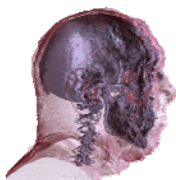
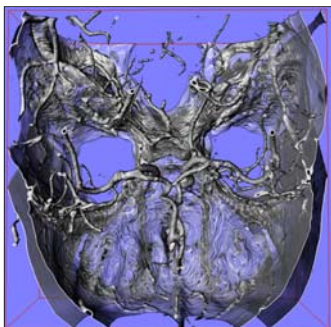


Tutorial 7
Real-Time Volume Graphics

Klaus Engel
Markus Hadwiger
Christof Rezk Salama

Real-Time Volume Graphics
[01] Introduction and Theory

Applications: Medicine

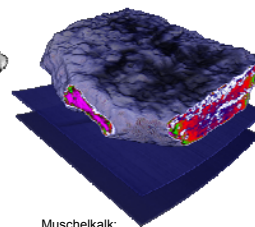
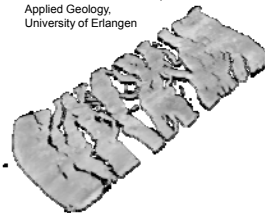


CT Human Head:
Visible Human Project,
US National Library of
Medicine, Maryland,
USA

CT Angiography:
Dept. of Neuroradiology
University of Erlangen,
Germany

Applications: Geology

Deformed Plasticine Model,
Applied Geology,
University of Erlangen



Muschelkalk:
Paläontologie,
Virtual Reality Group,
University of Erlangen

Applications: Archeology



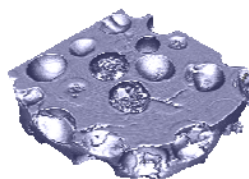
Hellenic Statue of Isis
3rd century B.C.
ARTIS, University of Erlangen-
Nuremberg, Germany



Sotades Pygmaios Statue,
5th century B.C
ARTIS, University of Erlangen-
Nuremberg, Germany

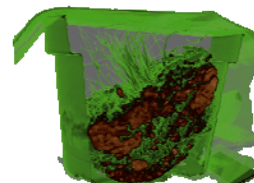
Applications:

**Material Science,
Quality Control**



Micro CT, Compound Material,
Material Science Department, University
of Erlangen

Biology



biological sample of the soil, CT,
Virtual Reality Group,
University of Erlangen

Applications

Computational Science and Engineering

Applications: Computer Science

- Visualization of Pseudo Random Numbers

Entropy of Pseudo Random Numbers
 Dan Kaminsky, Doxpara Research, USA,
 www.doxpara.com

Outline

- in real-time on commodity graphics hardware

Transfer Functions (TFs)

Map data value f to color and opacity

Shading, Compositing ...

Human Tooth CT

Physical Model of Radiative Transfer

Increase
Decrease

true emission
true absorption

in-scattering
out-scattering

Ray Integration

How do we determine the radiant energy along the ray?

Physical model: emission and absorption, no scattering

Initial intensity at s_0

Absorption along the ray segment $s_0 - s$

Extinction τ
Absorption κ
 Without absorption all the initial radiant energy would reach the point s .

$$I(s) = I(s_0) e^{-\tau(s_0-s)}$$

Ray Integration

How do we determine the radiant energy along the ray?
Physical model: emission and absorption, no scattering

One point \bar{s} along the viewing ray emits additional radiant energy.

Active emission at point \bar{s} Absorption along the distance $\bar{s} - s$

$$I(s) = I(s_0) e^{-\tau(s_0, s)} + \int_{s_0}^s q(\bar{s}) e^{-\tau(\bar{s}, s)} d\bar{s}$$

Ray Casting

- Software Solution

- Numerical Integration
- Resampling

High Computational Load

Numerical Solution

Approximate Integral by Riemann sum:

$$\tau(0, t) \approx \sum_{i=0}^{\lfloor t/\Delta t \rfloor} \kappa(i \cdot \Delta t) \Delta t$$

$$e^{-\tau(0, t)} \approx \prod_{i=0}^{\lfloor t/\Delta t \rfloor} e^{-\kappa(i \cdot \Delta t) \Delta t}$$

Numerical Solution

$$\tau(0, t) \approx \bar{\tau}(0, t) = \sum_{i=0}^{\lfloor t/\Delta t \rfloor} \kappa(i \cdot \Delta t) \Delta t$$

$$e^{-\tau(0, t)} \approx \prod_{i=0}^{\lfloor t/\Delta t \rfloor} e^{-\kappa(i \cdot \Delta t) \Delta t}$$

