

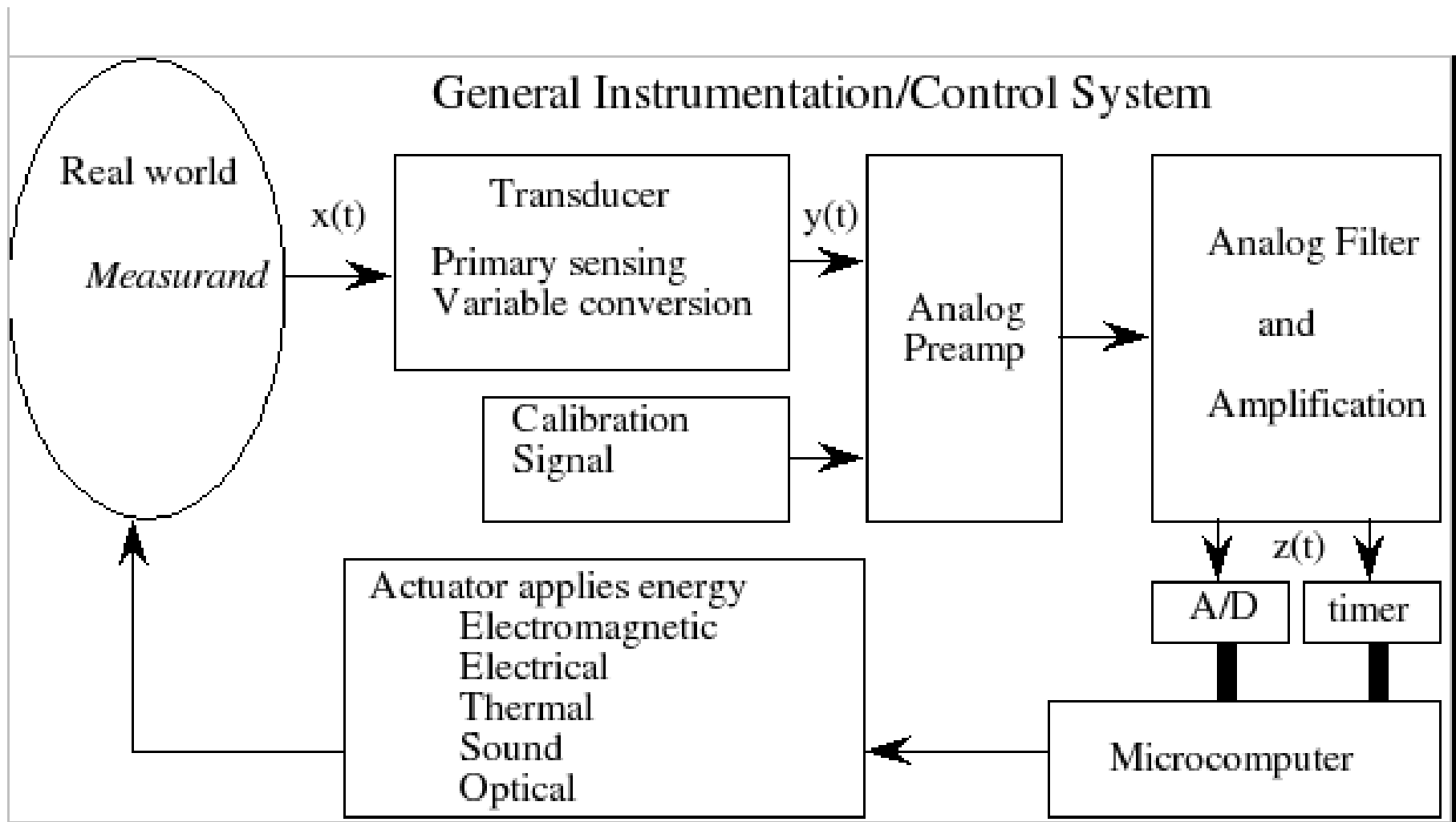
Today

- ◆ **Data acquisition**
- ◆ **Digital filters and signal processing**
 - **Filter examples and properties**
 - **FIR filters**
 - **Filter design**
 - **Implementation issues**
 - **DACs**
 - **PWM**

Data Acquisition Systems

- ◆ **Many embedded systems measure quantities from the environment and turn them into bits**
 - These are data acquisition systems (DAS)
 - This is fundamental
- ◆ **Sometimes data acquisition is the main idea**
 - Digital thermometer
 - Digital camera
 - Volt meter
 - Radar gun
- ◆ **Other times DAS is mixed with other functionality**
 - Digital signal processing
 - Networking, storage
 - Feedback control

Big Picture



Why Care About DAS?



- ◆ July 1983: Air Canada 143, a Boeing 767, runs out of fuel in mid-air, lands on “abandoned” runway
- ◆ Poorly soldered fuel level sensor + mistakes that defeated backup systems

Accuracy

- ◆ **Instrument accuracy** is the absolute error of the entire system, including transducer, electronics, and software
- ◆ Let x_{mi} be measured value and x_{ti} be the true value

- ◆ **Average accuracy:**
$$\frac{1}{n} \sum_{i=1}^n |x_{ti} - x_{mi}|$$

- ◆ **Average accuracy of reading:**
$$\frac{100}{n} \sum_{i=1}^n \frac{|x_{ti} - x_{mi}|}{x_{ti}}$$

- ◆ **Average accuracy of full scale:**
$$\frac{100}{n} \sum_{i=1}^n \frac{|x_{ti} - x_{mi}|}{x_{tmax}}$$

More Accuracy

◆ **Maximum error:** $\max |x_{ti} - x_{mi}|$

◆ **Maximum error of reading:** $100 \max \frac{|x_{ti} - x_{mi}|}{x_{ti}}$

◆ **Maximum error of full scale:** $100 \max \frac{|x_{ti} - x_{mi}|}{x_{tmax}}$

Resolution

- ◆ **Instrument resolution is the smallest input signal difference that can be detected by the entire system**
 - **May be limited by noise in either transducer or electronics**

- ◆ **Spatial resolution of the transducer is the smallest distance between two independent measurements**
 - **Determined by size and mechanical properties of the transducer**

Precision

- ◆ Precision is number of distinguishable alternatives, n_x , from which result is selected
- ◆ Can be expressed in bits or decimal digits
 - 1000 alternatives: 10 bits, 3 decimal digits
 - 2000 alternatives: 11 bits, 3.5 decimal digits
 - 4000 alternatives: 12 bits, 3.75 decimal digits
 - 10000 alternatives: >13 bits, 4 decimal digits
- ◆ Range is resolution times precision: $r_x = \Delta x n_x$

Reproducibility

- ◆ ***Reproducibility* specifies whether the instrument has equal outputs given identical inputs over some time period**
- ◆ **Specified as full range or standard deviation of output results given a fixed input**
- ◆ **Reproducibility errors often come from transducer drift**

ADC: How many bits?

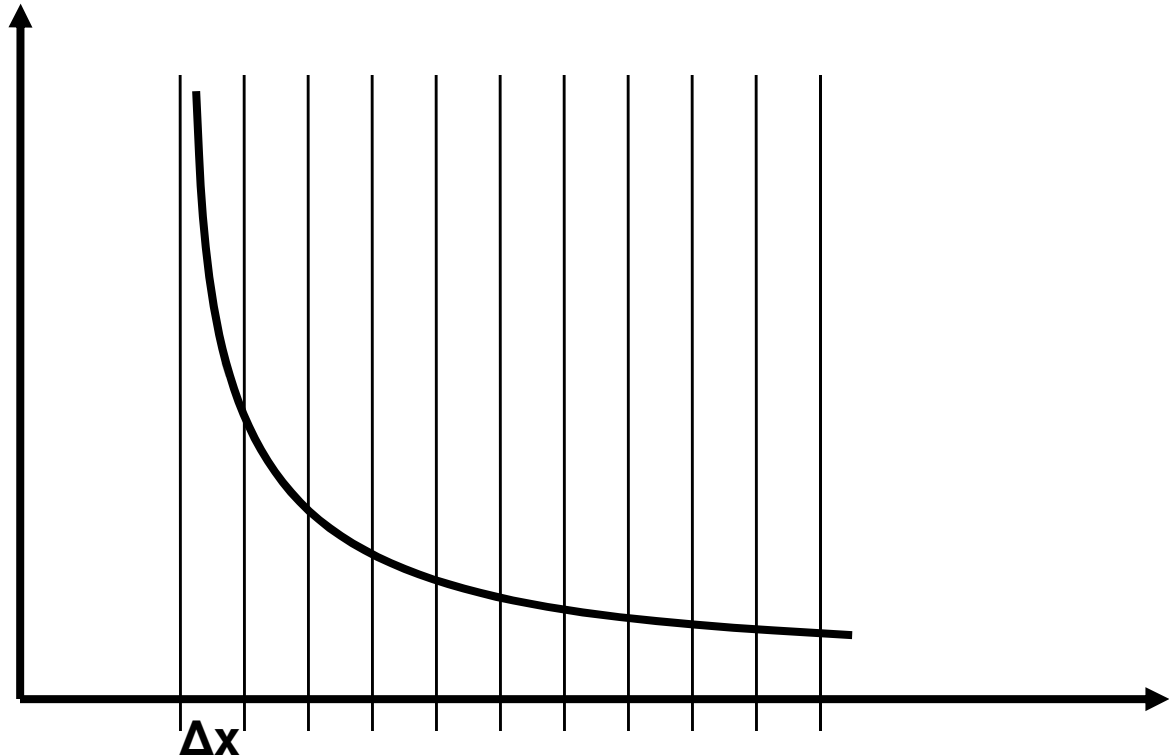
◆ Linear transducer case:

- ADC resolution must be \geq problem resolution

◆ Nonlinear transducer case:

