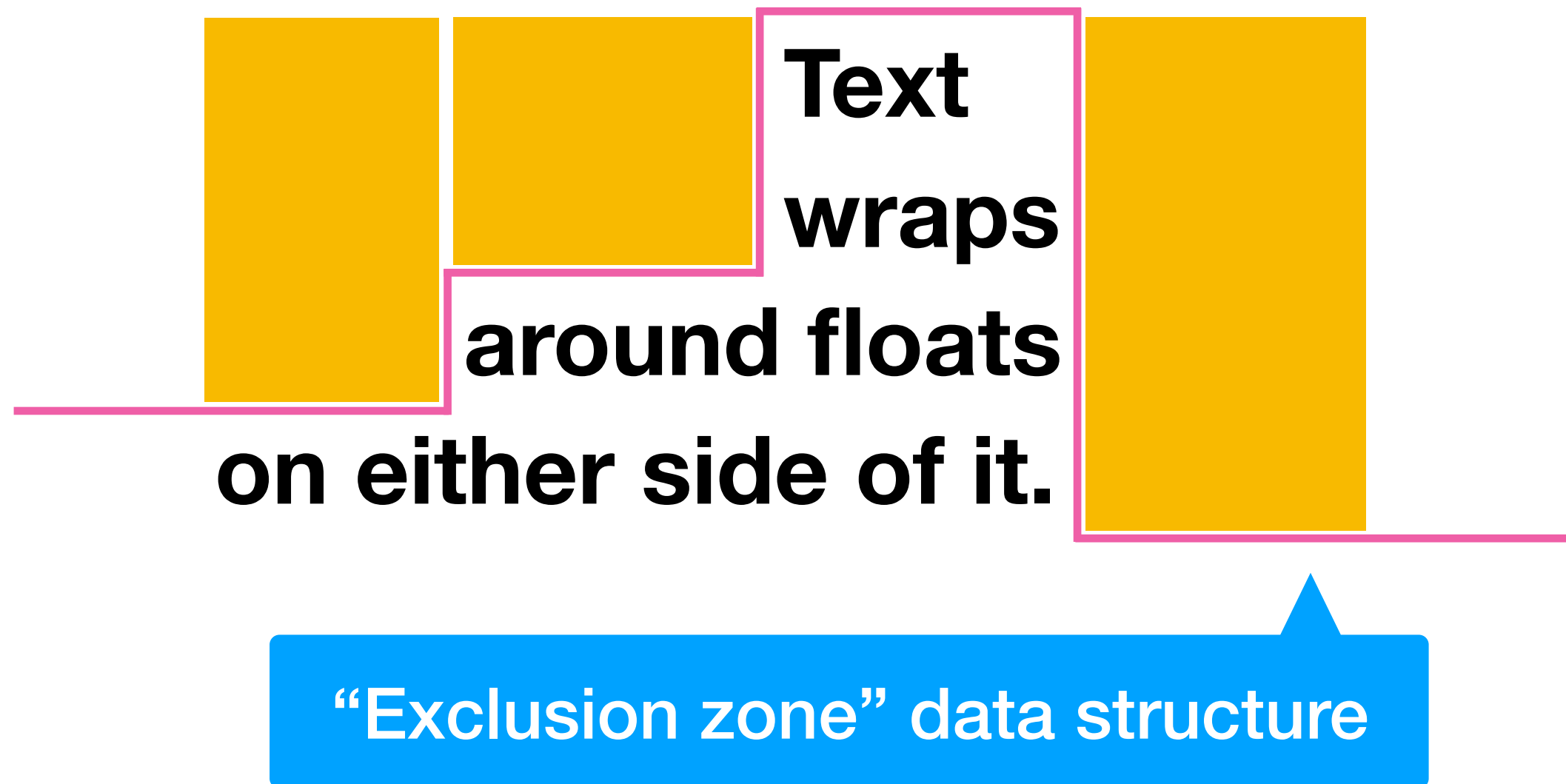
Problem: write a symbolic web browser



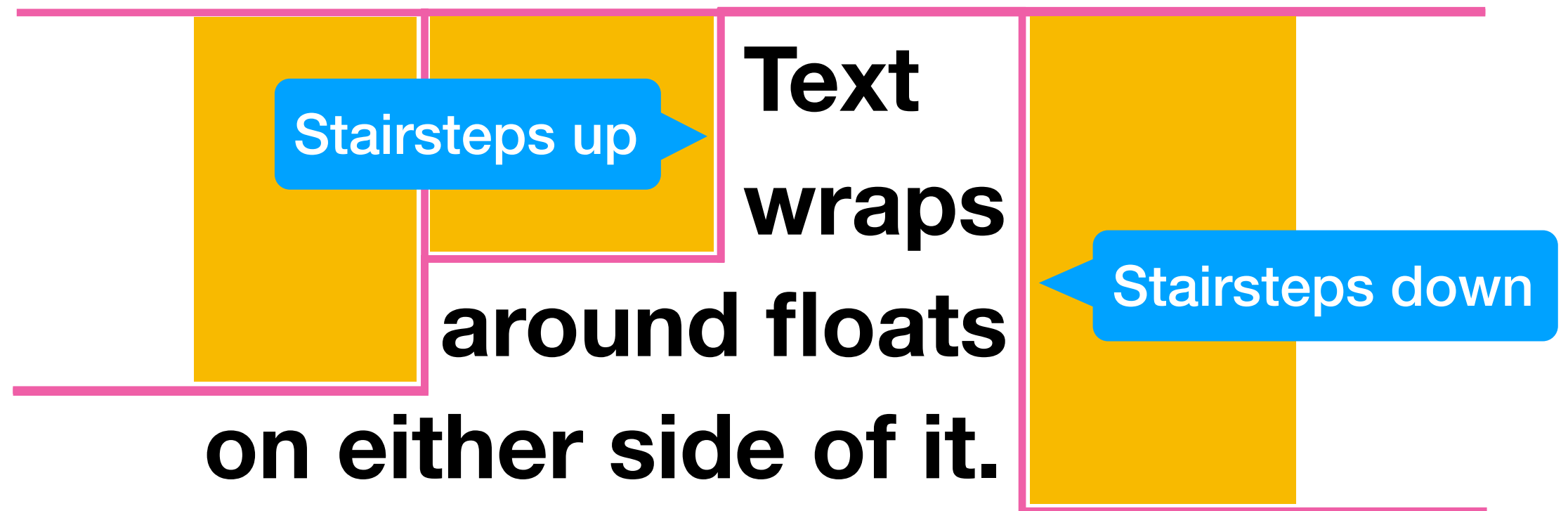
Encodings for visual properties

Scaling symbolic reasoning

Encoding Visual Props



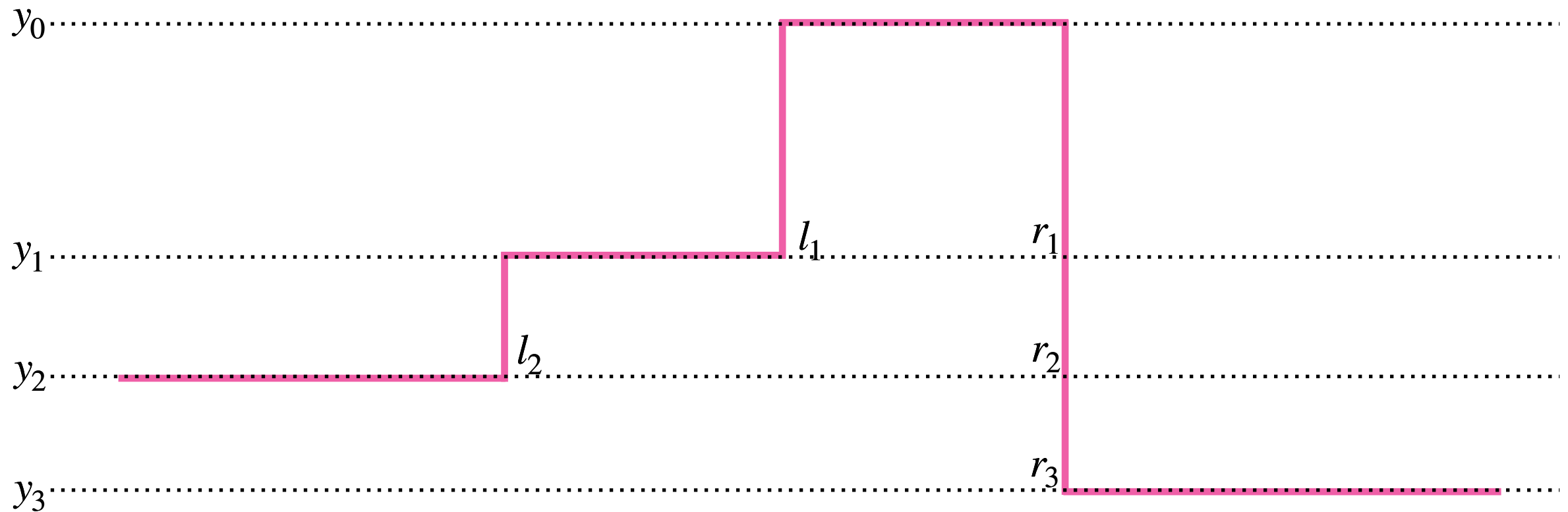
Encoding Visual Props



`ezone.add(size, position)`

`ezone.place(size) → position`

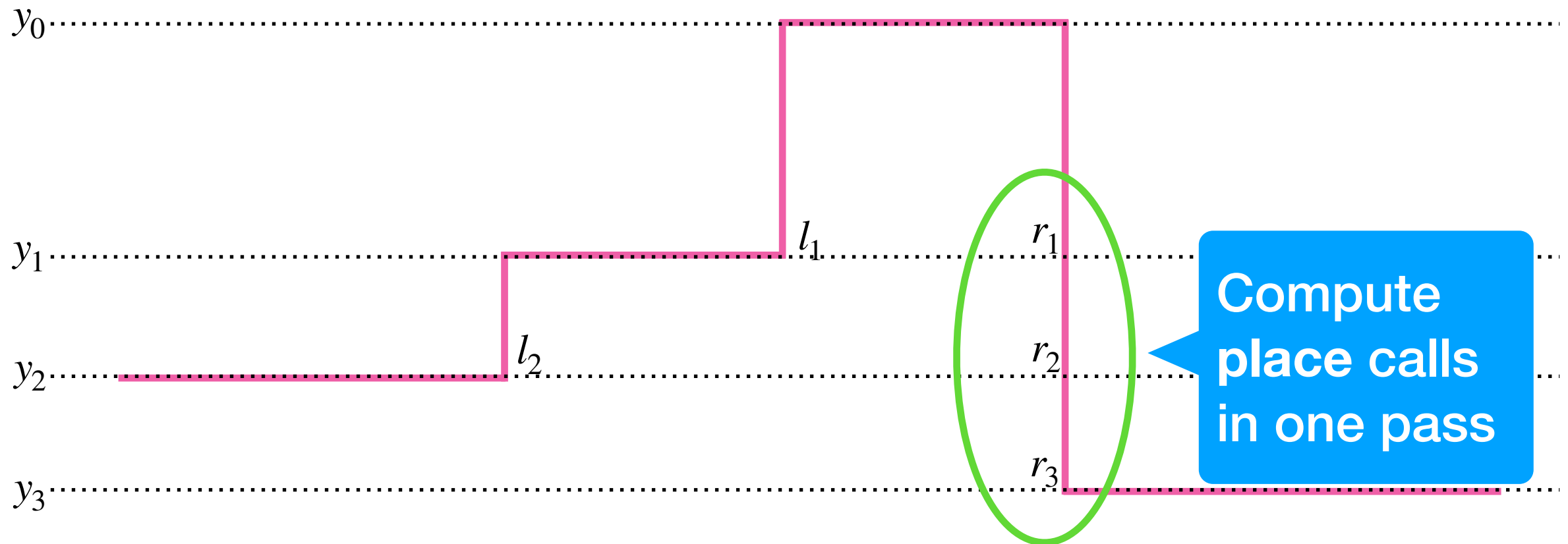
Encoding Visual Props



`ezone.add(size, position)`

`ezone.place(size) → position`

Encoding Visual Props



$\text{ezone} = y_0 \quad (y_1, l_1, r_1) \quad (y_2, l_2, r_2) \quad (y_3, \perp, r_3)$

$\text{ezone.add}(\text{size}, \text{position})$

$O(n)$ equations

$\text{ezone.place}(\text{size}) \rightarrow \text{position}$

$O(n)$ equations

Validating the Formalization

Non-automated

Standard Tests



Browsers



Evaluate: Differential testing vs browsers



Pass thousands of conformance tests

Found bugs in existing browsers

[OOPSLA'16]

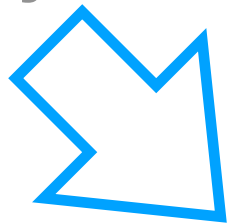
How It Works

Formalize

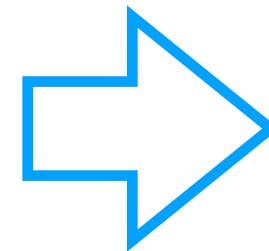
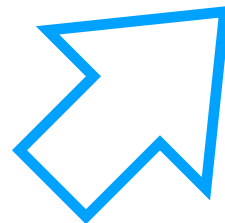
Solve

Scale Up