Now we introduce opacity:

$$(1 - A_i) = e^{-\kappa(i \cdot \Delta t) \Delta t}$$

Numerical Solution

$$\tau(0, t) \approx \bar{\tau}(0, t) = \sum_{i=0}^{\lfloor t/\Delta t \rfloor} \kappa(i \cdot \Delta t) \Delta t$$

$$q(t) \approx e^{-\tau(0, t)} \sum_{i=0}^{\lfloor t/\Delta t \rfloor} q(i \cdot \Delta t) \Delta t$$

Now we introduce opacity:

$$1 - A_i = e^{-\kappa(i \cdot \Delta t) \Delta t}$$

Numerical Solution

$$e^{-\tau(0, t)} = \prod_{i=0}^{\lfloor t/\Delta t \rfloor} (1 - A_i)$$

$$q(t) \approx \sum_{i=0}^{\lfloor t/\Delta t \rfloor} C_i e^{-\tau(0, t)}$$

where C_i is computed recursively:

$$C_i = (1 - A_i) C_{i-1} + q(i \cdot \Delta t) \Delta t$$

- Radiant energy observed at position i
- Radiant energy emitted at position i
- Absorption at position i
- Radiant energy observed at position $i-1$

Numerical Solution

Back-to-front compositing

$$\bar{C} = \sum_{i=0}^{[T/\Delta t]} C_i$$

Front-to-back compositing

Front-to-back computed recursively

$$C_i = C_{i+1} + (1 - A_{i+1})C_i$$

$$A_i = A_{i+1} + (1 - A_{i+1})A_i$$

Early Ray Termination:
Stop the calculation when $A_i \approx 1$

Summary

- Emission Absorption Model

$$I(s) = I(s_0) e^{-\tau(s_0, s)} + \int_{s_0}^s q(\bar{s}) e^{-\tau(\bar{s}, s)} d\bar{s}$$
- Numerical Solutions

<i>Back-to-front iteration</i>	<i>Front-to-back iteration</i>
$C_i = C_{i+1} + (1 - A_i)C_{i-1}$	$C_i = C_{i+1} + (1 - A_{i+1})C_i$
$A_i = A_{i+1} + (1 - A_{i+1})A_i$	$A_i = A_{i+1} + (1 - A_{i+1})A_i$

Real-Time Volume Graphics
[03] GPU-Based
Volume Rendering

Volume Rendering

Image order approach:

For each pixel {
calculate color of the pixel
}

Volume Rendering

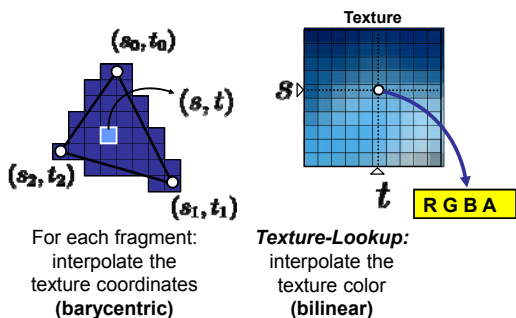
Object order approach:

For each pixel {
calculate color of the pixel
}

Texture-based Approaches

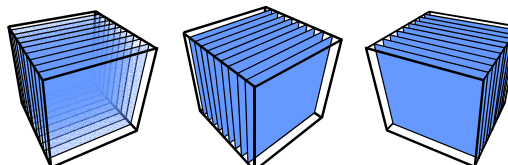
- No volumetric hardware-primitives!
- Proxy geometry (Polygonal Slices)

How does a texture work?



2D Textures

- Draw the volume as a stack of 2D textures
- Bilinear Interpolation in Hardware**
- Decomposition into axis-aligned slices



- 3 copies of the data set in memory

Implementation

```

GLfloat pModelViewMatrix[16];

//get the current modelview matrix
GLfloat *pModelViewMatrix = glGetFloatv(GL_MODELVIEW_MATRIX, pModelViewMatrix);

//rotate the initial viewing direction
GLfloat pViewVector[4] = {0.0f, 0.0f, -1.0f, 0.0f};
MatVecMultiply(pModelViewMatrix, pViewVector);

//find the maximal vector component
int nMax = FindAbsMaximum(pViewVector);

switch (nMax) {
case X:
    if (pViewVector[X] > 0.0f) {
        DrawSliceStack.PositiveX();
    } else {
        DrawSliceStack.NegativeX();
    }
    break;
case Y:
    if (pViewVector[Y] > 0.0f) {
        DrawSliceStack.PositiveY();
    } else {
        DrawSliceStack.NegativeY();
    }
    break;
}
    
```