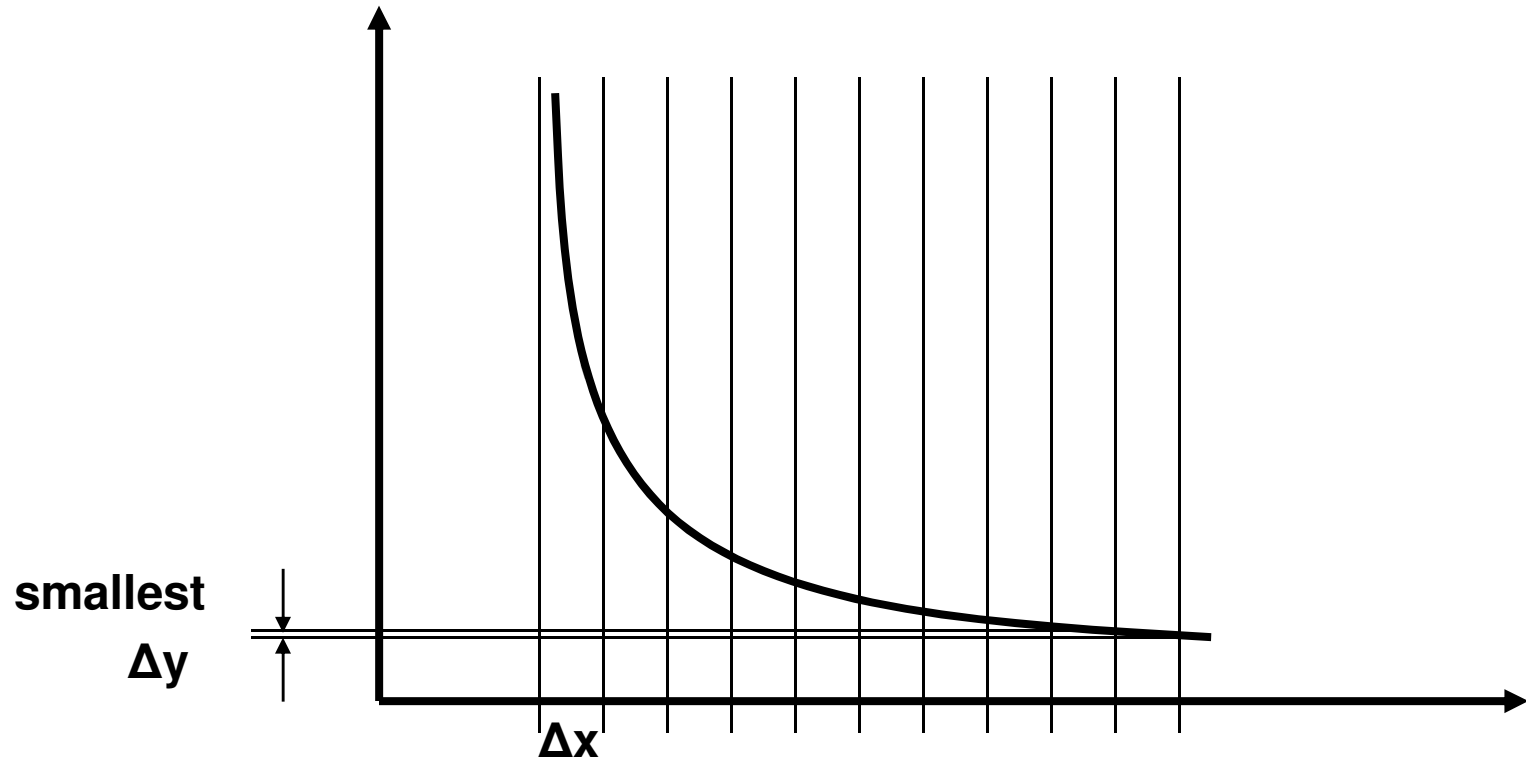
- Let x be the real-world signal with range r_x
- Let y be the transducer output with range r_y
- Let the required precision of x be n_x
- Resolutions of x and y are Δx and Δy
- Transducer response described by $y=f(x)$
- Required ADC precision n_y (number of alternatives) is:
 - $\Delta x = r_x/n_x$
 - $\Delta y = \min \{ f(x + \Delta x) - f(x) \}$ for all x in r_x
- Bits is $\text{ceiling}(\log_2 n_y)$

ADC: How many bits?



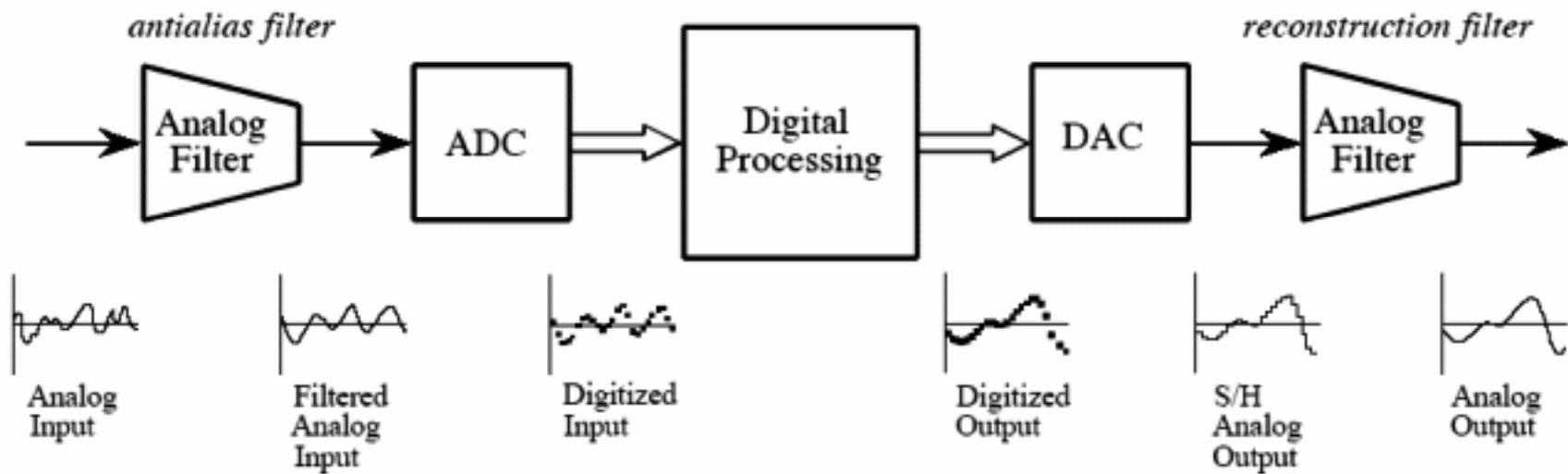
- ◆ ADC must be able to measure a change in voltage of the smallest Δy

ADC: How many bits?



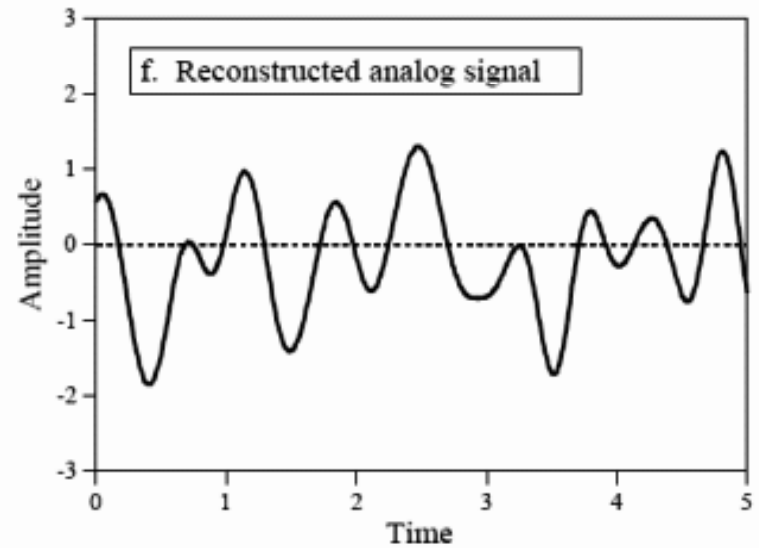
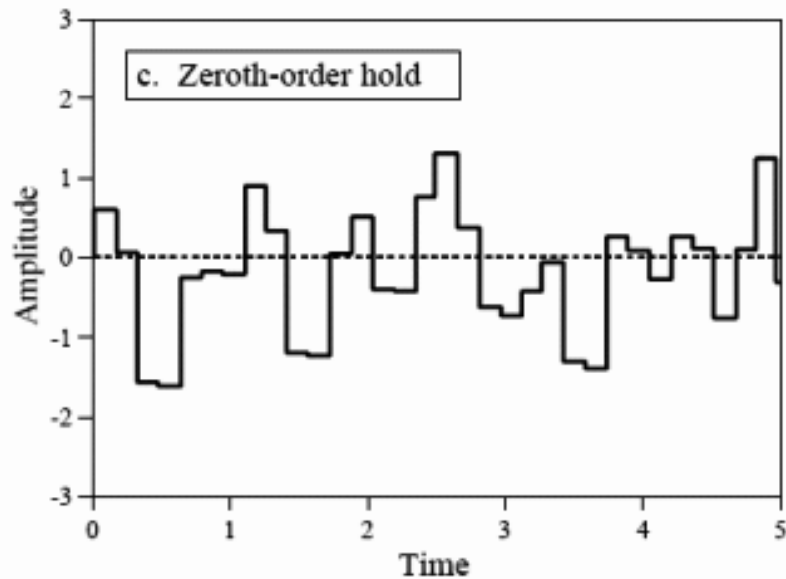
- ◆ ADC must be able to measure a change in voltage of the smallest Δy

DSP Big Picture



Signal Reconstruction

- ◆ Analog filter gets rid of unwanted high-frequency components in the output



Data Acquisition

- ◆ **Signal: Time-varying measurable quantity whose variation normally conveys information**
 - Quantity often a voltage obtained from some transducer
 - E.g. a microphone
- ◆ **Analog signals have infinitely variable values at all times**
- ◆ **Digital signals are discrete in time and in value**
 - Often obtained by sampling analog signals
 - Sampling produces sequence of numbers
 - E.g. { ... , $x[-2]$, $x[-1]$, $x[0]$, $x[1]$, $x[2]$, ... }
 - These are time domain signals

Sampling

◆ Transducers

- Transducer turns a physical quantity into a voltage
- ADC turns voltage into an n -bit integer
- Sampling is typically performed periodically
- Sampling permits us to reconstruct signals from the world
 - E.g. sounds, seismic vibrations

◆ Key issue: *aliasing*

- *Nyquist rate*: $0.5 * \text{sampling rate}$
- Frequencies higher than the Nyquist rate get mapped to frequencies below the Nyquist rate
- Aliasing cannot be undone by subsequent digital processing