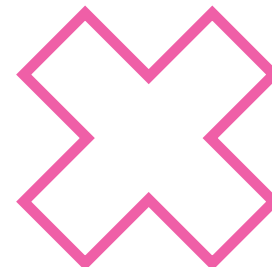
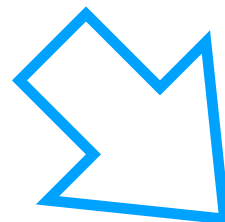
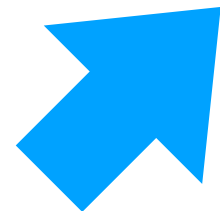
Accessibility



Equations



Web Page



Formalizing visual
properties

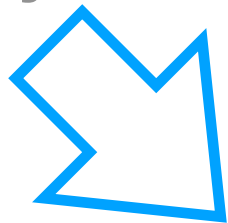
How It Works

Formalize

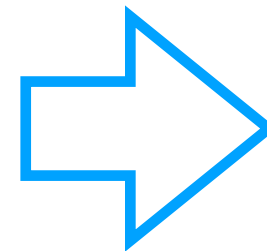
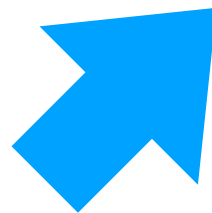
Solve

Scale Up

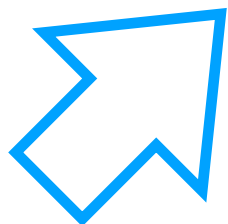
Accessibility



Equations

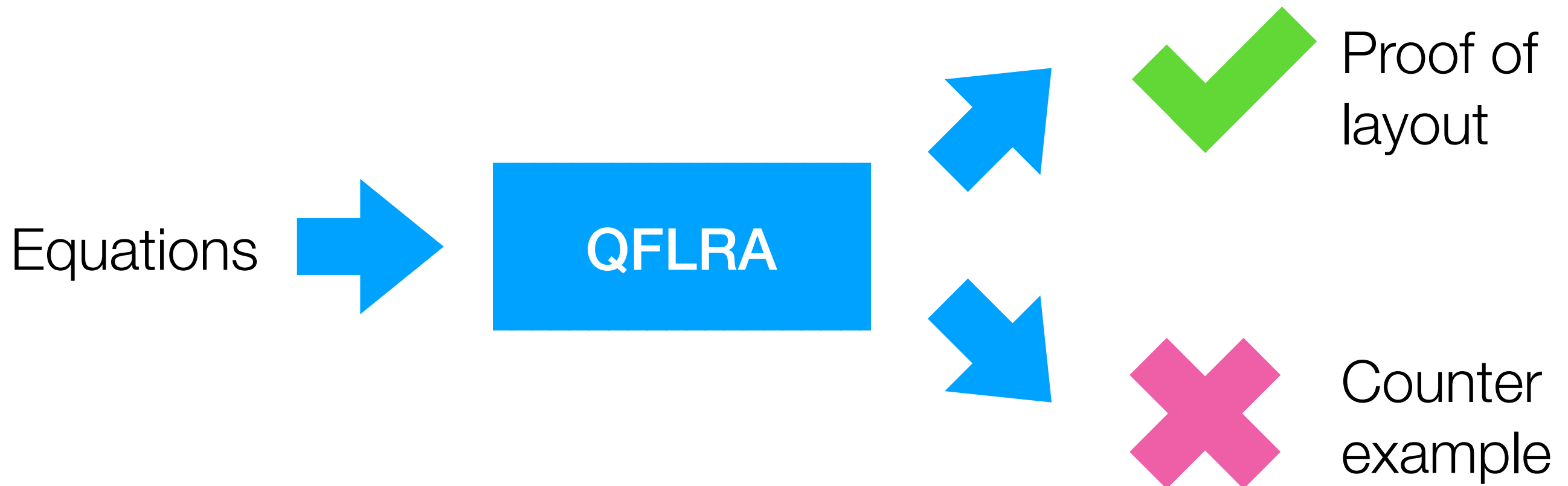


Web Page



Formalizing visual
properties

Solving the Equations

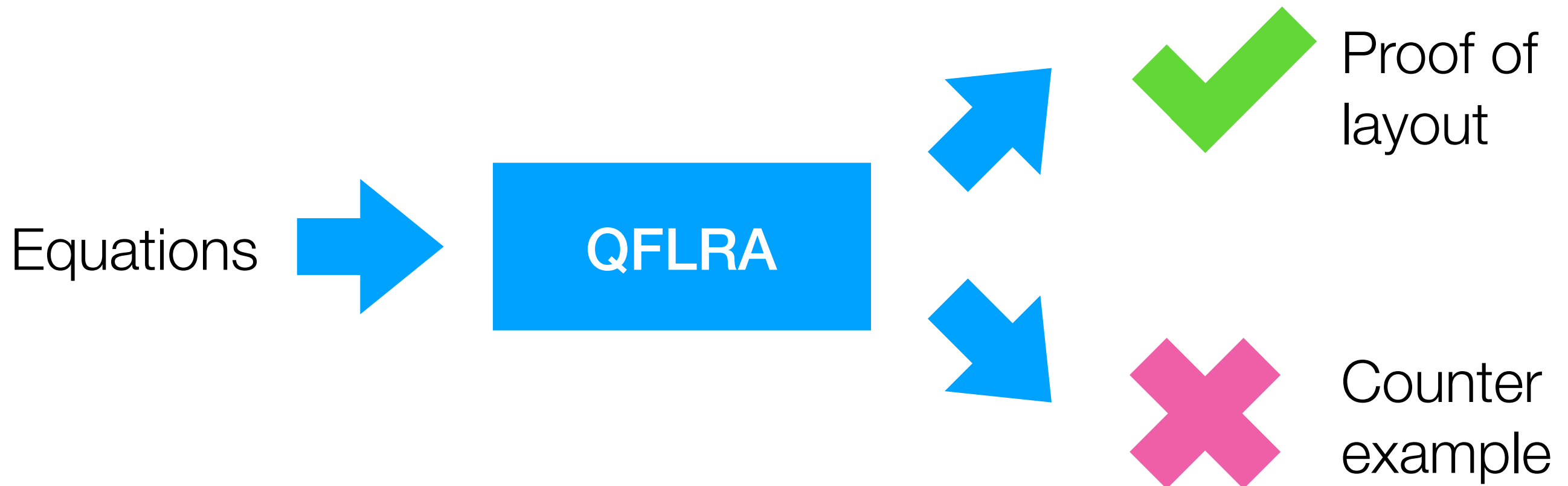


Quantifier **F**ree \longrightarrow No nested loops

Linear \longrightarrow No multiplication

Read **A**rithmetic \longrightarrow No rounding error

Solving the Equations



Simulated Rounding Error

$$a = b \longrightarrow -\varepsilon < a - b < \varepsilon$$

Real Arithmetic 

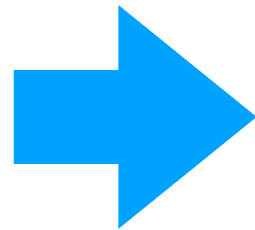
No nested loops

No multiplication

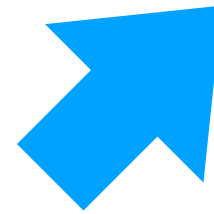
No rounding error

Solving the Equations

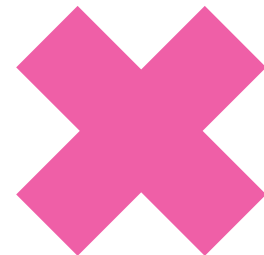
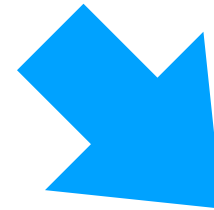
Equations