Implementation

```

//draw slices perpendicular to x-axis
//in back-to-front order
void DrawSliceStack.NegativeX() {

    double dxPos = -1.0;
    double dxStep = 2.0/double(XDIM);

    for(int slice = 0; slice < XDIM; ++slice) {
        //select the texture image corresponding to the slice
        glBindTexture(GL_TEXTURE_2D, textureNameStackX[slice]);

        //draw the slice polygon
        glBegin(GL_QUADS);
        glTexCoord2d(0.0, 0.0); glVertex3d(dxPos, -1.0, -1.0);
        glTexCoord2d(0.0, 1.0); glVertex3d(dxPos, -1.0, 1.0);
        glTexCoord2d(1.0, 1.0); glVertex3d(dxPos, 1.0, 1.0);
        glTexCoord2d(1.0, 0.0); glVertex3d(dxPos, 1.0, -1.0);
        glEnd();

        dxPos += dxStep;
    }
}
    
```

Fragment Program

```

// simple 2D texture sampling
float4 main (half2 texUV : TEXCOORD0,
             uniform sampler2D slice) : COLOR
{
    float4 result = tex2D(slice, texUV);
    return result;
}
    
```

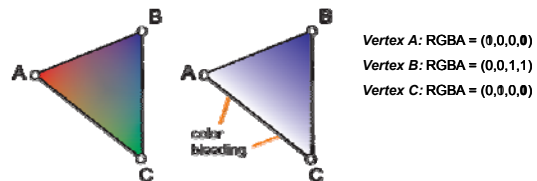
We assume here that the RGBA texture already contains emission/absorption coefficients.
Transfer functions are discussed later

Compositing

```

//alpha blending for colour pre-multiplied with opacity
glBlendFunc(GL_BLEND);
glAlphaFunc(GL_LESS, GL_FUNC_SRC_ALPHA);
    
```

The standard alpha blending causes color bleeding!



Solution: Associated Colors:
RGB values must be pre-multiplied by opacity A!

Compositing

- **Maximum Intensity Projection**
No emission/absorption
Simply compute maximum value along a ray

```

#ifdef GL_EXT_blend_minmax
//enable alpha blending
glEnable(GL_BLEND);

//enable maximum selection
glBlendEquationEXT(GL_MAX_EXT);

//setup arguments for the blending equation
glBlendFunc(GL_SRC_COLOR, GL_DST_COLOR);
#endif
    
```

Compositing

A Emission/Absorption **B** Maximum Intensity Projection

2D Textures: Drawbacks

- Sampling rate is inconsistent

- Emission/absorption slightly incorrect
- **Super-sampling on-the-fly impossible**

3D Textures

Don't be confused: 3D textures are not volumetric rendering primitives! Only planar polygons are supported as rendering primitives.

RGBA

3D Textures

3D Texture: Volumetric Texture Object

- Trilinear Interpolation in Hardware
- ➡ Slices parallel to the image plane

- One large texture block in memory

Resampling via 3D Textures

- **Sampling rate is constant**

- Supersampling by increasing the number of slices

Bricking

- What happens if data set is too large to fit into local video memory?
- ➔ Divide the data set into smaller chunks (bricks)

One plane of voxels must be duplicated to enable correct interpolation across brick boundaries

incorrect interpolation!

Bricking

- What happens if data set is too large to fit into local video memory?
- ➔ Divide the data set into smaller chunks (bricks)

Problem: Bus-Bandwidth

- Unbalanced Load for GPU und Memory Bus

GPU: draw, draw
Bus: transfer brick, transfer brick

Inefficient!

Bricking

- What happens if data set is too large to fit into local video memory?
- ➔ Divide the data set into smaller chunks (bricks)

Problem: Bus-Bandwidth

- Keep the bricks small enough!
More than one brick must fit into video memory !
 - Transfer and Rendering can be performed in parallel
 - Increased CPU load for intersection calculation!
 - Effective load balancing still very difficult!**

Cube-Slice Intersection

Question: Can we compute this in a vertex program?

Vertex program:
Input: 6 Vertices
Output: 6 Vertices

- P0: Intersection with red path
- P1: Intersection with dotted red edge or P0
- P2: Intersection with green path
- P3: Intersection with dotted green edge or P1
- P4: Intersection with blue path
- P5: Intersection with dotted blue edge or P2

Back to 2D Textures

- ~~fixed~~ number of object aligned slices
- visual artifacts due to bilinear interpolation

- Utilize Multi-Textures (2 textures per polygon) to implement trilinear interpolation!