Sampling Theorem

- ◆ **Discovered by Claude Shannon in 1949:**

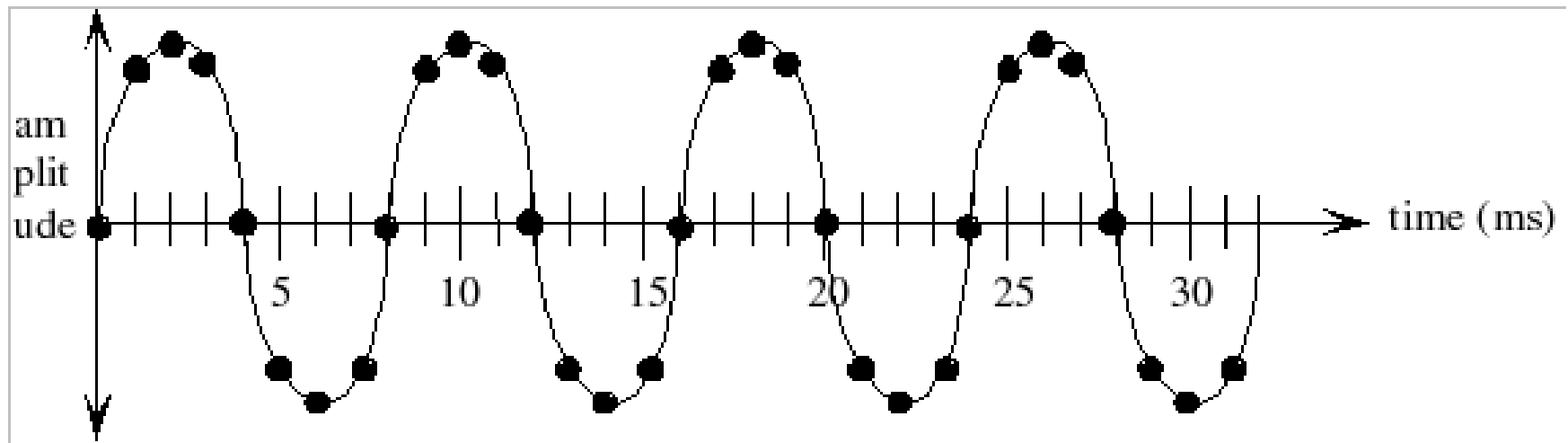
A signal can be reconstructed from its samples without loss of information, if the original signal has no frequencies above $1/2$ the sampling frequency

- ◆ **This is a pretty amazing result**
 - **But note that it applies only to discrete time, not discrete values**

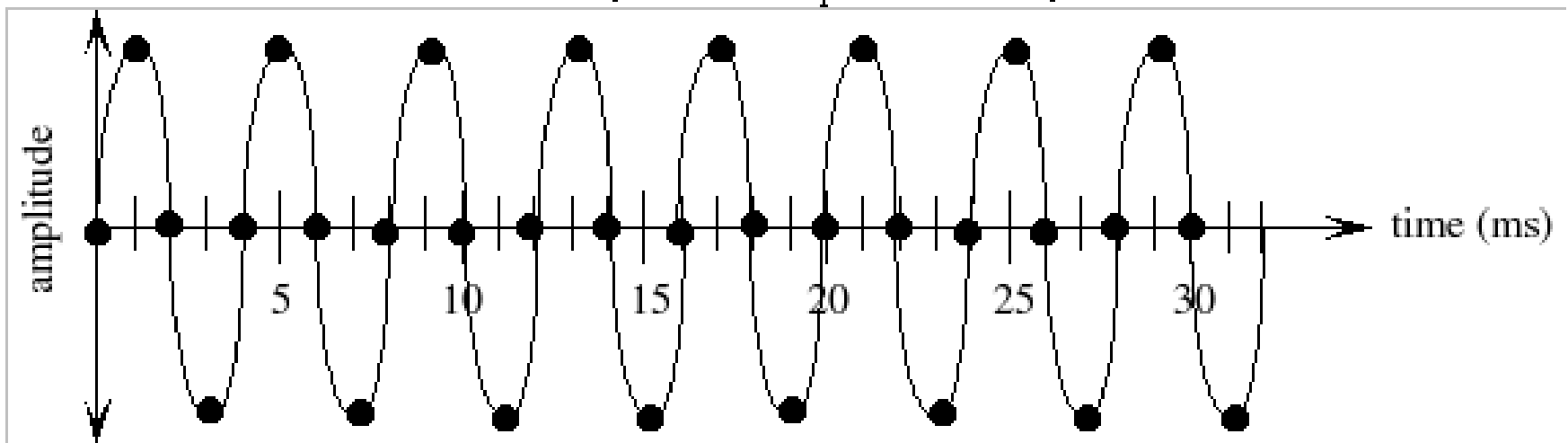
Aliasing Details

- ◆ Let N be the sampling rate and F be a frequency found in the signal
 - Frequencies between 0 and $0.5*N$ are sampled properly
 - Frequencies $>0.5*N$ are aliased
 - Frequencies between $0.5*N$ and N are mapped to $(0.5*N)-F$ and have phase shifted 180°
 - Frequencies between N and $1.5*N$ are mapped to $f-N$ with no phase shift
 - Pattern repeats indefinitely
- ◆ Aliasing may or may not occur when $N == F*2*X$ where X is a positive integer