QFLRA



Proof of layout



Counter example

Simplifying Multiplication

Value-set analysis: $a \in \{2, 3\}$

$$a \times b \rightarrow \begin{cases} 2 \times b & \text{if } a = 2 \\ 3 \times b & \text{if } a = 3 \end{cases}$$

No nested loops

No multiplication

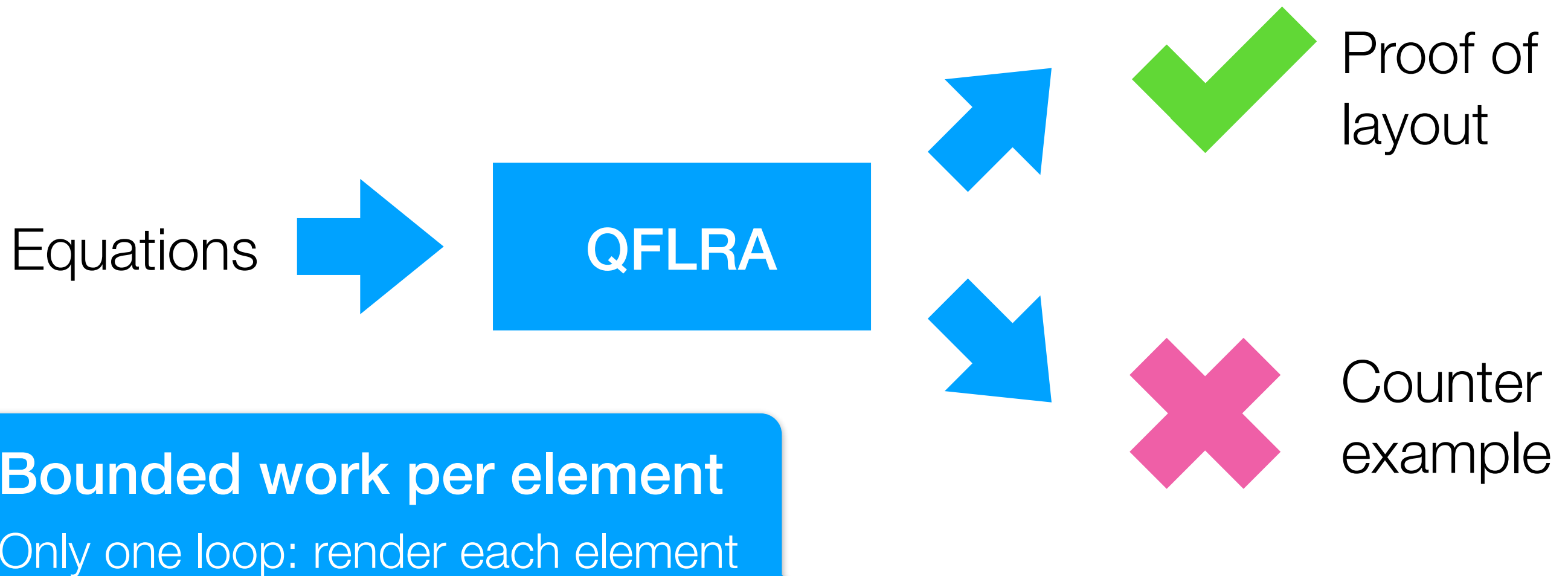
Real Arithmetic



No rounding error



Solving the Equations



Quantifier **F**ree



No nested loops

Linear



No multiplication



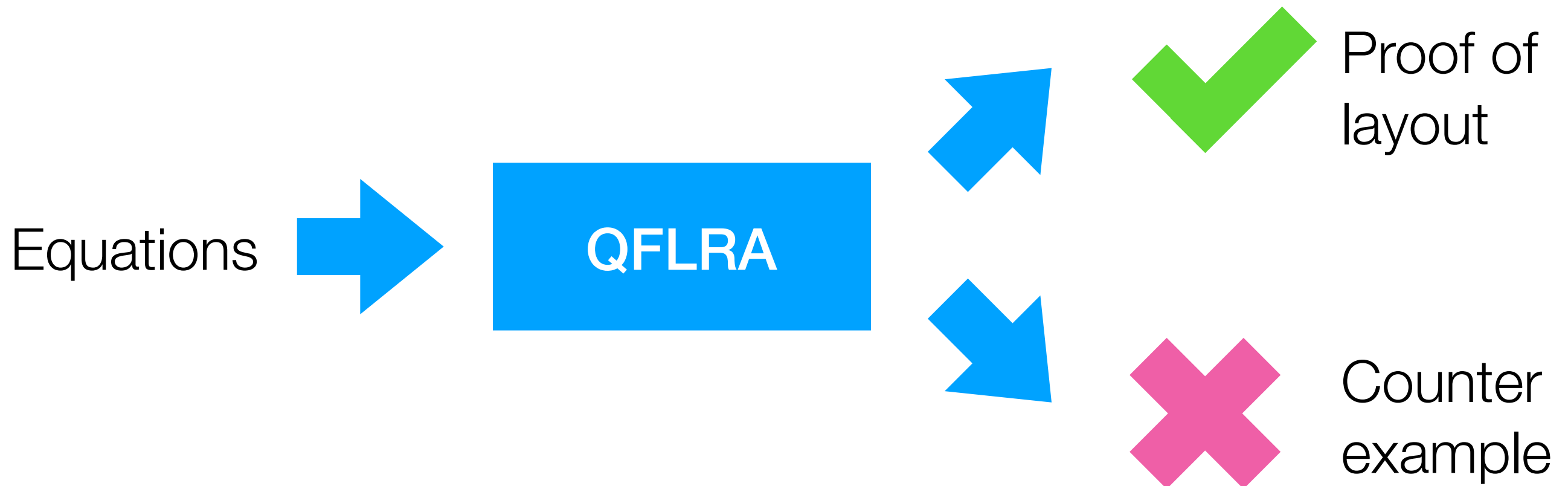
Read **A**rithmetic



No rounding error



Solving the Equations



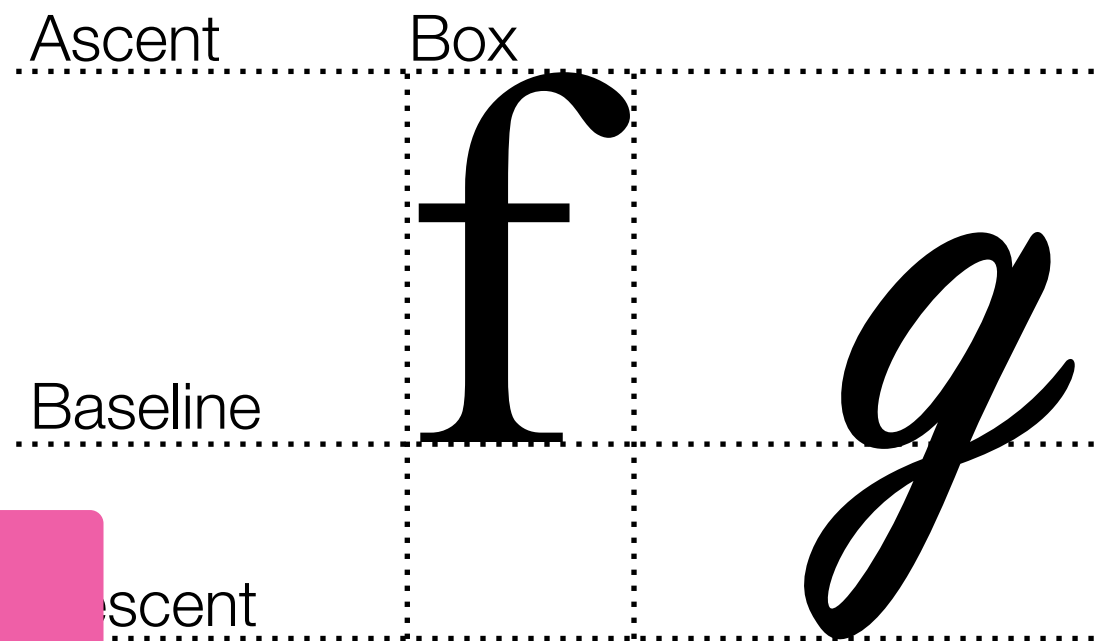
Problem: bounded work per element



Incrementalization, fusion, and unrolling

Inspired by compiler optimizations

Computing Line Height

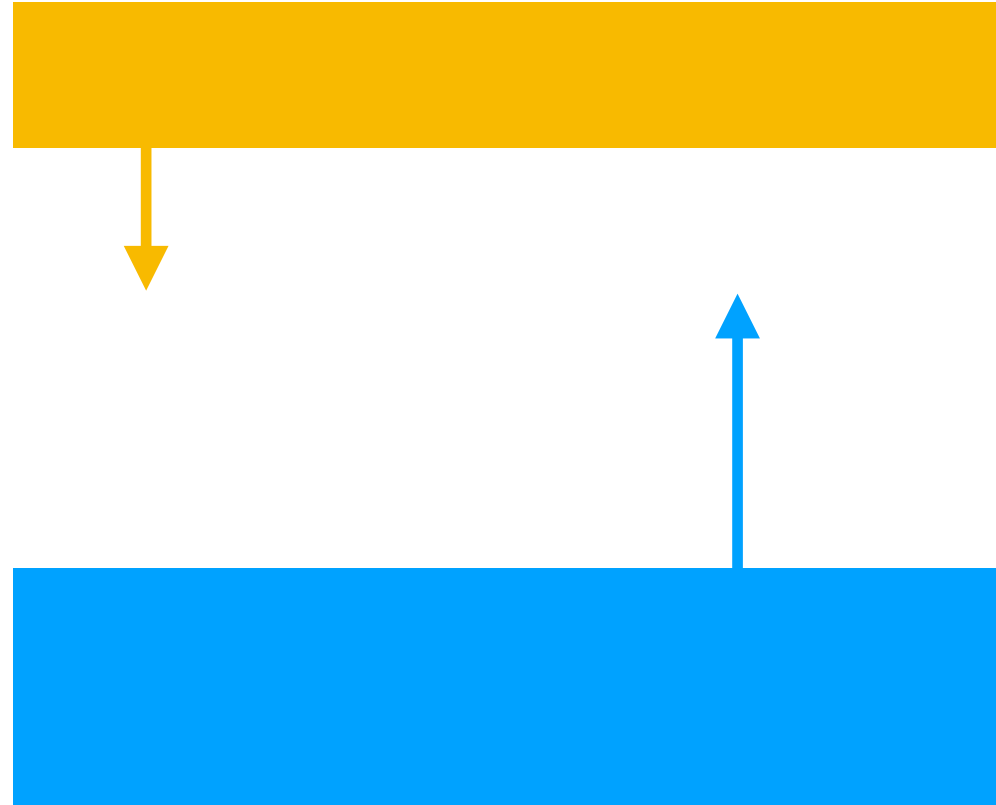


Loop over
elements in line

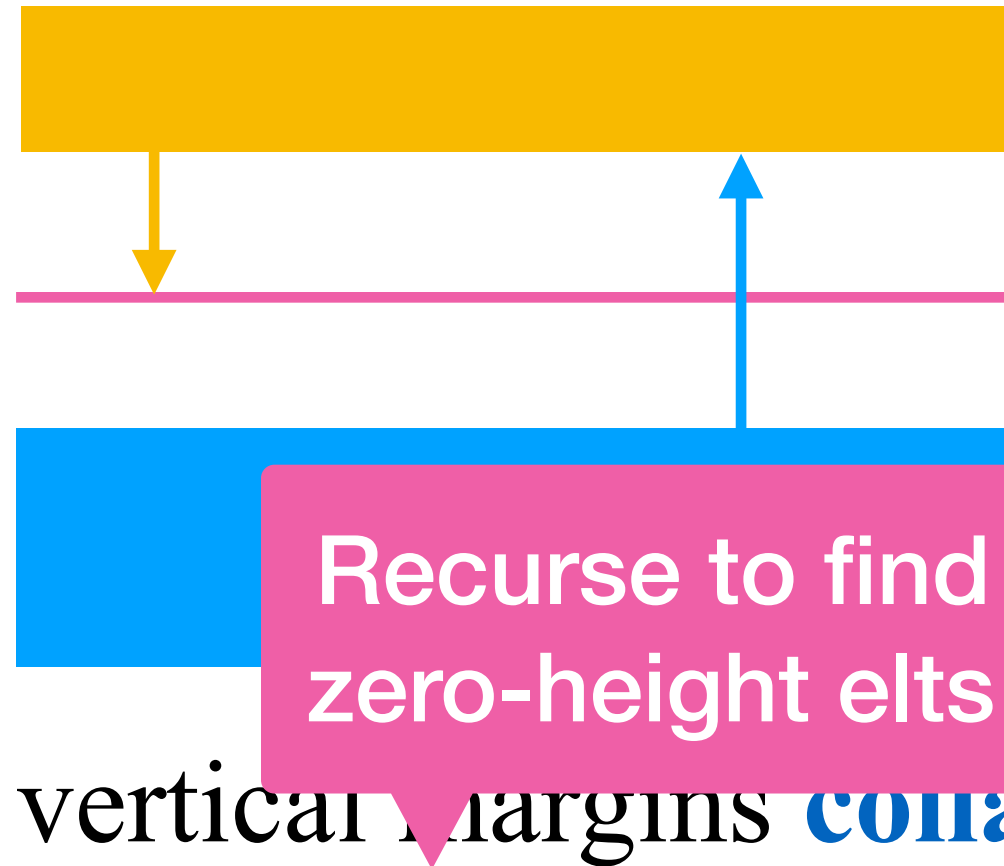
“The line box height is the distance between the **uppermost** box top and the **lowermost** box bottom”