2D Multi-Textures

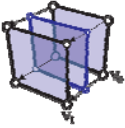
Axis-Aligned Slices

- Bilinear Interpolation by 2D Texture Unit
- Blending of two adjacent slice images

$$S_{i+\alpha} = (1 - \alpha)S_i + \alpha \cdot S_{i+1}$$

- Trilinear Interpolation

Implementation



```

//vertex program for computing object aligned slices
void main() float4 Vertex0 : POSITION,
float4 Vertex1 : TEXCOORD0,
half3 TexCoord0 : TEXCOORD1,

uniform float slicePos,
uniform float4x4 matModelViewProj,

out float4 VertxDut : POSITION,
out half3 TexCoordOut : TEXCOORD0

{
//interpolate between the two positions
float4 Vertex = lerp(Vertex0, Vertex1, slicePos);

//transform vertex into screen space
VertxDut = mul(matModelViewProj, Vertex);

//compute the correct 3D texture coordinate
TexCoordOut = half3(TexCoord.xy, slicePos);

return;
}
    
```

Implementation

```

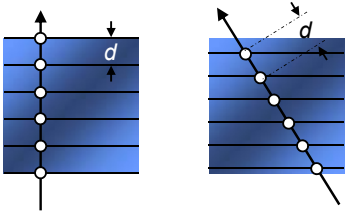
//fragment program for trilinear interpolation
//using 2D multi-textures
float4 main (half3 texUV : TEXCOORD0,
uniform sampler2D texture0,
uniform sampler2D texture1 ) : COLOR
{
//two bilinear texture fetches
float4 tex0 = tex2D(texture0, texUV.xy);
float4 tex1 = tex2D(texture1, texUV.xy);

//additional linear interpolation
float4 result = lerp(tex0,tex1,texUV.z);

return result;
}
    
```

2D Multi-Textures

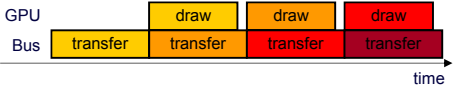
- Sampling rate is constant



- Supersampling by increasing the number of slices

Advantages

- More efficient load balancing



- Exploit the GPU and the available memory bandwidth in parallel
- Transfer the smallest amount of information required to draw the slice image!
- **Significantly higher performance**, although 3 copies of the data set in main memory


Summary

Rasterization Approaches for Direct Volume Rendering

- **2D Texture Based Approaches**
 - 3 fixed stacks of object aligned slices
 - Visual artifacts due to bilinear interpolation only
 - No supersampling
- **3D Texture Based Approaches**
 - Viewport aligned slices
 - Supersampling with trilinear interpolation
 - Bricking: Bus transfer inefficient for large volumes
- **2D Texture Based Approaches**
 - 3 variable stacks of object aligned slices
 - Supersampling with Trilinear interpolation
 - Higher performance for larger volumes

Real-Time Volume Graphics

[04] GPU-Based Ray-Casting



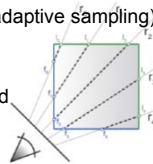
Talk Outline

- Why use ray-casting instead of slicing?
- Ray-casting of rectilinear (structured) grids
 - Basic approaches on GPUs
 - Basic acceleration methods
 - Object-order empty space skipping
 - Isosurface ray-casting
 - Endoscopic ray-casting



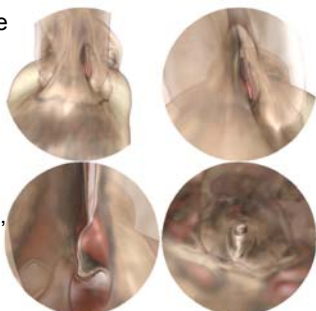
Why Ray-Casting on GPUs?

- Most GPU rendering is object-order (rasterization)
- Image-order is more “CPU-like”
 - Recent fragment shader advances
 - Simpler to implement
 - Very flexible (e.g., adaptive sampling)
 - Correct perspective projection
 - Can be implemented in single pass!
 - Native 32-bit compositing



Where Is Correct Perspective Needed?

- Entering the volume
- Wide field of view
- Fly-throughs
- Virtual endoscopy
- Integration into perspective scenes, e.g., games



Recent GPU Ray-Casting Approaches

- Rectilinear grids
 - [Krüger and Westermann, 2003]
 - [Röttger et al., 2003]
 - [Green, 2004] (NVIDIA SDK Example)
 - [Stegmaier et al., 2005]
 - [Scharsach et al., 2006]
- Unstructured (tetrahedral) grids
 - [Weiler et al., 2002, 2003, 2004]
 - [Bernardon, 2004]



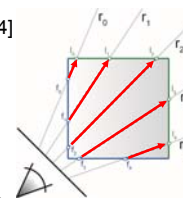
Single-Pass Ray-Casting

- Enabled by conditional loops in fragment shaders (Shader Model 3; e.g., Geforce 6800, ATI X1800)
- Substitute multiple passes and early-z testing by single loop and early loop exit
- No compositing buffer: full 32-bit precision!
- NVIDIA example: compute ray intersections with bounding box, march along rays and composite



Basic Ray Setup / Termination

- Two main approaches:
 - Procedural ray/box intersection [Röttger et al., 2003], [Green, 2004]
 - Rasterize bounding box [Krüger and Westermann, 2003]
- Some possibilities
 - Ray start position and exit check
 - Ray start position and exit position
 - Ray start position and direction vector