No Aliasing

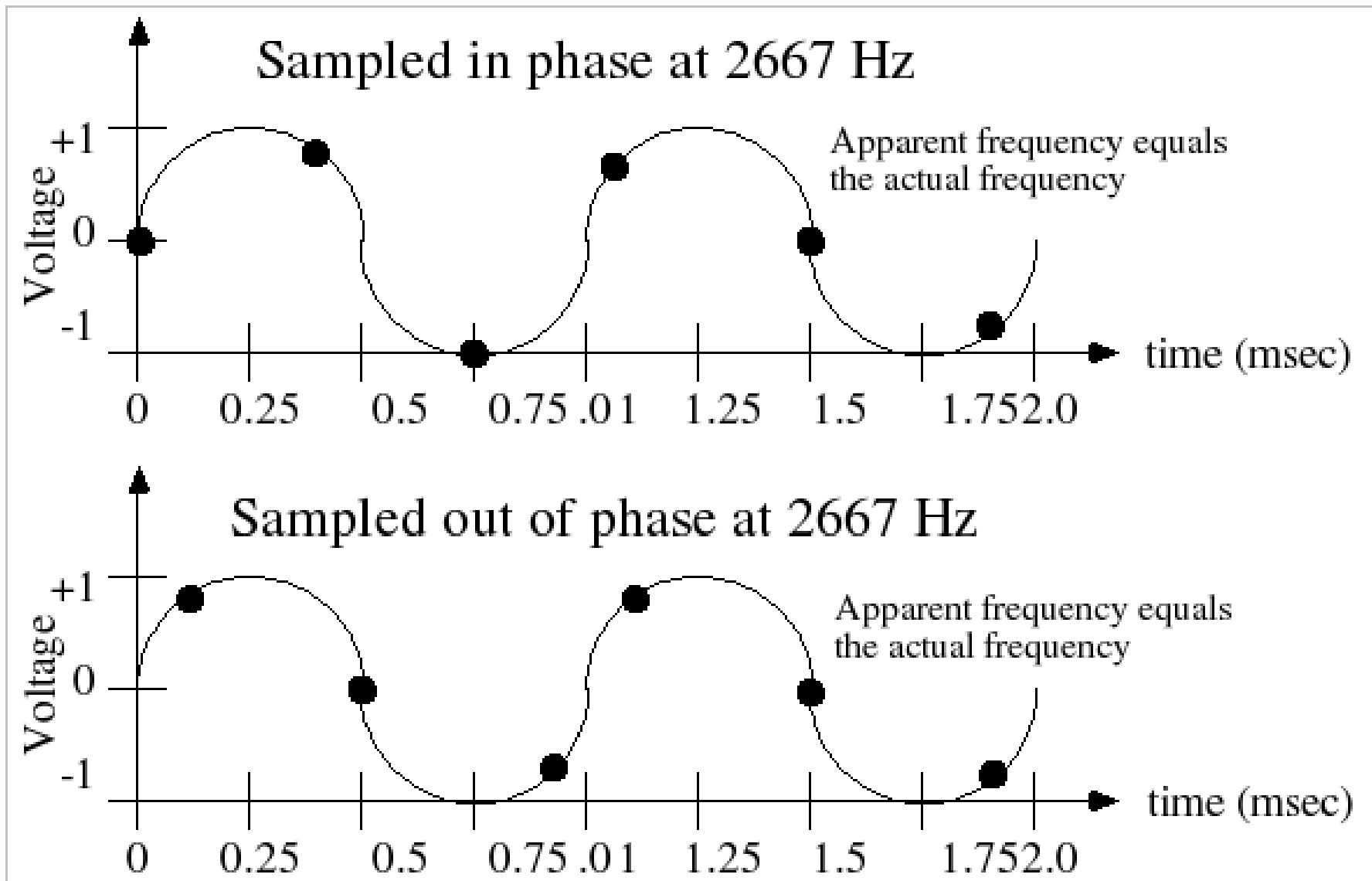


125 Hz sin wave sampled at 1000 Hz.

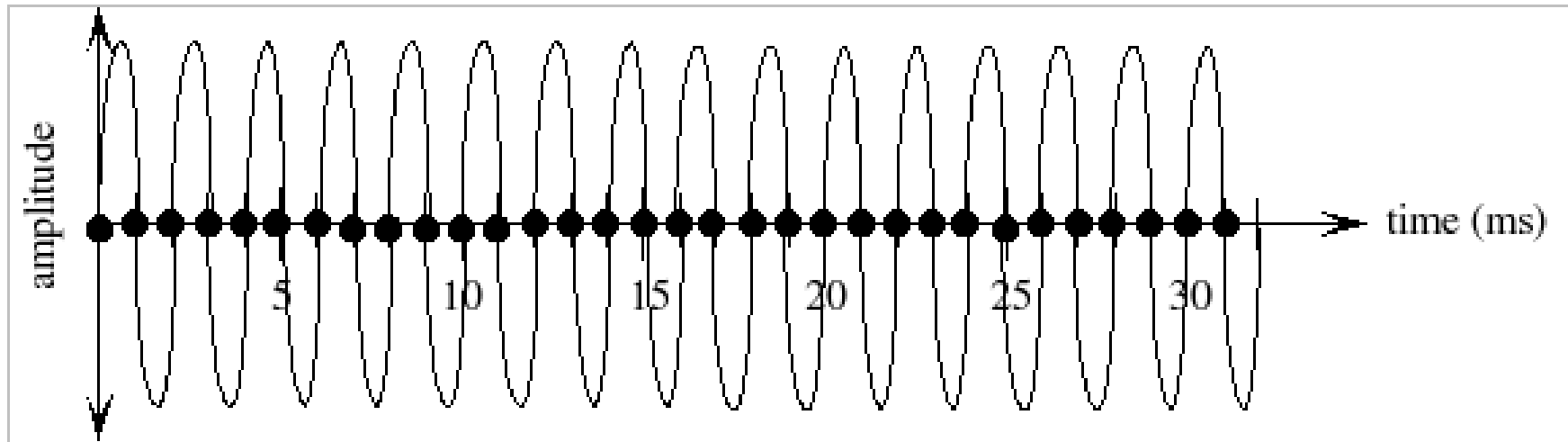


250 Hz sin wave sampled at 1000 Hz.

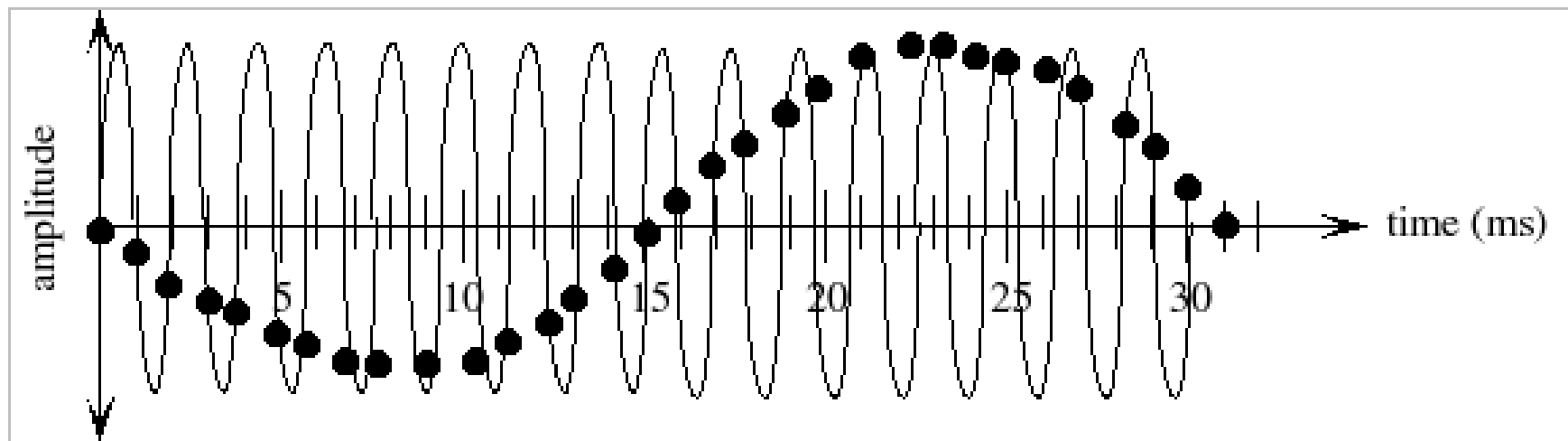
1 kHz Signal, No Aliasing



Aliasing



500 Hz sin wave sampled at 1000 Hz.



533 Hz sin wave sampled at 1000 Hz.

Avoiding Aliasing

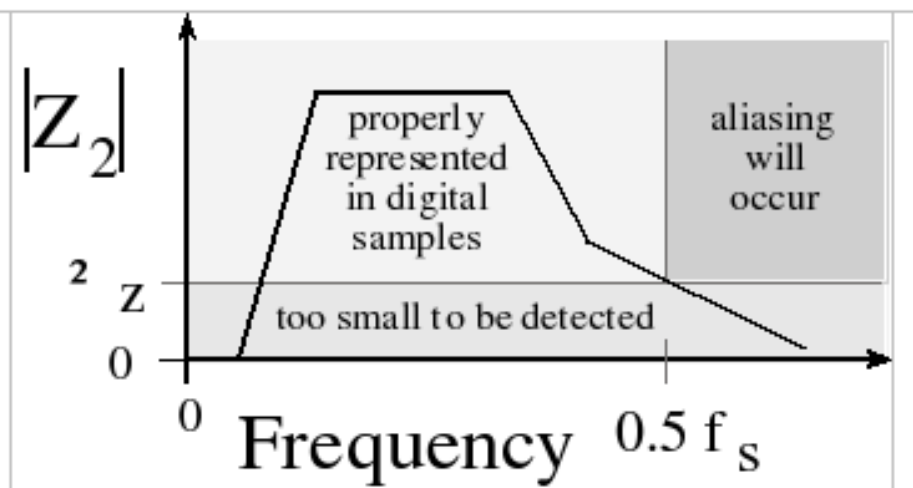
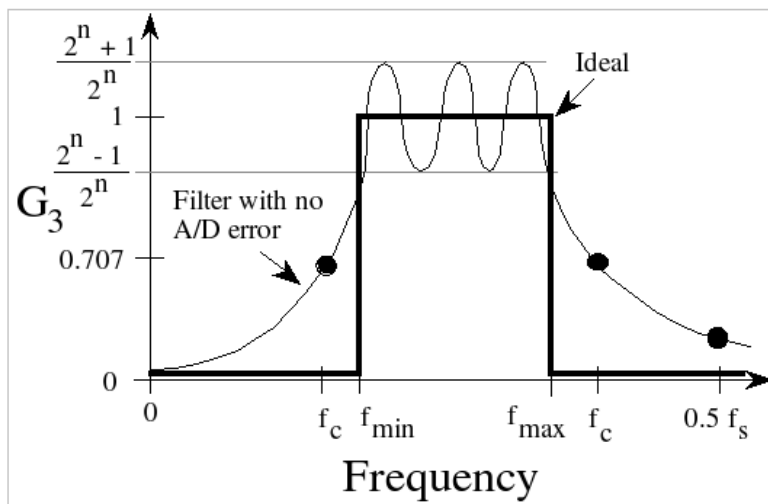
1. Increase sampling rate

- Not a general-purpose solution
 - White noise is not band-limited
 - Faster sampling requires:
 - Faster ADC
 - Faster CPU
 - More power
 - More RAM for buffering

2. Filter out undesirable frequencies before sampling using analog filter(s)

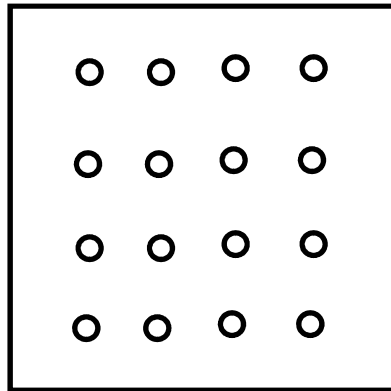
- This is what is done in practice
- Analog filters are imperfect and require tradeoffs

Signal Processing Pragmatics

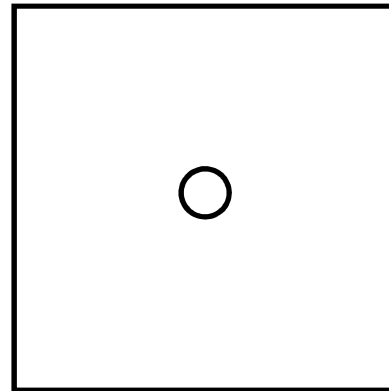


Aliasing in Space

- ◆ **Spatial sampling incurs aliasing problems also**
- ◆ **Example: CCD in digital camera samples an image in a grid pattern**
 - **Real world is not band-limited**
 - **Can mitigate aliasing by increasing sampling rate**

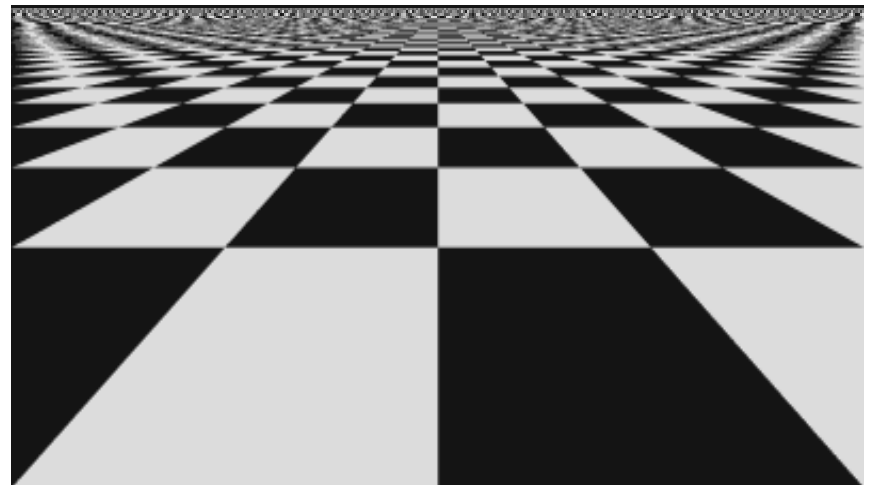
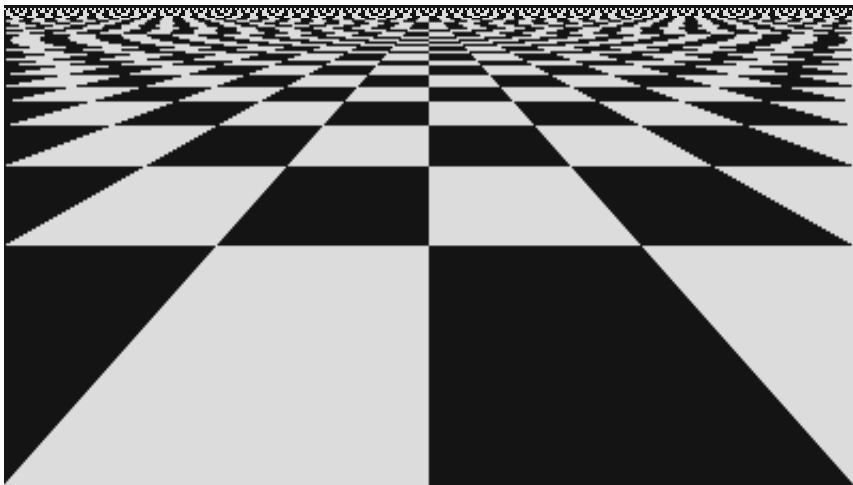
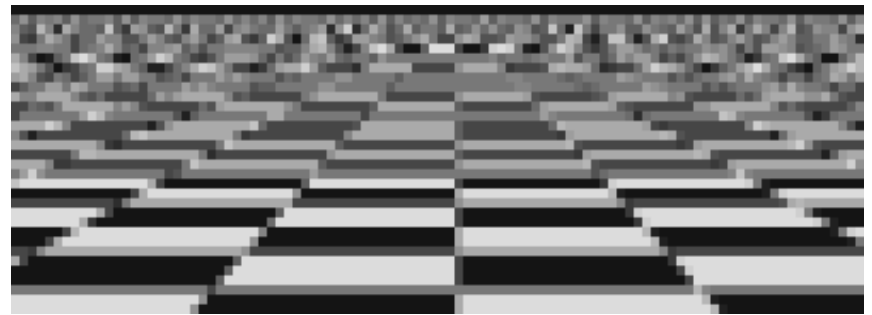
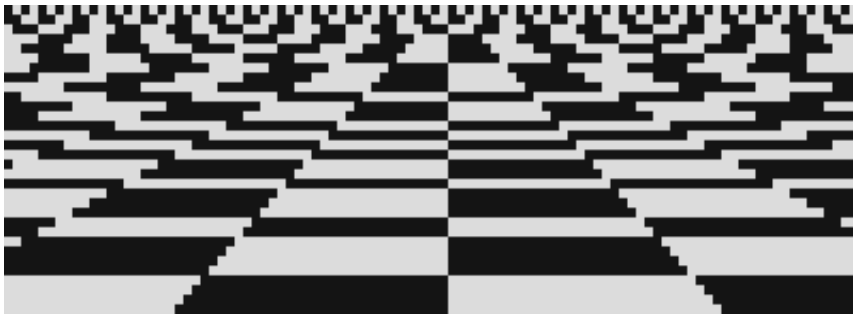


Samples



Pixel

Point vs. Supersampling



Point sampling

4x4 Supersampling

Digital Signal Processing

◆ Basic idea

- Digital signals can be manipulated losslessly
- SW control gives great flexibility