Incrementalization: update running maximum

Computing Margins



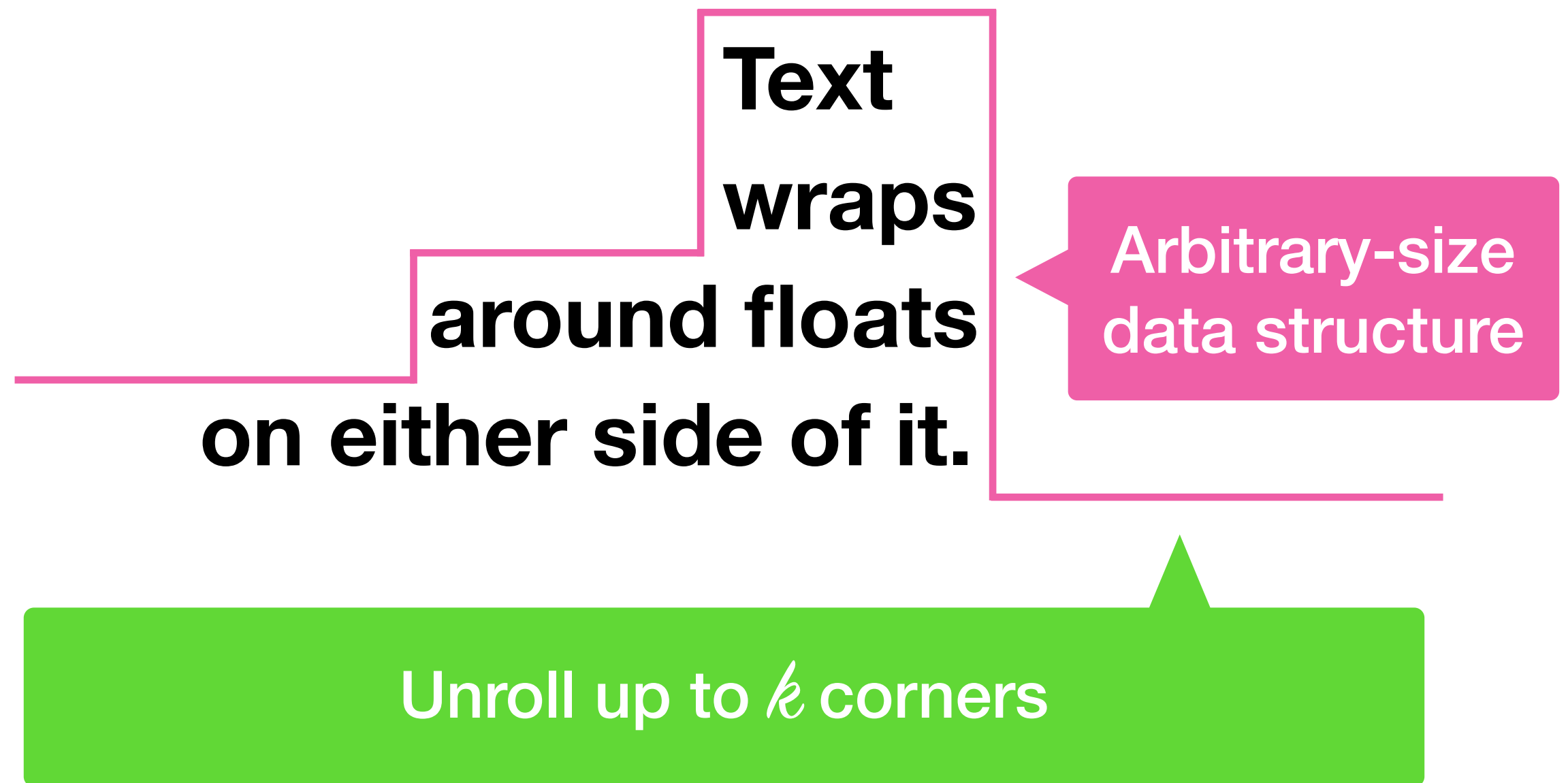
Computing Margins



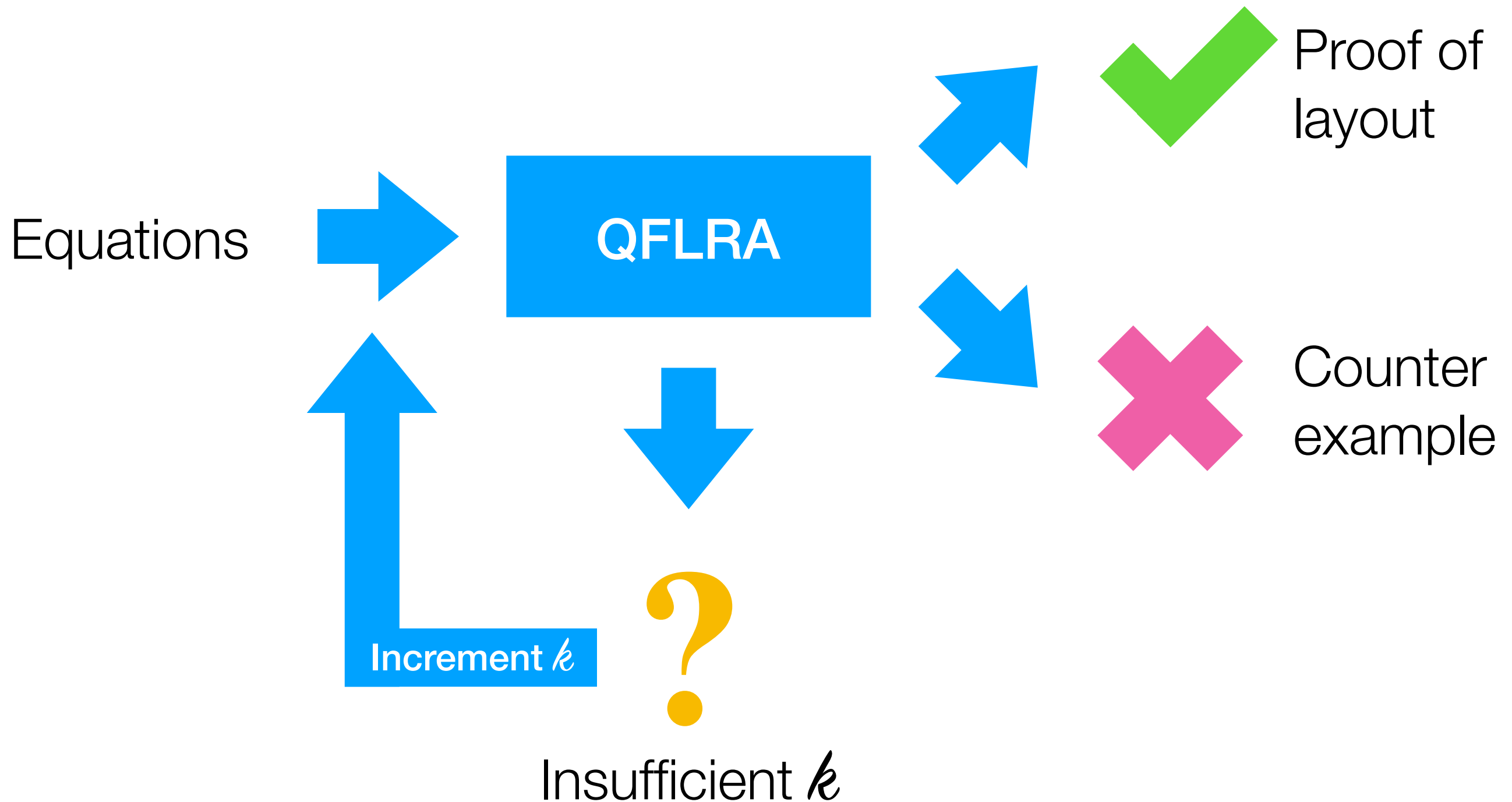
“Adjoining vertical margins **collapse**;
two margins are **adjoining** if and only if ...”

Fusion: interleave with outer render loop

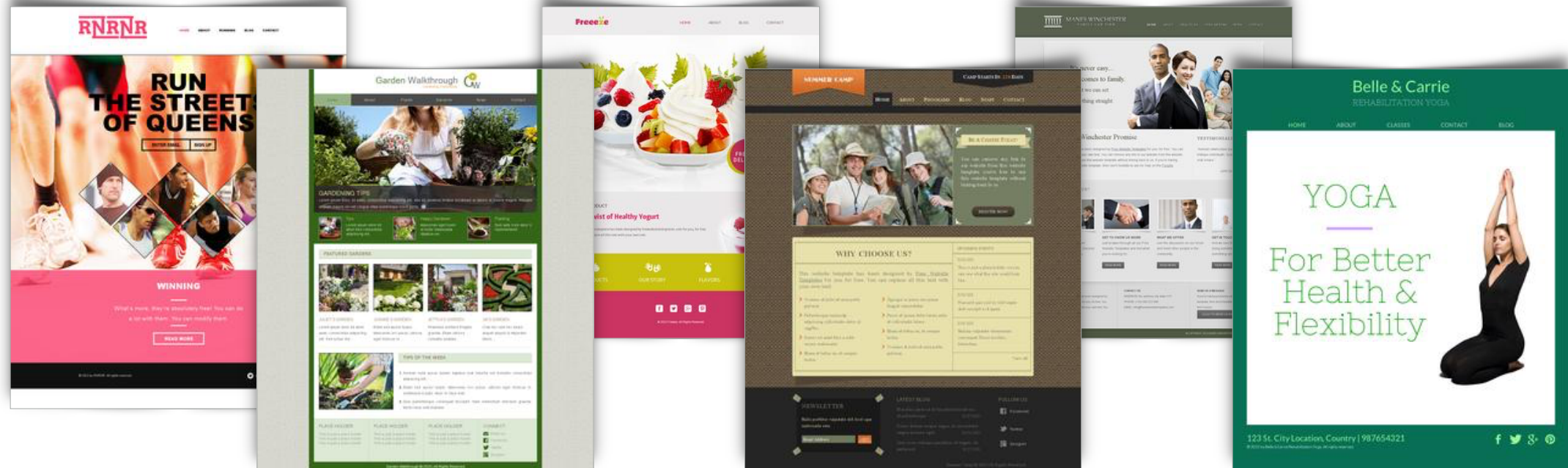
Computing Float Layout



Solving the Equations



Verifying Real Pages



Websites.com

Only use formalized subset of CSS

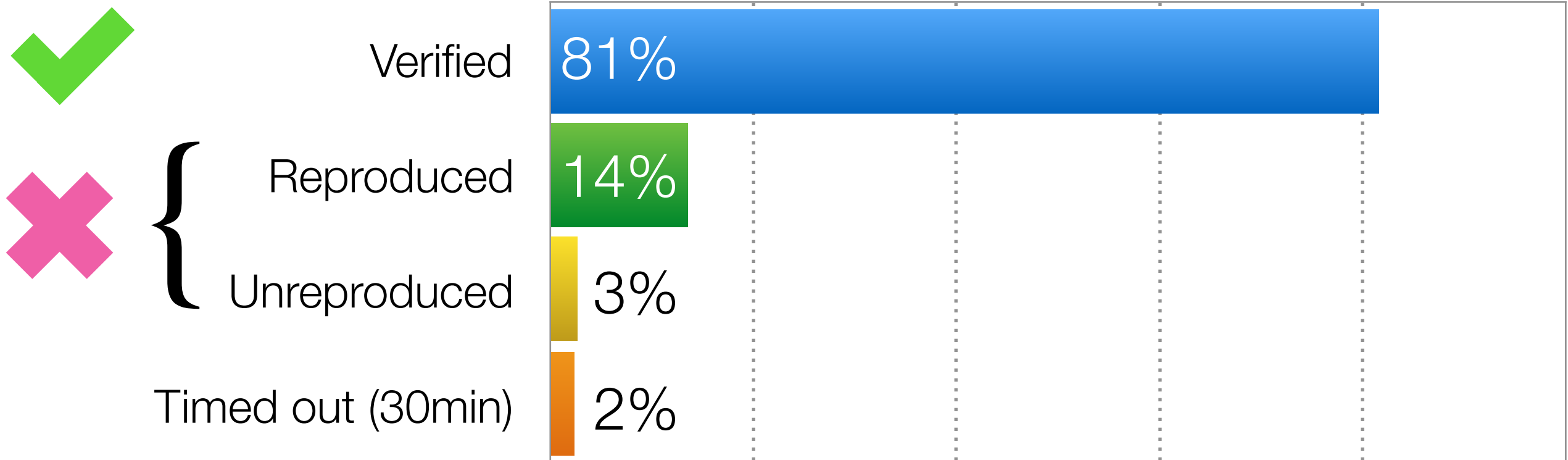
62 web pages

14 properties

476 sensible combinations

From Apple, Google, DOJ accessibility guides

Verifying Real Pages



Evaluate: verified majority of real-world inputs



Found many real accessibility bugs