Procedural Ray Setup/Termination

- Everything handled in the fragment shader
- Procedural ray / bounding box intersection
- Ray is given by camera position and volume entry position
- Exit criterion needed
- Pro: simple and self-contained
- Con: full load on the fragment shader

Fragment Shader

- Rasterize front faces of volume bounding box
- Texcoords are volume position in [0,1]
- Subtract camera position
- Repeatedly check for exit of bounding box

```

// Cg fragment shader code for single-pass ray casting
float4 main(VOLCOORD IN, float4 TexCoord0 : TEXCOORD0,
            uniform sampler3D SamplerDataVolume,
            uniform samplerID SamplerTransferFunction,
            uniform float4 camera,
            uniform float stepsize,
            uniform float3 volExtentMin,
            uniform float3 volExtentMax
            ) : COLOR
{
    float4 value;
    float scalar;
    // Initialize accumulated color and opacity
    float4 det = float4(0.0,0.0);
    // Determine volume entry position
    float3 position = TexCoord0.xyz;
    // Compute ray direction
    float3 direction = TexCoord0.xyz - camera;
    direction = normalize(direction);
    // Loop for ray traversal
    for (int i = 0; i < 200; i++) // Some large number
    {
        // Data access to scalar value in 3D volume texture
        value = tex3D(SamplerDataVolume, position);
        scalar = value.a;
        // Apply transfer function
        float4 src = texID(SamplerTransferFunction, scalar);
        // Front-to-back compositing
        det = (1.0-det.a) * src + det;
        // Advance ray position along ray direction
        position = position + direction * stepsize;
        // Ray termination: Test if outside volume ...
        float3 temp1 = sign(position - volExtentMin);
        float3 temp2 = sign(volExtentMax - position);
        float inside = det(temp1, temp2);
        // ... and exit loop
        if (inside < 3.0)
            break;
    }
    return det;
}
    
```

"Image-Based" Ray Setup/Termination

- Rasterize bounding box front faces and back faces [Krüger and Westermann, 2003]
- Ray start position: front faces
- Direction vector: back-front faces
- Independent of projection (orthogonal/perspective)

Standard Ray-Casting Optimizations (1)

Early ray termination

- Isosurfaces: stop when surface hit
- Direct volume rendering: stop when opacity >= threshold
- Several possibilities
 - Older GPUs: multi-pass rendering with early-z test
 - Shader model 3: break out of ray-casting loop
 - Current GPUs: early loop exit not optimal but good

Standard Ray-Casting Optimizations (2)

Empty space skipping

- Skip transparent samples
- Depends on transfer function
- Start casting close to first hit
- Several possibilities
 - Per-sample check of opacity (expensive)
 - Traverse hierarchy (e.g., octree) or regular grid
 - These are image-order: what about object-order?

Object-Order Empty Space Skipping (1)

- Modify initial rasterization step

rasterize bounding box rasterize "tight" bounding geometry

Object-Order Empty Space Skipping (2)

- Store min-max values of volume bricks
- Cull bricks against isovalue or transfer function
- Rasterize front and back faces of active bricks

Object-Order Empty Space Skipping (3)

- Rasterize front and back faces of active min-max bricks
- Start rays on brick front faces
- Terminate when
 - Full opacity reached, or
 - Back face reached

Object-Order Empty Space Skipping (3)

- Rasterize front and back faces of active min-max bricks
- Start rays on brick front faces
- Terminate when
 - Full opacity reached, or
 - Back face reached
- Not all empty space is skipped

Isosurface Ray-Casting

- Isosurfaces/Level Sets
 - scanned data
 - distance fields
 - CSG operations
 - level sets: surface editing, simulation, segmentation, ...

Intersection Refinement (1)

- Fixed number of bisection or binary search steps
- Virtually no impact on performance
- Refine already detected intersection
- Handle problems with small features / at silhouettes with adaptive sampling

Intersection Refinement (2)

without refinement

with refinement

sampling rate 1/5 voxel (no adaptive sampling)

Intersection Refinement (3)

Sampling distance 1.0, 24 fps Sampling distance 5.0, 66 fps

Deferred Isosurface Shading

- Shading is expensive
 - Gradient computation; conditional execution not free
- Ray-casting step computes only intersection image

Enhancements (1)

- Build on image-based ray setup
- Allow viewpoint inside the volume

- Intersect polygonal geometry

Enhancements (2)

1. Starting position computation
⇒ Ray start position image
2. Ray length computation
⇒ Ray length image
3. Render polygonal geometry
⇒ Modified ray length image
4. Raycasting
⇒ Compositing buffer
5. Blending
⇒ Final image

Moving Into The Volume (1)