◆ DSP examples

- Amplification or attenuation
- Filtering – leaving out some unwanted part of the signal
- Rectification – making waveform purely positive
- Modulation – multiplying signal by another signal
 - E.g. a high-frequency sine wave

Assumptions

1. **Signal sampled at fixed and known rate f_s**
 - **I.e., ADC driven by timer interrupts**
2. **Aliasing has not occurred**
 - **I.e., signal has no significant frequency components greater than $0.5 \cdot f_s$**
 - **These have to be removed before ADC using an analog filter**
 - **Non-significant signals have amplitude smaller than the ADC resolution**

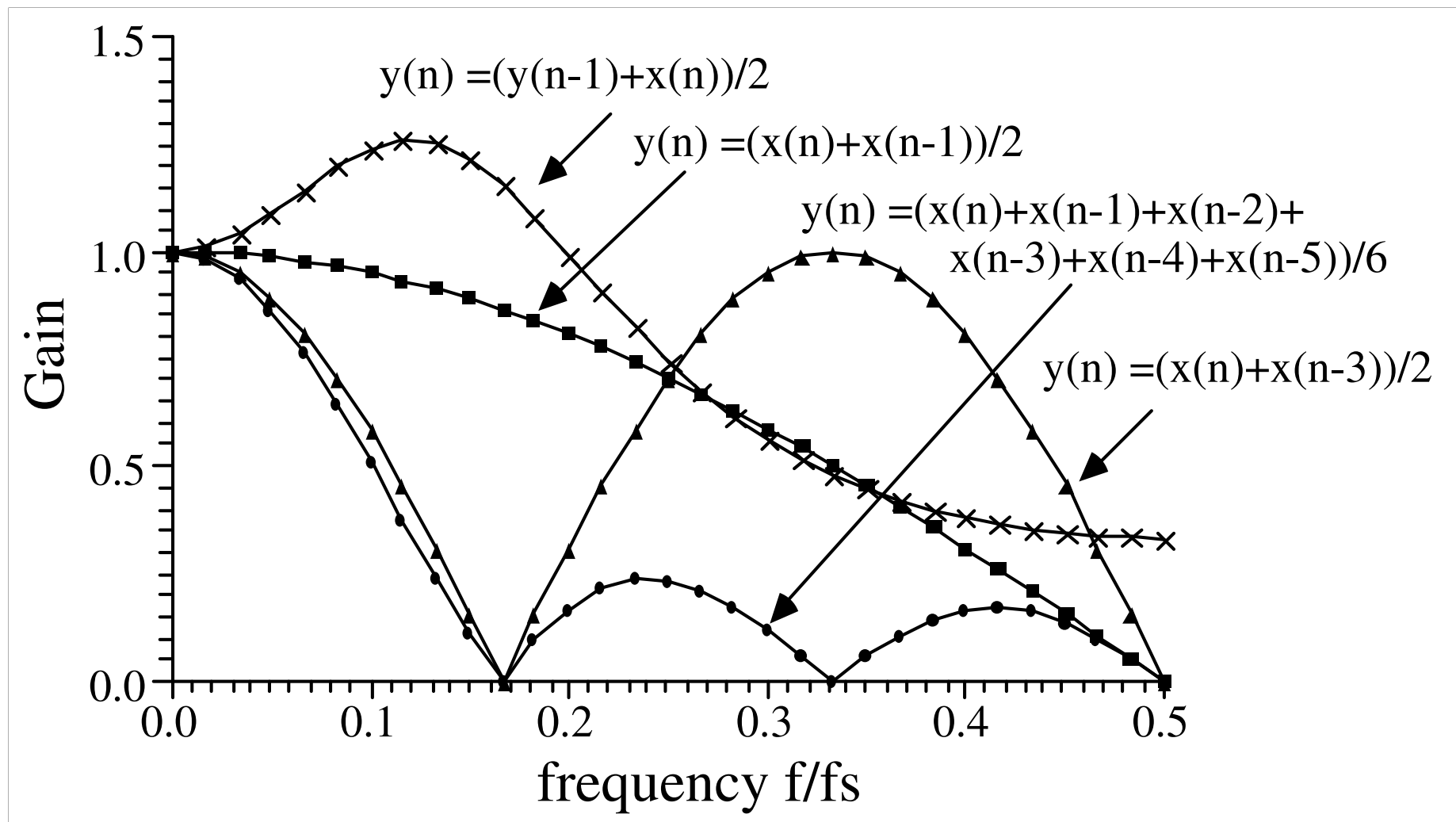
Filter Terms for CS People

- ◆ **Low pass** – lets low frequency signals through, suppresses high frequency
- ◆ **High pass** – lets high frequency signals through, suppresses low frequency
- ◆ **Passband** – range of frequencies passed by a filter
- ◆ **Stopband** – range of frequencies blocked
- ◆ **Transition band** – in between these

Simple Digital Filters

- ◆ $y(n) = 0.5 * (x(n) + x(n-1))$
 - Why not use $x(n+1)$?
- ◆ $y(n) = (1.0/6) * (x(n) + x(n-1) + x(n-2) + \dots + x(n-5))$
- ◆ $y(n) = 0.5 * (x(n) + x(n-3))$
- ◆ $y(n) = 0.5 * (y(n-1) + x(n))$
 - What makes this one different?
- ◆ $y(n) = \text{median} [x(n) + x(n-1) + x(n-2)]$

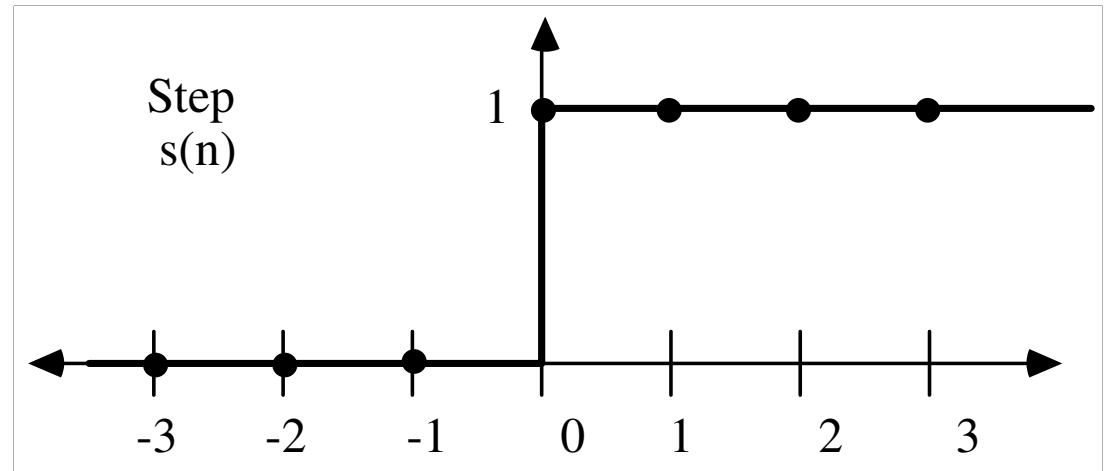
Gain vs. Frequency



Useful Signals

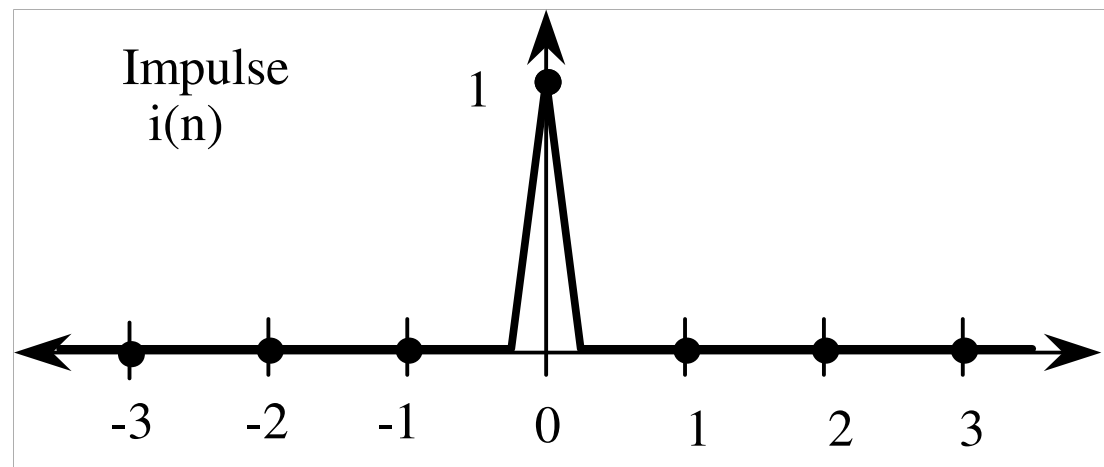
◆ Step:

➤ ..., 0, 0, 0, 1, 1, 1, ...