Few false positives and few timeouts

[PLDI'18]

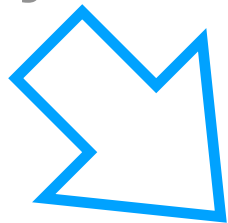
How It Works

Formalize

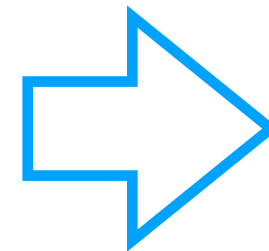
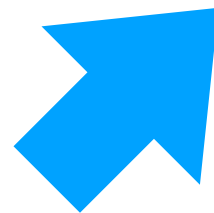
Solve

Scale Up

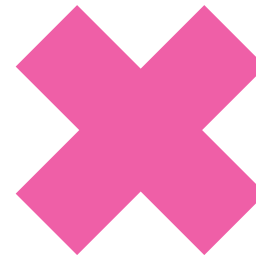
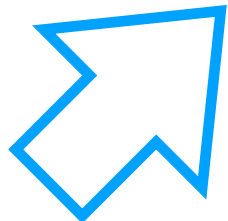
Accessibility



Equations



Web Page



Formalizing visual
properties

Overcoming solver
limitations

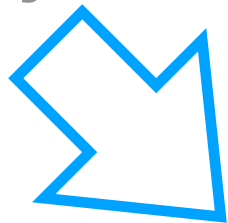
How It Works

Formalize

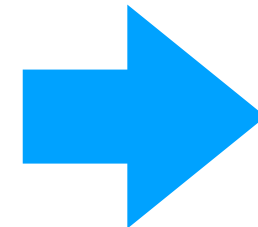
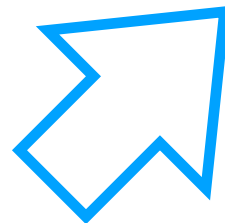
Solve

Scale Up

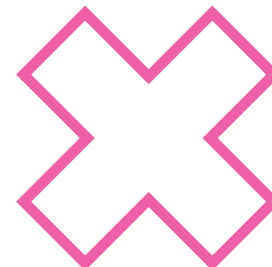
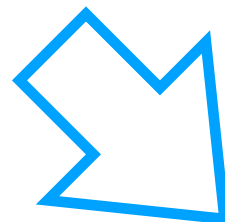
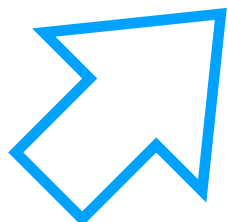
Accessibility