- Near clipping plane clips into front faces

- Fill in holes with near clipping plane
- Can use depth buffer [Scharsach et al., 2006]

Moving Into The Volume (2)

1. Rasterize near clipping plane
 - Disable depth buffer, enable color buffer
 - Rasterize entire near clipping plane
2. Rasterize nearest back faces
 - Enable depth buffer, disable color buffer
 - Rasterize *nearest back faces* of active bricks
3. Rasterize nearest front faces
 - Enable depth buffer, enable color buffer
 - Rasterize *nearest front faces* of active bricks

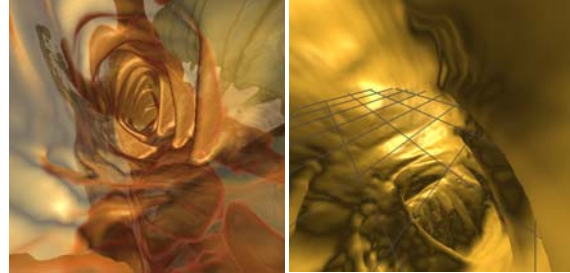
Virtual Endoscopy

- Viewpoint inside the volume with wide field of view
- E.g.: virtual colonoscopy
- Hybrid isosurface rendering / direct volume rendering
- E.g.: colon wall and structures behind



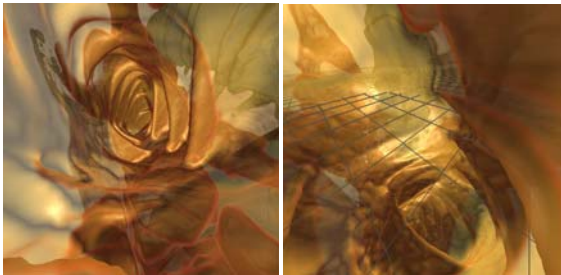
Virtual Colonoscopy

- First find isosurface; then continue with DVR



Virtual Colonoscopy

- First find isosurface; then continue with DVR



Hybrid Ray-Casting (1)

- Isosurface rendering
 - Find isosurface first
 - Semi-transparent shading provides surface information
- Additional unshaded DVR
 - Render volume behind the surface with unshaded DVR
 - Isosurface is starting position
 - Start with (1.0-iso_opacity)



Hybrid Ray-Casting (2)

- Hiding sampling artifacts (similar to interleaved sampling, [Heidrich and Keller, 2001])



Conclusions

- GPU ray-casting is an attractive alternative
- Very flexible and easy to implement
- Fragment shader conditionals are very powerful; performance pitfalls very likely to go away
- Mixing image-order and object-order well suited to GPUs (vertex and fragment processing!)
- Deferred shading allows complex filtering and shading at high frame rates

Thank You!

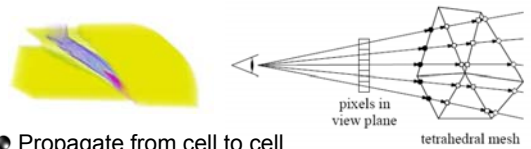


Acknowledgments

- Henning Scharsach, Christian Sigg, Daniel Weiskopf
- VRVis is funded by the Kplus program of the Austrian government

Tetrahedral Grids

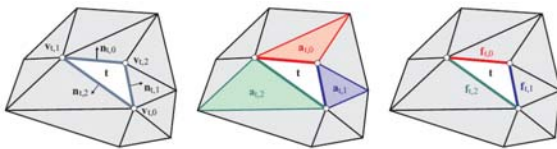
- Traditional (rasterization): Projected Tetrahedra
- Ray casting: store mesh in textures



- Propagate from cell to cell [Weiler et al.]
- Ray/face intersection computations
- Pre-integration; (store current pos in texture)

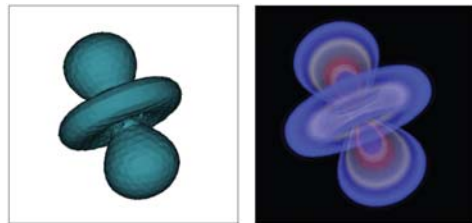
Tetrahedral Grids

- fd



Tetrahedral Grids

- dfd

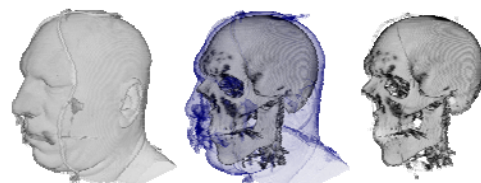


Real-Time Volume Graphics

[05] Transfer Functions

Classification

- During Classification the user defines the „**Look**“ of the data.
 - Which parts are transparent?
 - Which parts have which color?



Classification

- During Classification the user defines the „**Look**“ of the data.
 - Which parts are transparent?
 - Which parts have which color?
- The user defines a **Transfer Function**.