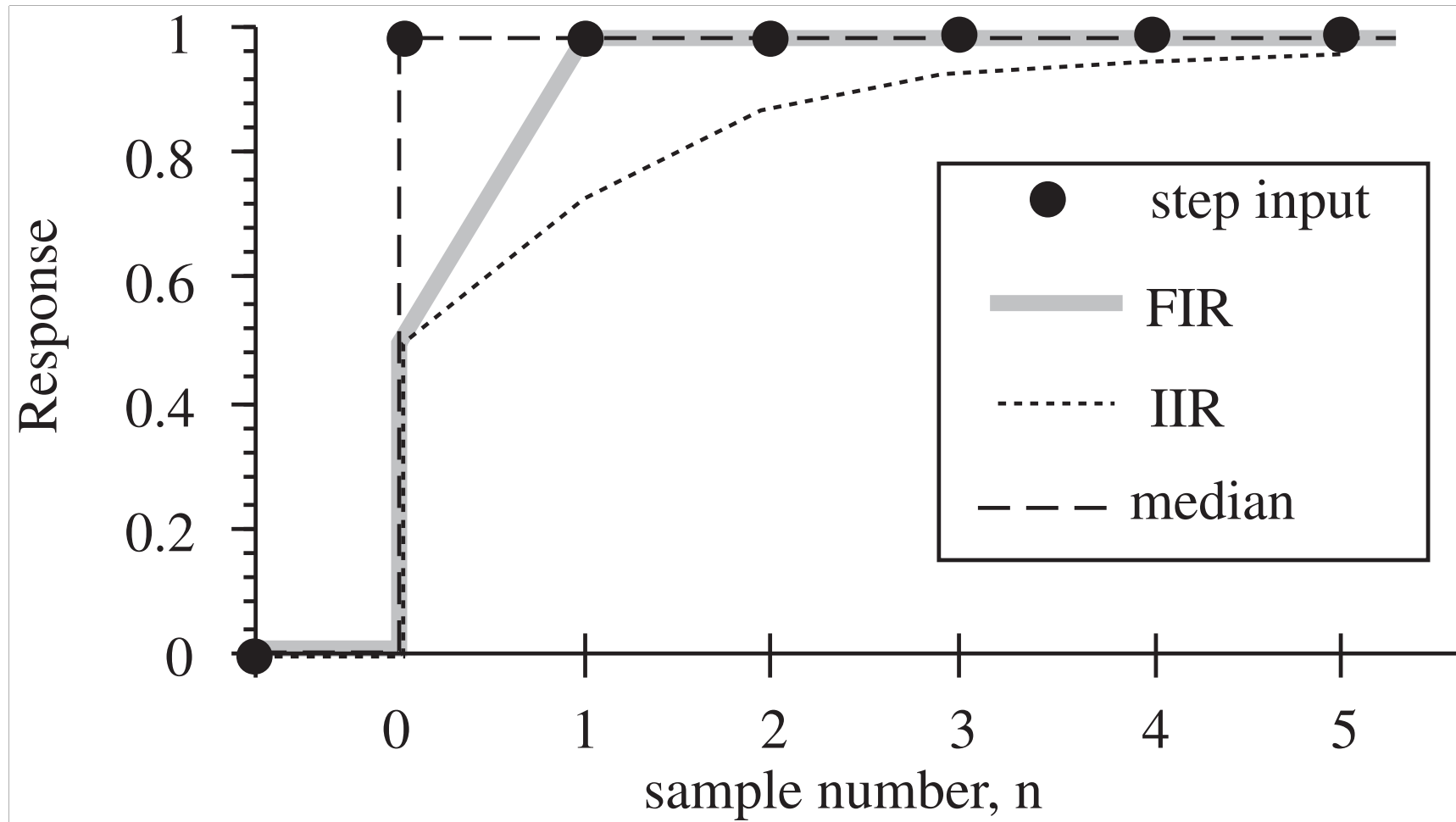


◆ Impulse:

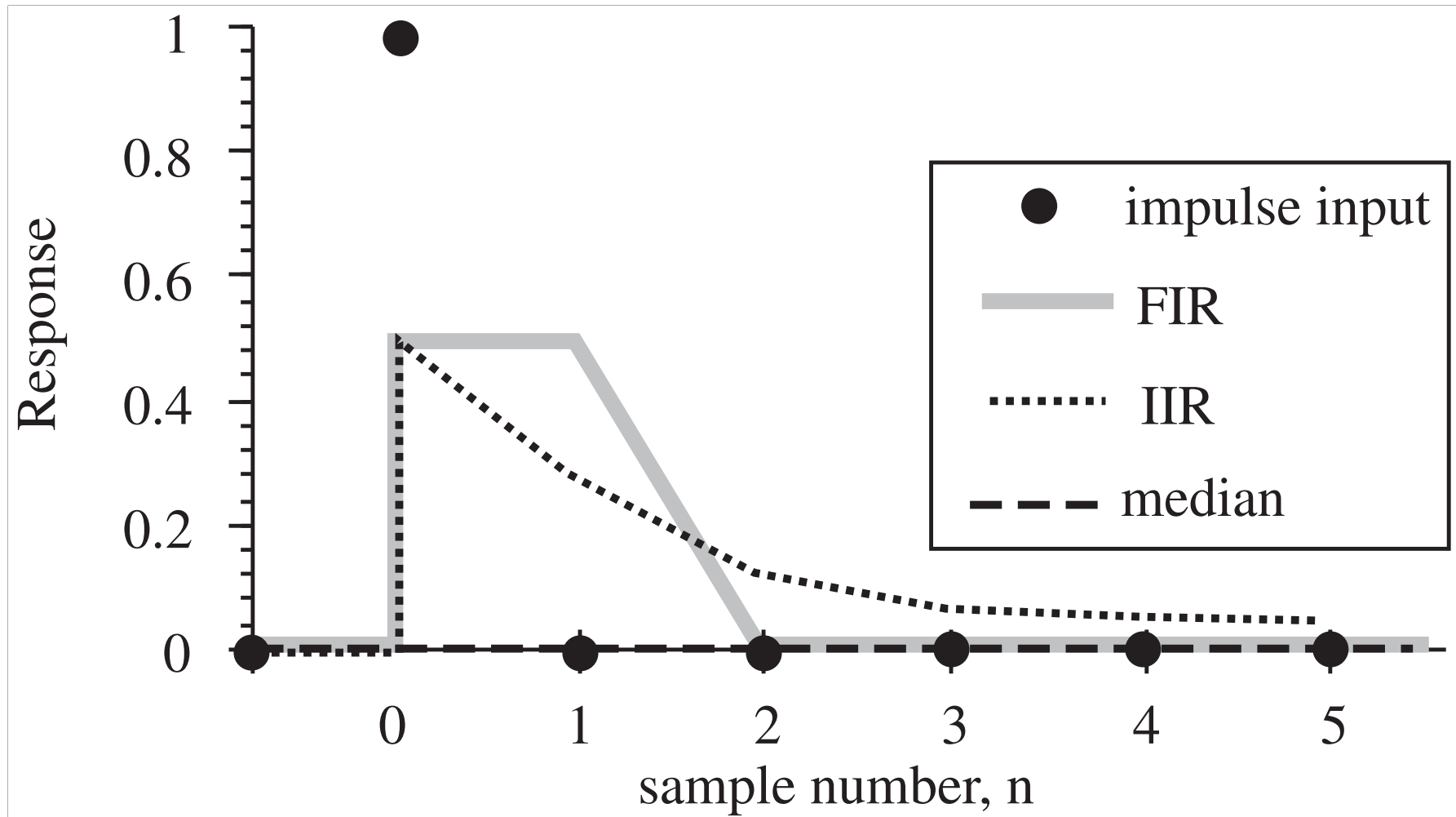
➤ ..., 0, 0, 0, 1, 0, 0, ...



Step Response



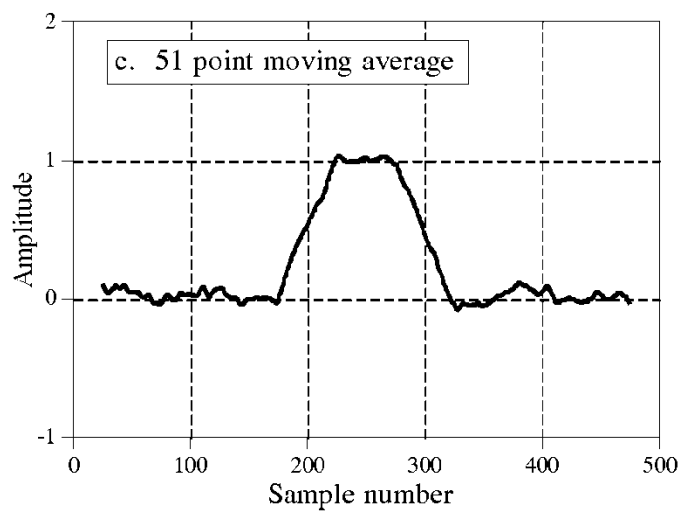
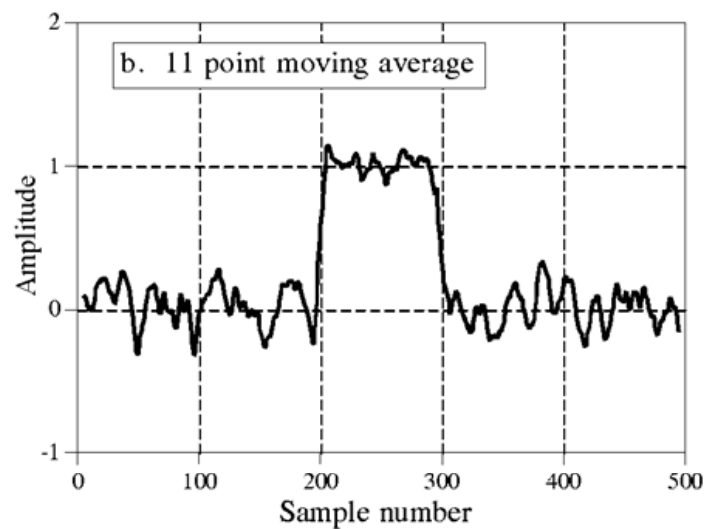
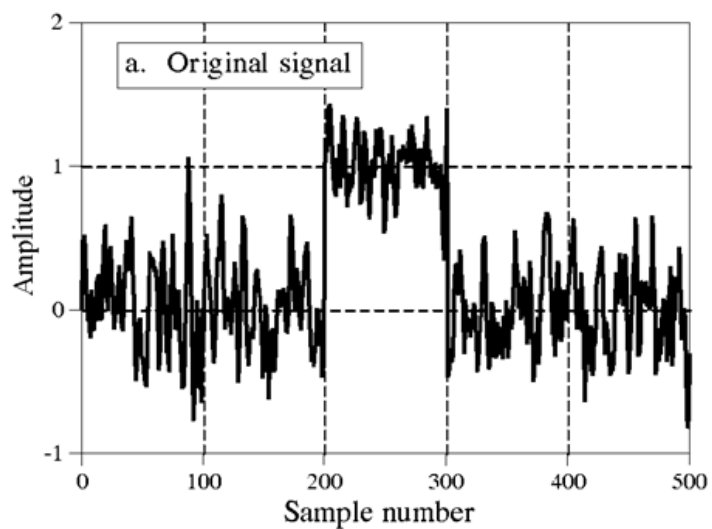
Impulse Response



FIR Filters

- ◆ **Finite impulse response**
 - Filter “remembers” the arrival of an impulse for a finite time
- ◆ **Designing the coefficients can be hard**
- ◆ **Moving average filter is a simple example of FIR**

Moving Average Example



FIR in C

```
SAMPLE fir_basic (SAMPLE input, int ntaps,
                  const SAMPLE coeff[],
                  SAMPLE z[])
{
    z[0] = input;
    SAMPLE accum = 0;
    for (int ii = 0; ii < ntaps; ii++) {
        accum += coeff[ii] * z[ii];
    }
    for (ii = ntaps - 2; ii >= 0; ii--) {
        z[ii + 1] = z[ii];
    }
    return accum;
}
```

Implementation Issues

- ◆ Usually done with fixed-point
- ◆ How to deal with overflow?
- ◆ A few optimizations
 - Put coefficients in registers
 - Put sample buffer in registers
 - Block filter
 - Put both samples and coefficients in registers
 - Unroll loops
 - Hardware-supported circular buffers
- ◆ Creating very fast FIR implementations is important

Filter Design

- ◆ **Where do coefficients come from for the moving average filter?**
- ◆ **In general:**
 1. **Design filter by hand**
 2. **Use a filter design tool**
- ◆ **Few filters designed by hand in practice**
- ◆ **Filters design requires tradeoffs between**
 1. **Filter order**
 2. **Transition width**
 3. **Peak ripple amplitude**
- ◆ **Tradeoffs are inherent**