Equations



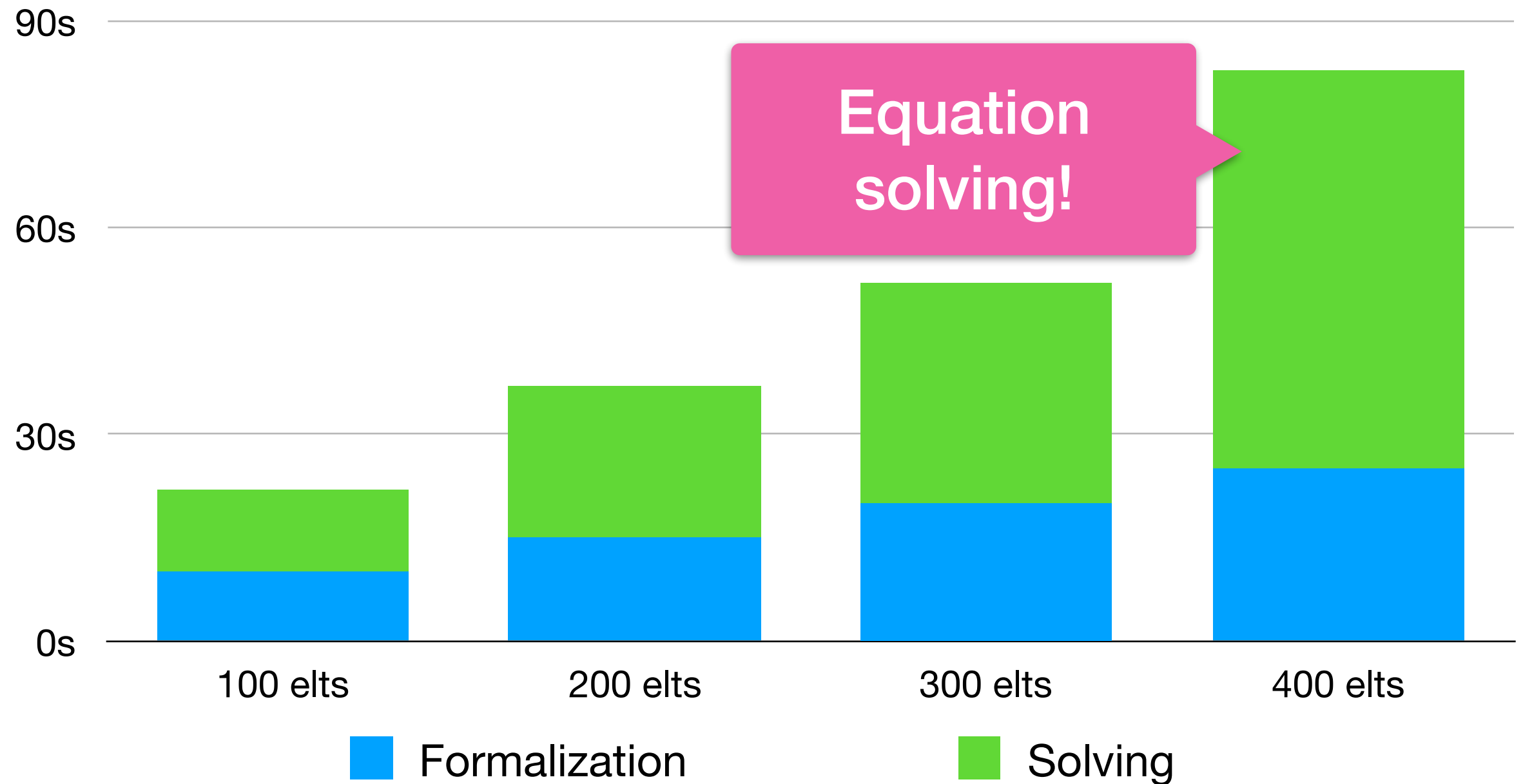
Web Page



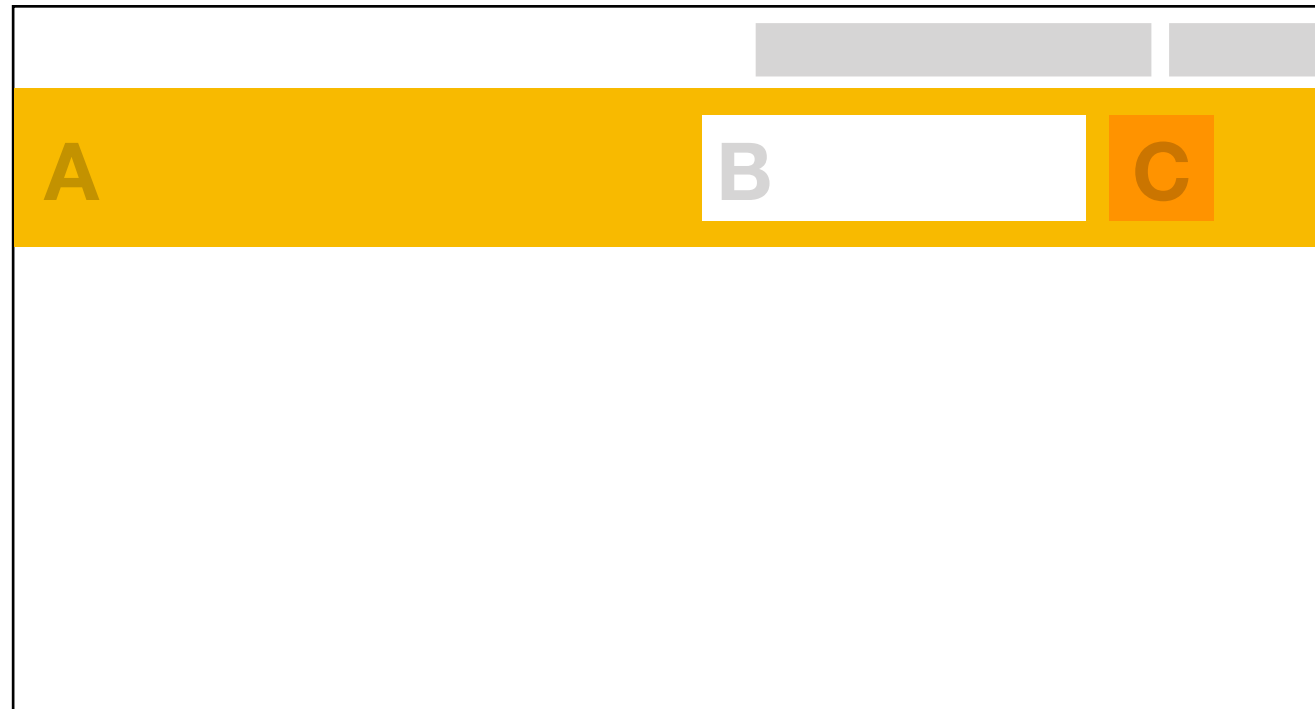
Formalizing visual
properties

Overcoming solver
limitations

Scaling Verification

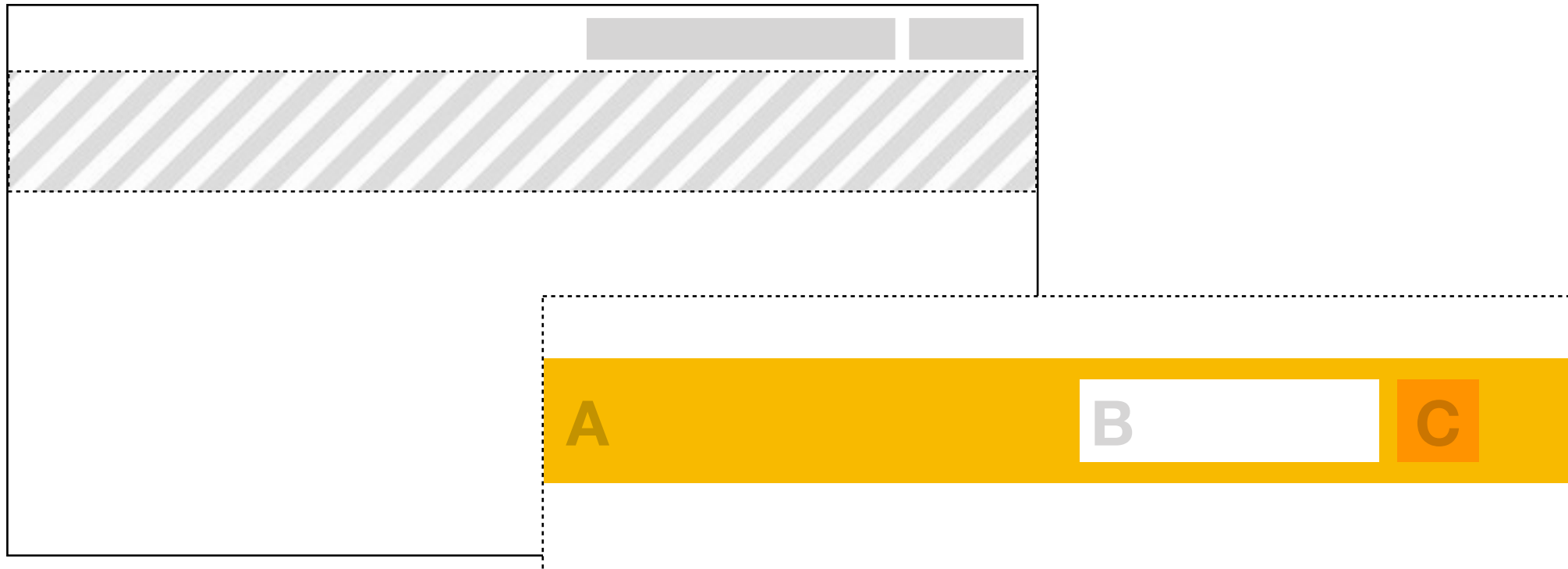


Scaling Verification



Problem: reason about large pages quickly

Scaling Verification



Problem: reason about large pages quickly