Classification

Classification

Pre- vs Post-Interpolative Classification

Pre-Classification

- **Pre-Classification:**
Color table is applied before interpolation.
(pre-interpolative Transferfunction)

- A color value is fetched from a table **for each Voxel**
- A RGBA Value is determined **for each Voxel**

Possible Implementations

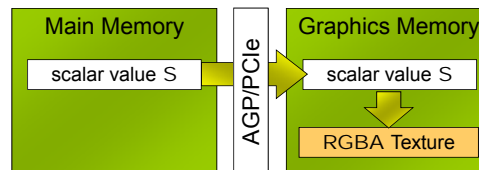
- **The naive Approach:**
Save Emission and Absorption terms directly in the Texture.

Possible Implementations

- **The naive Approach:**
Save Emission and Absorption terms directly in the Texture.
- Very high memory consumption
 - Main Memory (RGBA und scalar volumes)
 - Graphics Memory (RGBA volume)
- High Load on memory bus
RGBA Volume must be transferred.
- **Upload necessary on TF change**

Possible Implementations

- **A better Approach:**
Apply color table during texture transfers from main memory to graphics card (standard OpenGL feature)

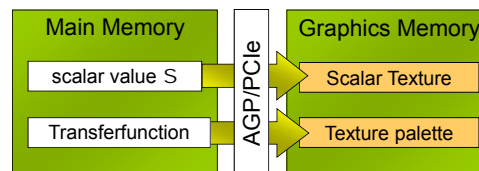


Possible Implementations

- **A better Approach:**
Apply color table during texture transfers from main memory to graphics card (standard OpenGL feature)
- High memory consumption
 - Main Memory (only scalar volume)
 - Graphics Memory (RGBA volume)
- Reduced load on memory bus
 - Only the scalar volume is transferred.
- **Upload necessary on TF change**

Possible Implementations

- **The best approach:** Paletted Textures
Store the scalar volume together with the color table directly in graphics memory.
- Hardware-Support necessary!



Possible Implementations

- **The best approach:** Paletted Textures
Store the scalar volume together with the color table directly in graphics memory.
- Hardware-Support necessary!
- Low memory consumption
 - Main Memory (scalar volume can be deleted!)
 - Graphics Memory (scalar volume + TF)
- Low load on memory bus
 - Scalar volume must be transferred only once!
- **Only the color table must be re-uploaded on TF change**

Pre-Classification Summary

- **Summary Pre-Classification**
 - Application of the Transferfunction before Rasterization
 - One RGBA Lookup **for each Voxel**
 - Different Implementations:
 - Texture Transfer
 - Texture Color Tables (paletted textures)
 - Simple and Efficient
 - Good for coloring segmented data

Post-Classification

- **Post-Classification:**
The color table is applied after Interpolation (*post-interpolative Transfer Function*).

- A color is fetched from the color table **for each Fragment**

Post-Classification

Texture 0 = Scalar field

$R = G = B = A = \text{Scalar field } S$

$\text{RGBA} = T(S)$

Texture 1 = Transfer Function [Emission RGB, Absorption A]

CG Implementation

```

//fragment program for post-classification
//using 3D textures
float4 main (float3 texUV : TEXCOORD0,
             uniform sampler3D volume_texture,
             uniform sampler1D transfer_function) :
    COLOR
{
    float index = tex3D(volume_texture, texUV);
    float4 result = tex1D(transfer_function, index);
    return result;
}
    
```