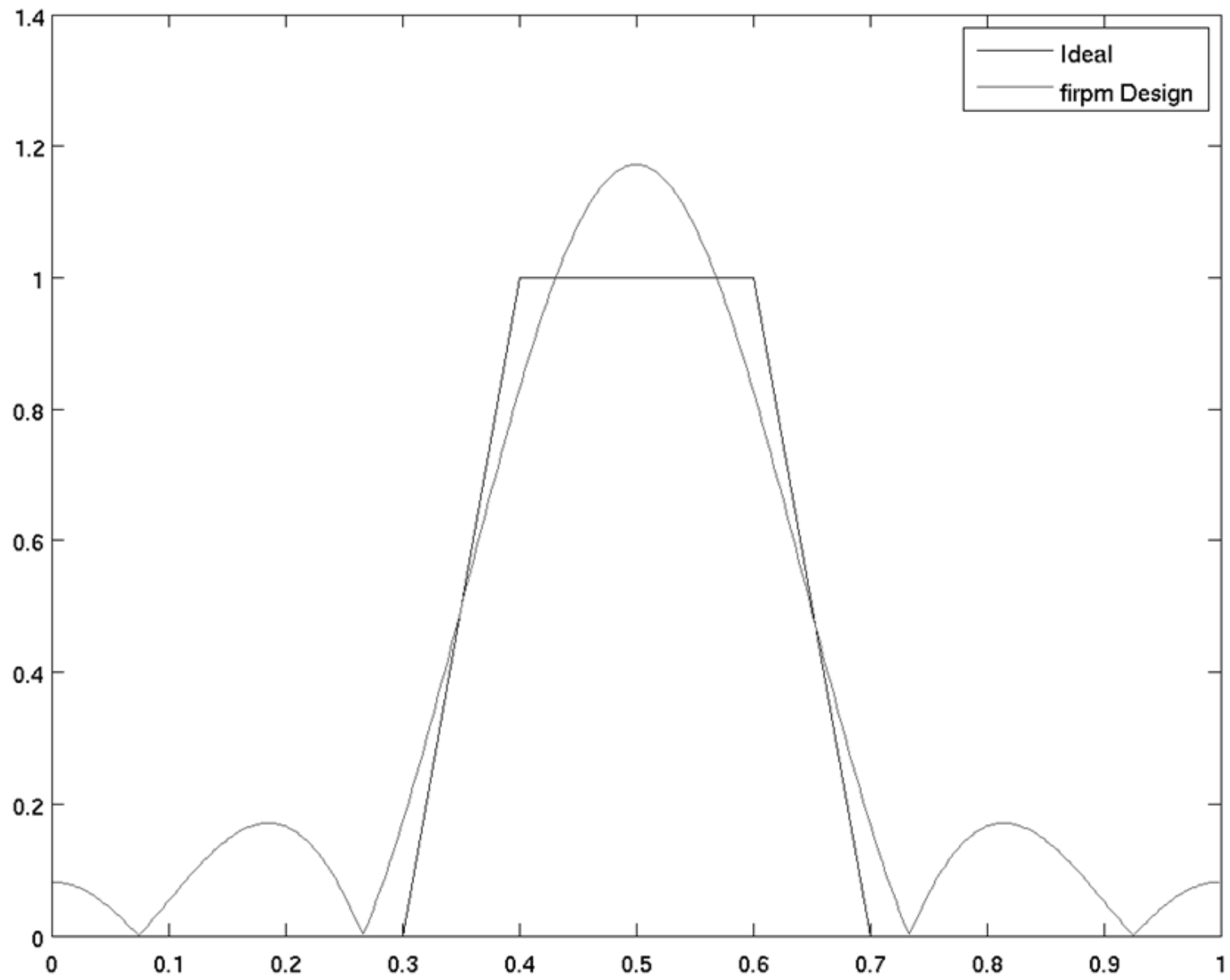
Filter Design in Matlab

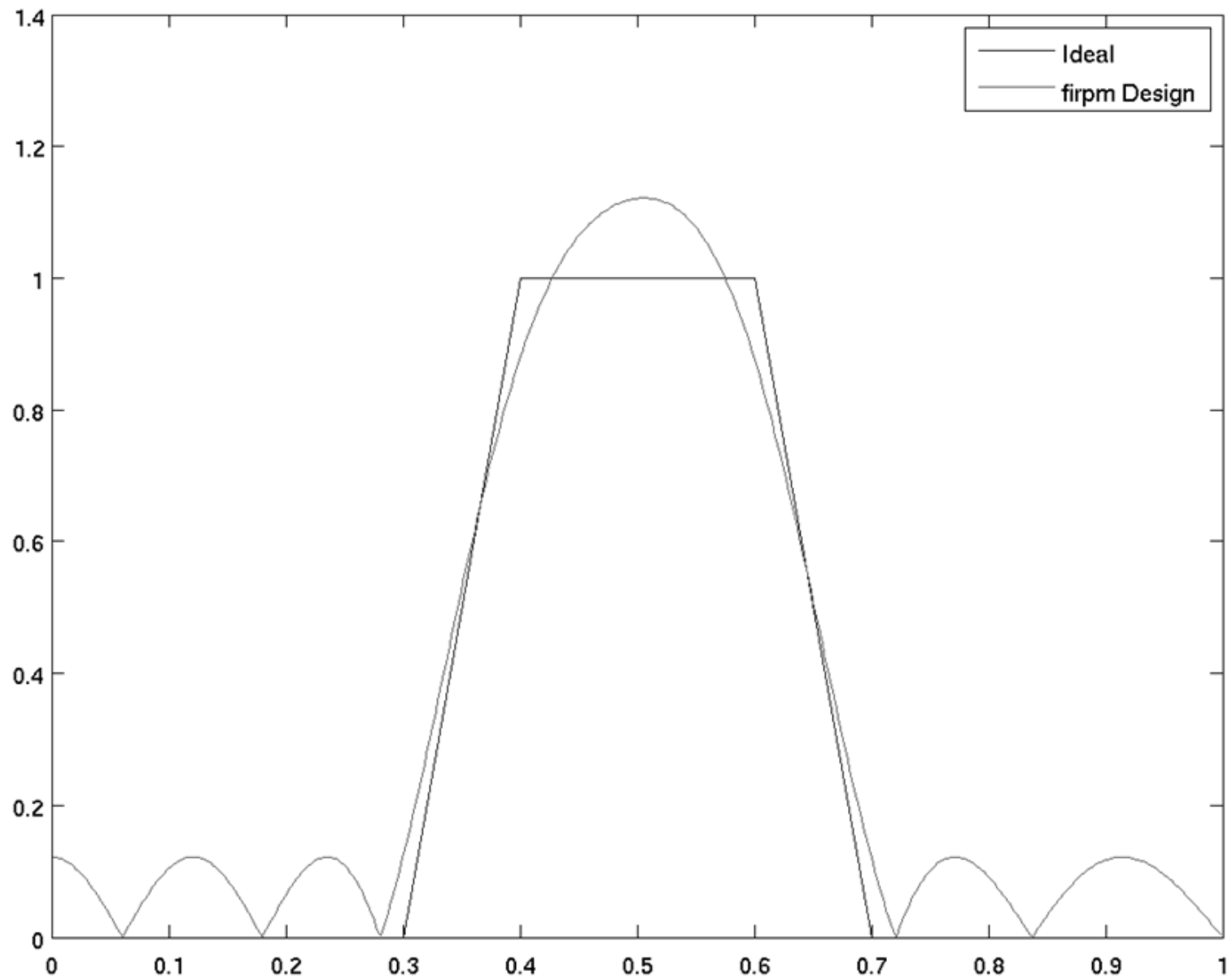
- ◆ **Matlab has excellent filter design support**
 - **`C = firpm (N, F, A)`**
 - **N = length of filter - 1**
 - **F = vector of frequency bands normalized to Nyquist**
 - **A = vector of desired amplitudes**
- ◆ **`firpm` uses minimax – it minimizes the maximum deviation from the desired amplitude**