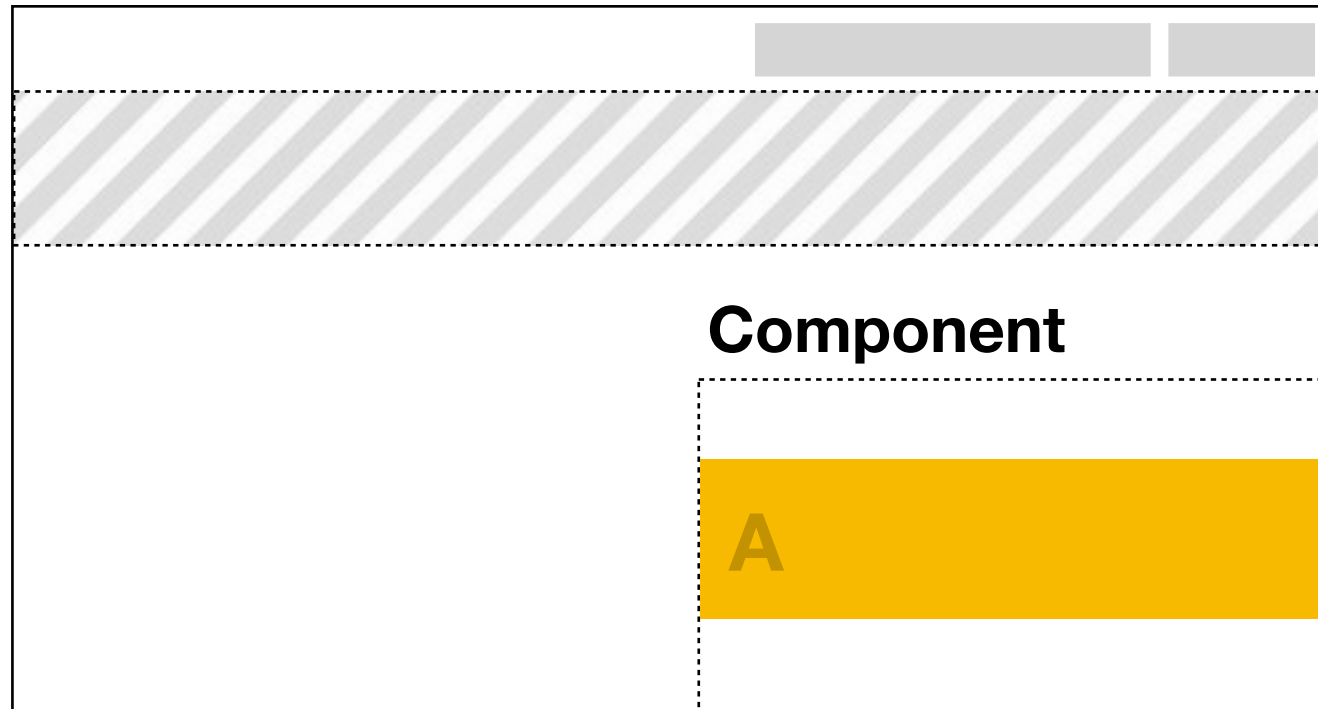


Divide web page into small components

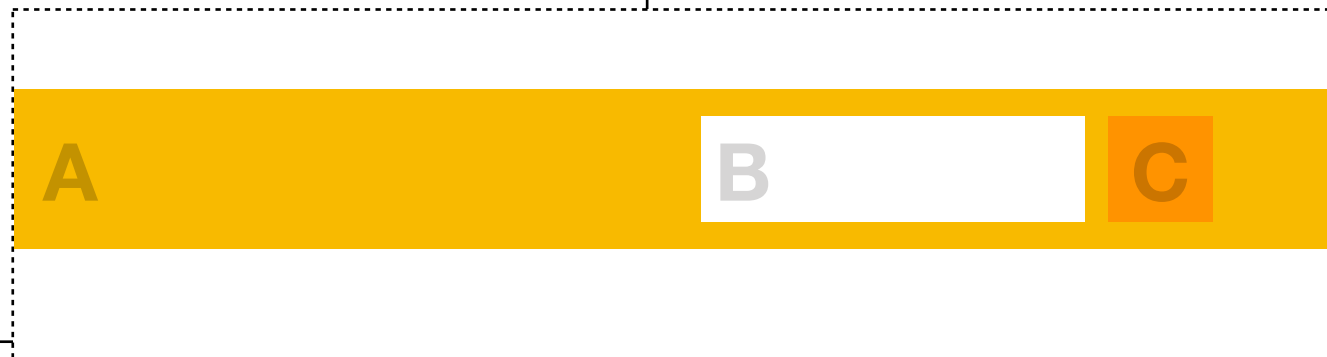
Combine components with rely/guarantee logic

Isolating Components

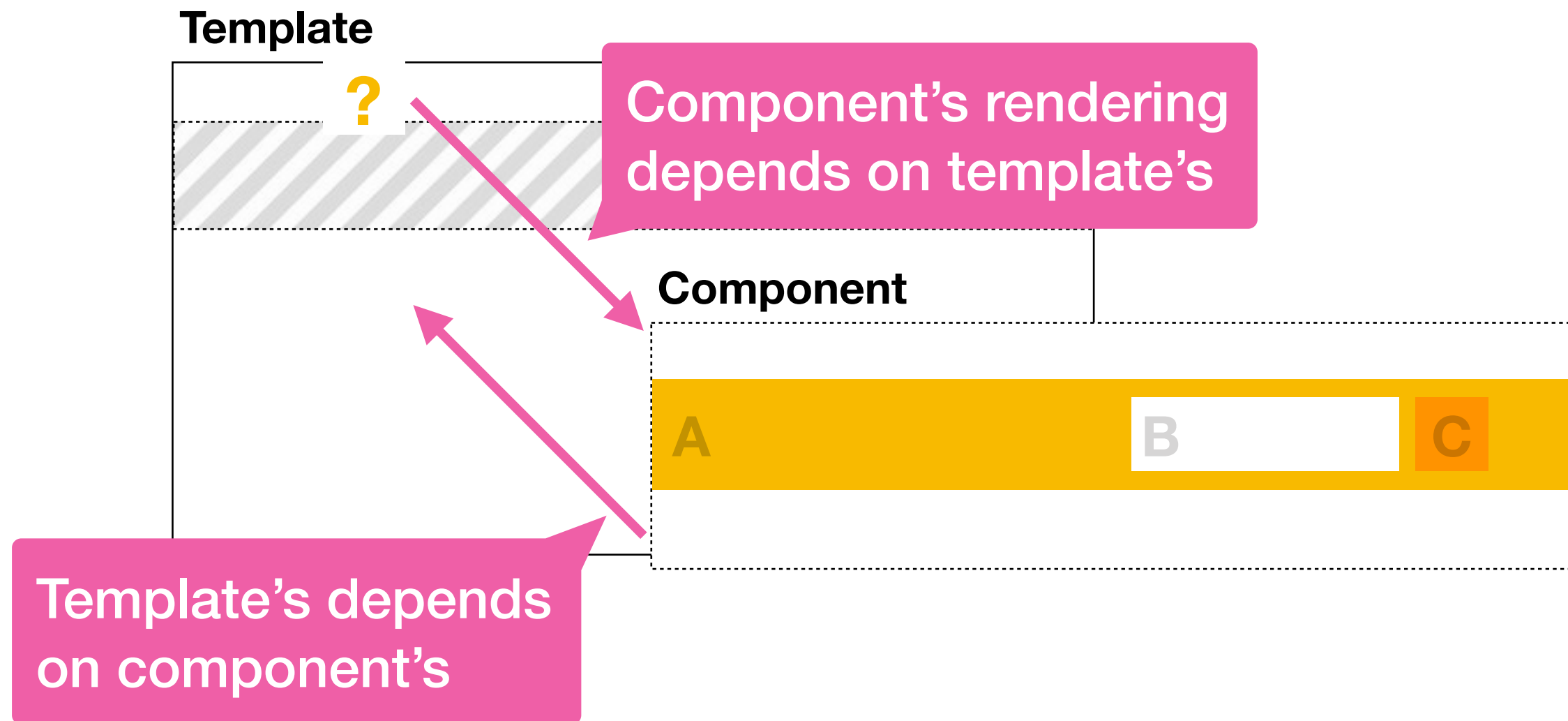
Template



Component

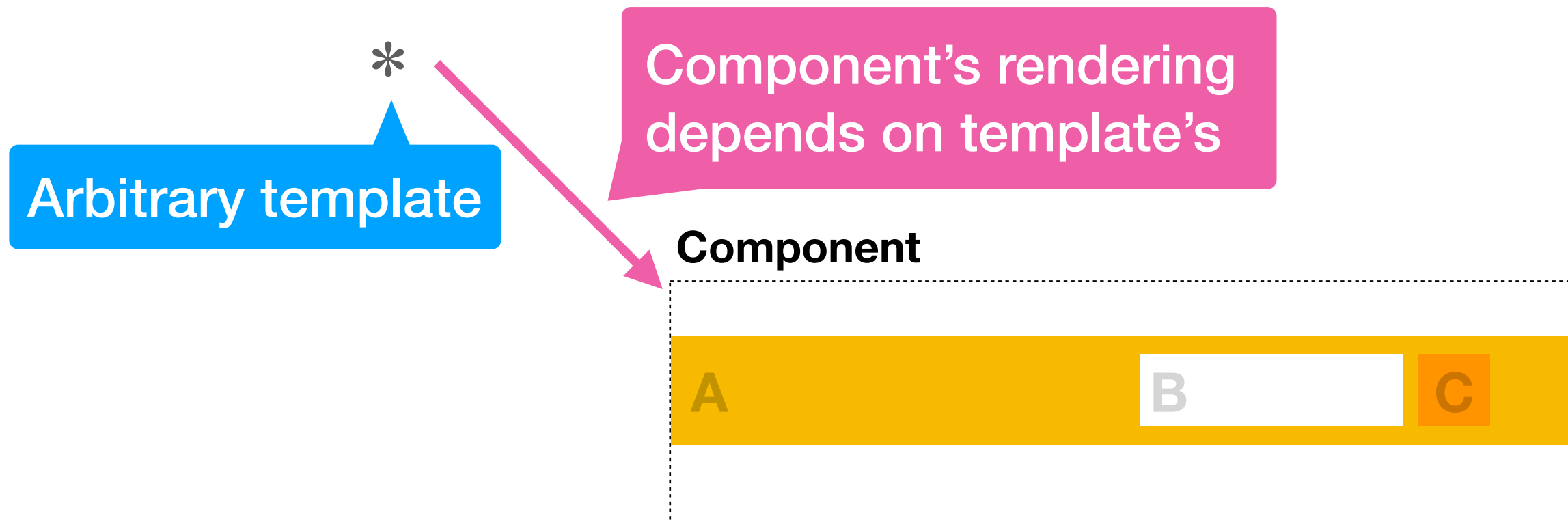


Isolating Components



No module or function boundaries!