Quality: Pre- vs. Post-Classification

- Comparison of image quality

Pre-Classification Post-Classification

Same TF, same Resolution, same Sampling Rate

Quality

Pre-Classification Post-Classification

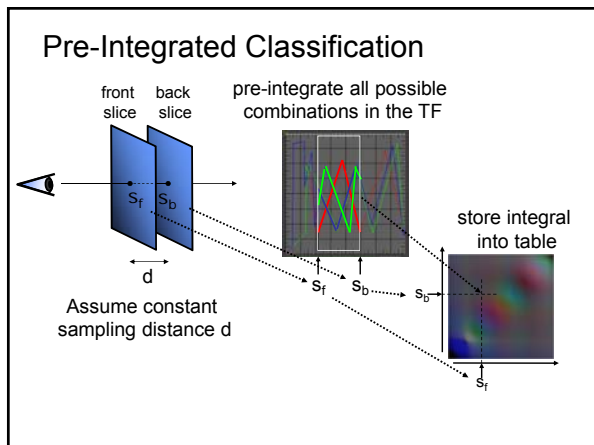
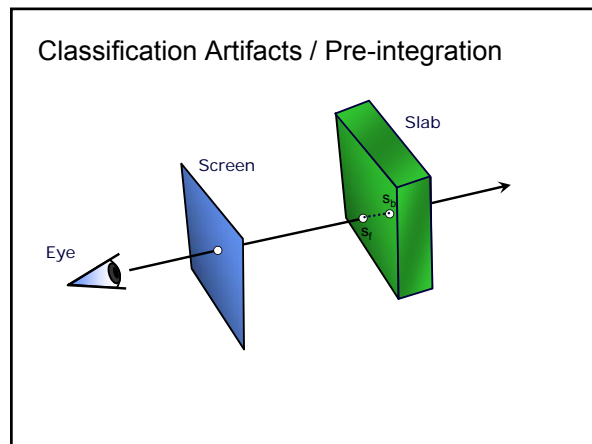
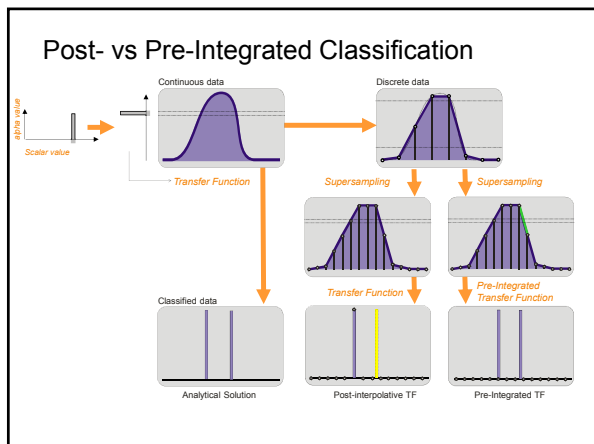
Pre- vs Post-Classification

Continuous data Discrete data

Transfer Function Transfer Function

Supersampling Supersampling

Classified data Analytical Solution Pre-interpolative TF Post-interpolative TF



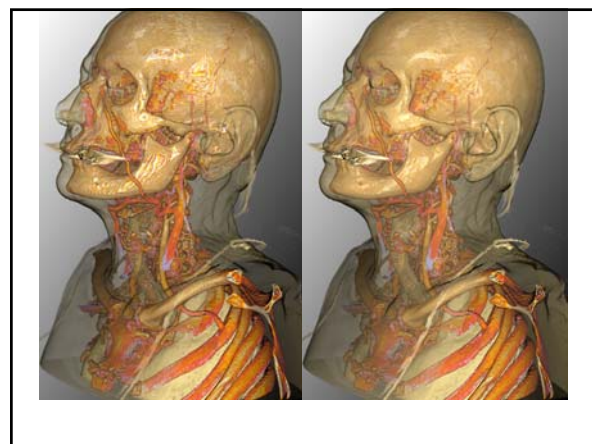
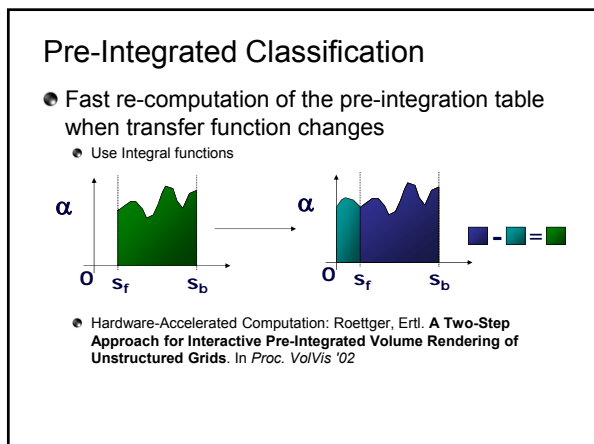
Classification Artifacts / Pre-integration

```

struct v2f_simple {
    float4 Rposition : POSITION;
    float3 TexCoord0 : TEXCOORD0;
    float3 TexCoord1 : TEXCOORD1;
    float4 Color0 : COLOR0;
};

float4 main(v2f_simple IN,
            uniform sampler3D Volume,
            uniform sampler2D TransferFunction,
            uniform sampler2D PreIntegrationTable) : COLOR
{
    float4 lookup;
    //sample front scalar
    lookup.x = tex3D(Volume, IN.TexCoord0.xyz).x;
    //sample back scalar
    lookup.y = tex3D(Volume, IN.TexCoord1.xyz).x;
    //lookup and return pre-integrated value
    return tex2D(PreIntegrationTable, lookup.yx);
}
    
```

Cg Fragment Program



When to use which Classification

- Pre-Interpolative Classification
 - If the graphics hardware does not support fragment shaders
 - For simple segmented volume data visualization
- Post-Interpolative Classification
 - If the transfer function is "smooth"
 - For good quality and good performance (especially when slicing)
- Pre-Integrated Classification
 - If the transfer function contains high frequencies
 - For best quality