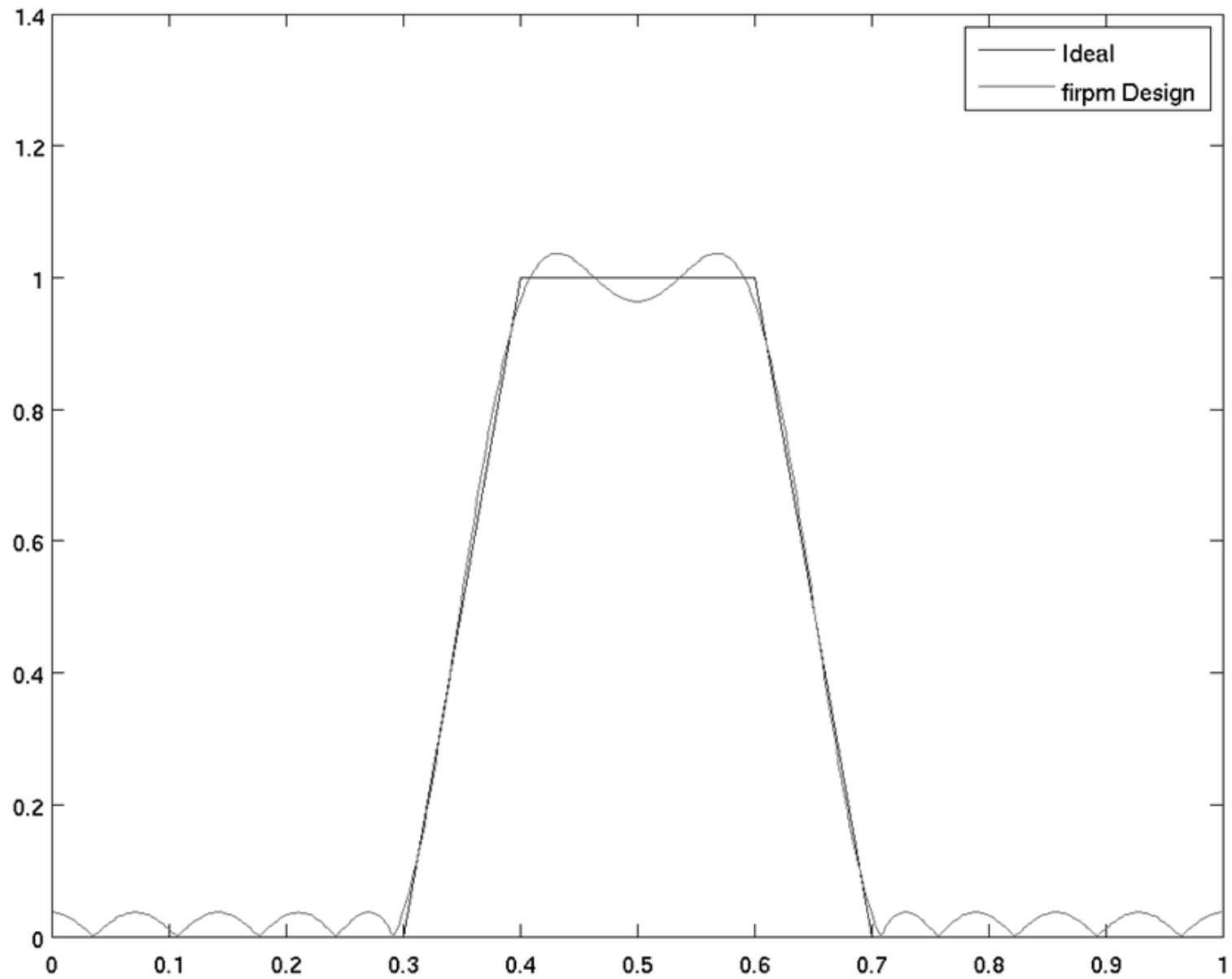
Filter Design Examples

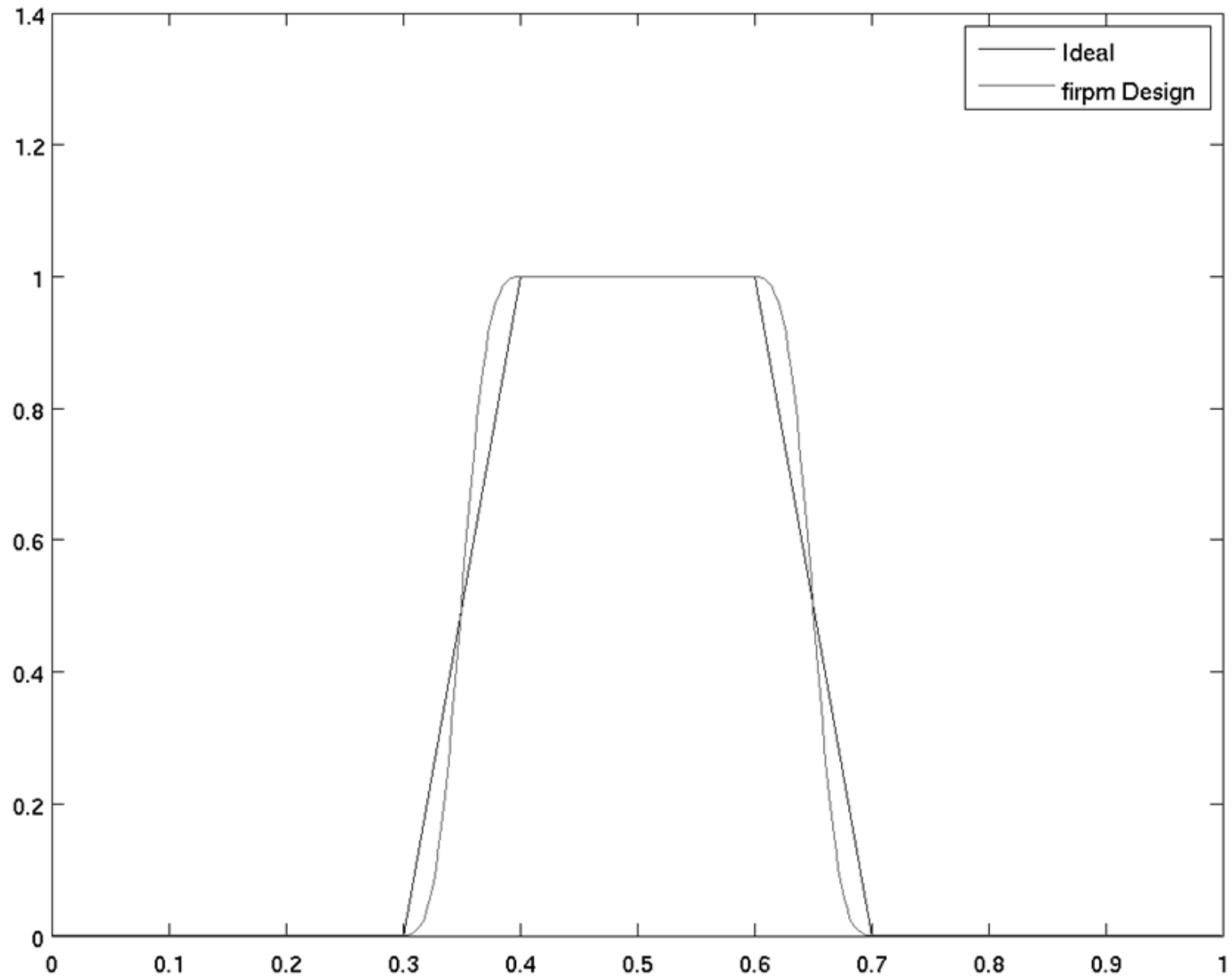
```
f = [ 0.0 0.3 0.4 0.6 0.7 1.0];  
a = [ 0 0 1 1 0 0];  
fil1 = firpm( 10, f, a);  
fil2 = firpm( 17, f, a);  
fil3 = firpm( 30, f, a);  
fil4 = firpm(100, f, a);
```

```
fil2 =  
  Columns 1 through 8  
-0.0278 -0.0395 -0.0019 -0.0595  0.0928  0.1250 -0.1667 -0.1985  
  Columns 9 through 16  
 0.2154  0.2154 -0.1985 -0.1667  0.1250  0.0928 -0.0595 -0.001  
  Columns 17 through 18  
-0.0395 -0.0278
```







Testing an FIR Filter

◆ Impulse test

- Feed the filter an impulse
- Output should be the coefficients

◆ Step test

- Feed the filter a test
- Output should stabilize to the sum of the coefficients

◆ Sine test

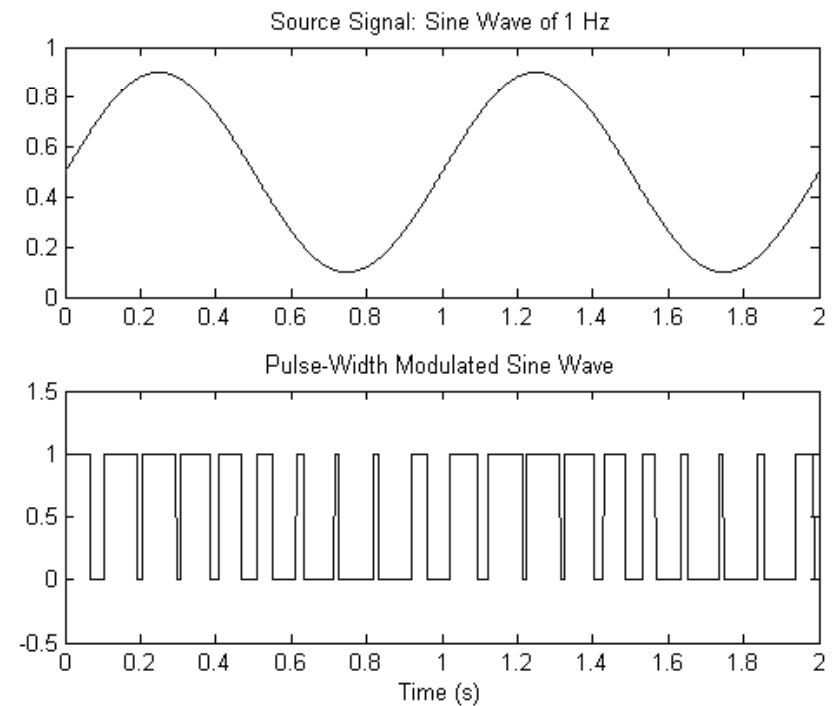
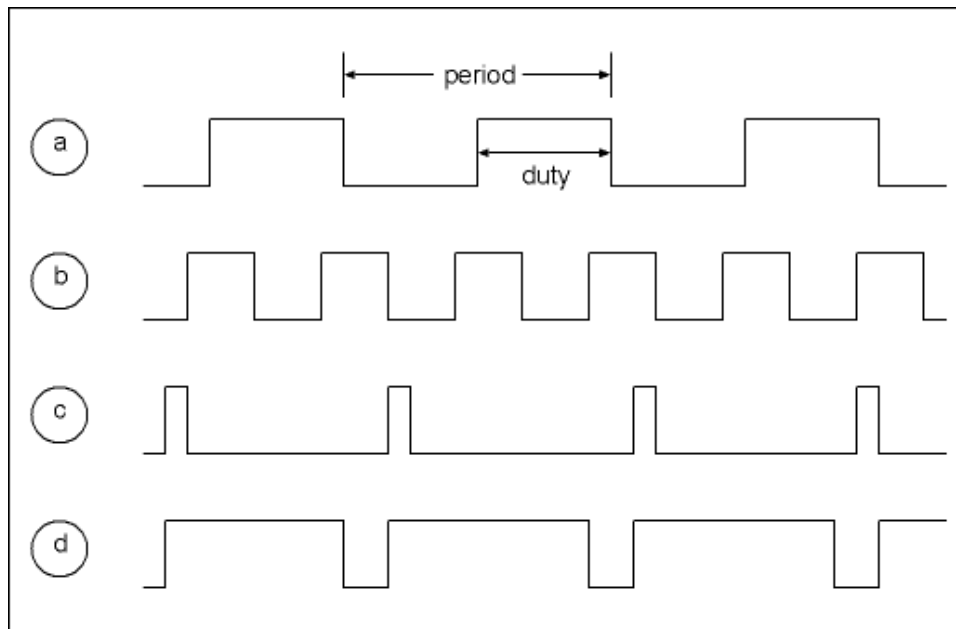
- Feed the filter a sine wave
- Output should have the expected amplitude

Digital to Analog Converters

- ◆ **Opposite of an ADC**
- ◆ **Available on-chip and as separate modules**
 - **Also not too hard to build one yourself**
- ◆ **DAC properties:**
 - **Precision: Number of distinguishable alternatives**
 - **E.g. 4092 for a 12-bit DAC**
 - **Range: Difference between minimum and maximum output (voltage or current)**
 - **Speed: Settling time, maximum output rate**
- ◆ **LPC2129 has no built-in DACs**

Pulse Width Modulation

- ◆ **PWM answers the question: How can we generate analog waveforms using a single-bit output?**
 - **Can be more efficient than DAC**



PWM

- ◆ **Approximating a DAC:**

- **Set PWM period to be much lower than DAC period**
- **Adjust duty cycle every DAC period**

- ◆ **Important application of PWM is in motor control**

- **No explicit filter necessary – inertia makes the motor its own low-pass filter**

- ◆ **PWM is used in some audio equipment**

Summary

- ◆ **Filters and other DSP account for a sizable percentage of embedded system activity**
- ◆ **Filters involve unavoidable tradeoffs between**
 - **Filter order**
 - **Transition width**
 - **Peak ripple amplitude**
- ◆ **In practice filter design tools are used**
- ◆ **We skipped all the theory!**
 - **Lots of ECE classes on this**