Isolating Components



Template layout: part of component configuration

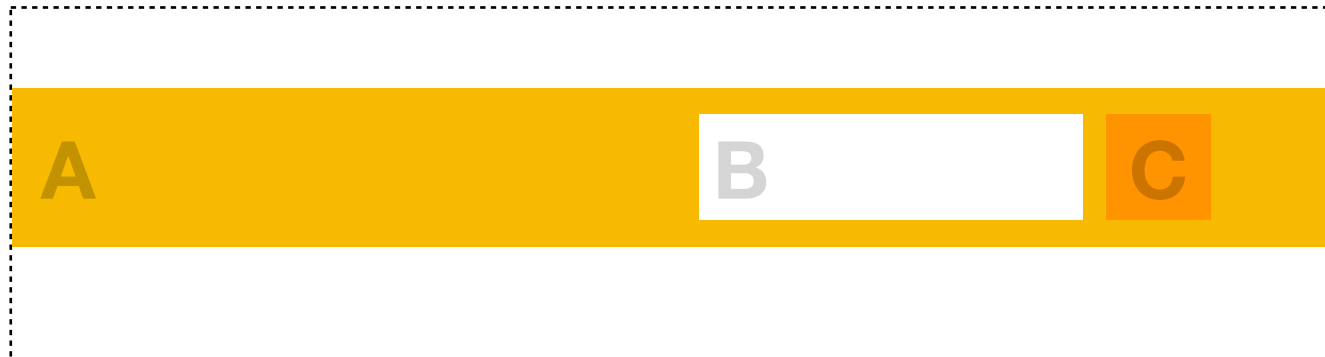
Isolating Components

Precondition

Width available
Current font size
Floating elements

Component's rendering
depends on template's

Component



Template layout: part of component configuration

Rely / Guarantee

Component

Precondition \Rightarrow Specification

Too abstract

- Callout?
- HC.gov example?

Rely / Guarantee

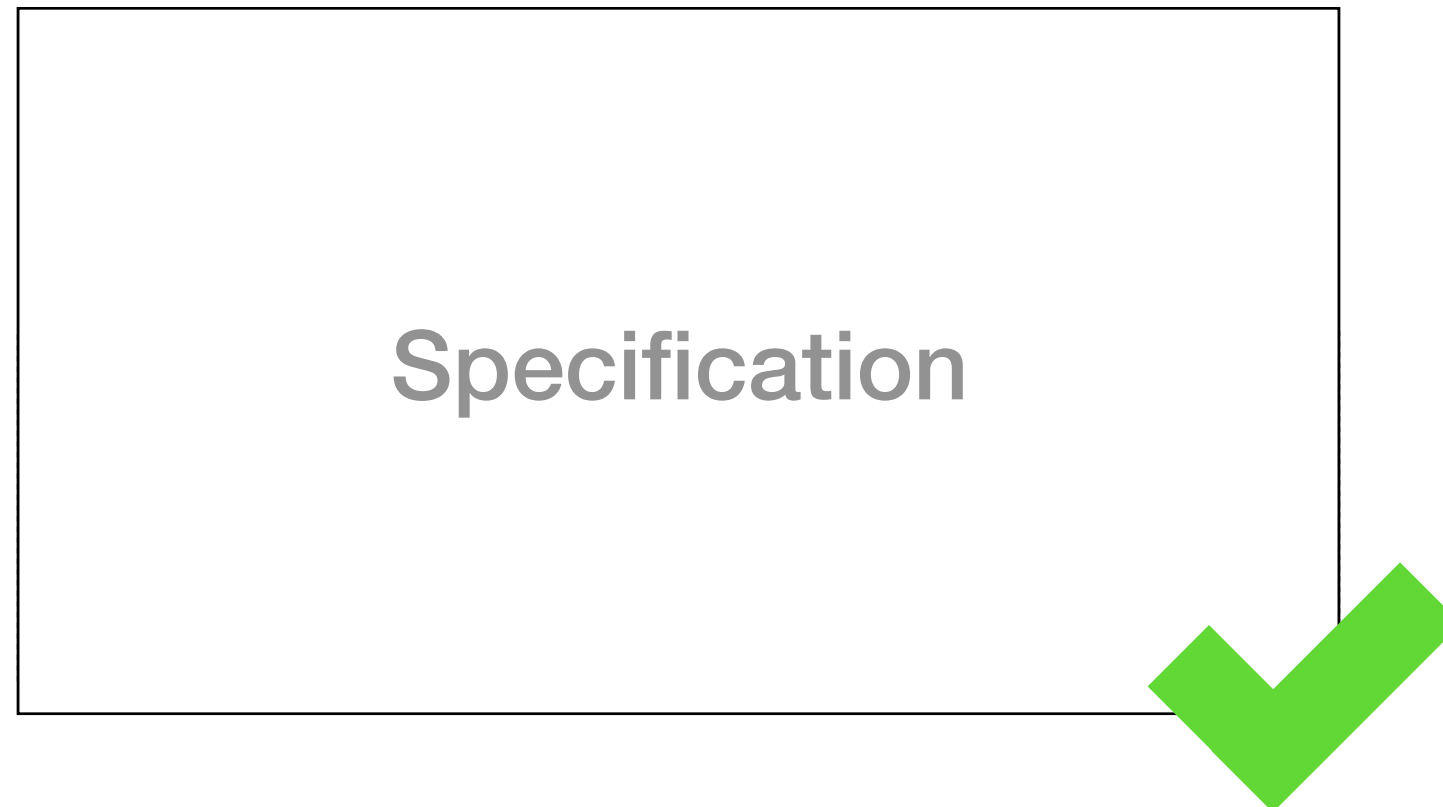
Template

Precondition

Component

Precondition \Rightarrow Specification

Rely / Guarantee

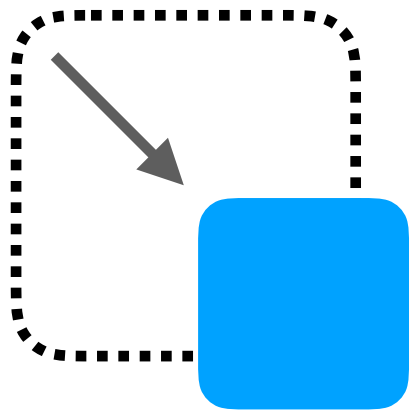


Preconditions checked purely logically

No rendering \Rightarrow fast

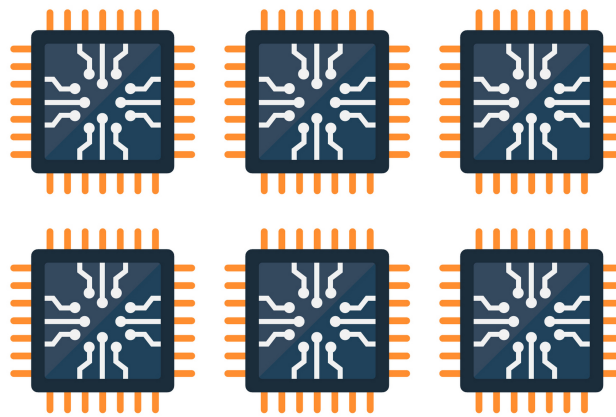
Improving Scale

Problem Size



+

Parallelism



+

Caching



Evaluate: broader class of verified pages



Scaled to 11× larger pages, to 1400× faster

Scaled to multiple pages on one site

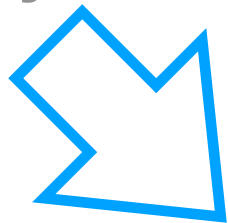
How It Works

Formalize

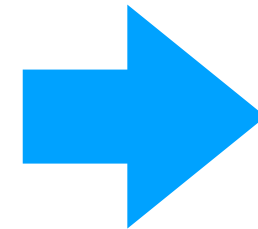
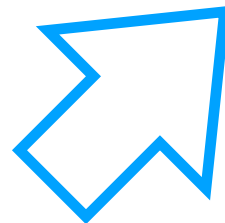
Solve

Scale Up

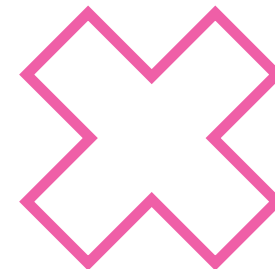
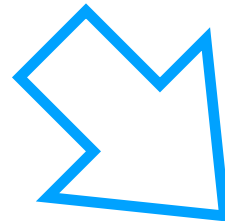
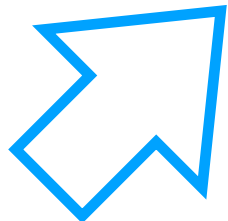
Accessibility



Equations



Web Page



Formalizing visual
properties

Overcoming solver
limitations

Finding modularity
for rely/guarantee

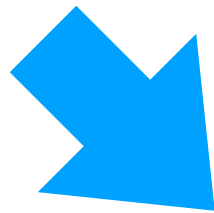
How It Works

Formalize

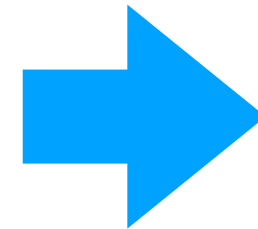
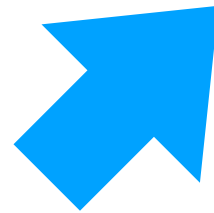
Solve

Scale Up

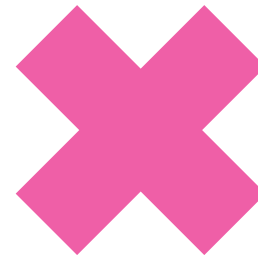
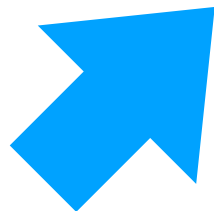
Accessibility



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Where We're Going

From Logic to Programs

Three Parts



Write a
specification

Propagate
into program

Scale to
systems

Program Reasoning

How to **define / write** a programming language

Syntax, two types of semantics, and interpretation

Symbolic execution of program expressions

Dealing with function calls, conditionals, and feasibility

Changes in state due to program statements

Hoare logic, invariants, and termination

Next class:

Symbolic Execution

To do:

- ☐ Course feedback
- ☐ Project Proposal