

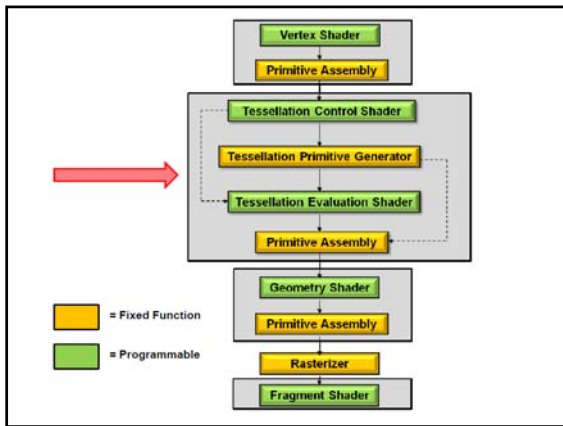
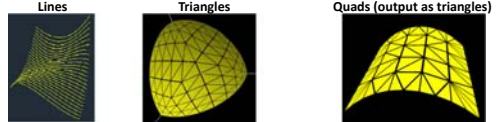
# Tessellation Shaders

Thanks to Mike Bailey (OSU)

## Why a tessellation shader

- You can perform adaptive subdivision based on a variety of criteria (size, curvature, etc.)
- Your application can provide coarser models (≈ geometric compression)
- You can apply detailed displacement maps without supplying equally detailed geometry
- You can adapt visual quality to the required level of detail
- You can create smoother silhouettes

What patterns can the Tessellation shaders produce?



## Another view of the Tess Shader

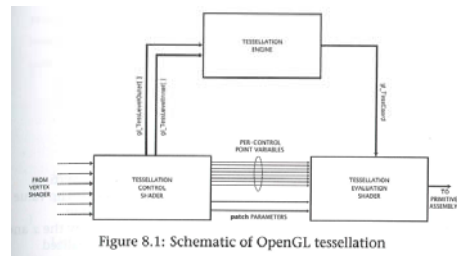
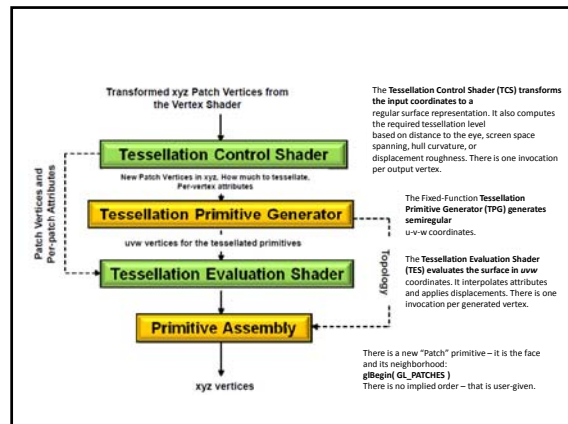
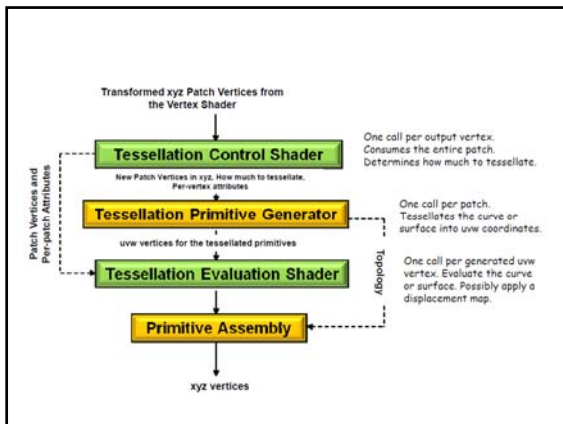


Figure 8.1: Schematic of OpenGL tessellation



### In the OpenGL Program

```

glBegin( GL_PATCHES );
    glVertex3f( ... );
    glVertex3f( ... );
glEnd();

GLuint tcs = glCreateShader( GL_TESS_CONTROL_SHADER );
GLuint tes = glCreateShader( GL_TESS_EVALUATION_SHADER );

glPatchParameteri( GL_PATCH_VERTICES, num );
// vertices in each patch

    
```

These have no implied topology – it's up to how your shader interprets the order

If you have a TCS, you must also have a Vertex Shader

### vertex arrays

```

glGenVertexArrays( 1, &vao );
glBindVertexArray( vao );

glGenBuffers( 1, &position_buffer );
glBindBuffer( GL_ARRAY_BUFFER, position_buffer );
glBufferData( GL_ARRAY_BUFFER,
    sizeof( vertex_positions ),
    vertex_positions,
    GL_STATIC_DRAW );
glVertexAttribPointer( 0, 3, GL_FLOAT, GL_FALSE, 0, NULL );
glEnableVertexAttribArray( 0 );

glGenBuffers( 1, &index_buffer );
glBindBuffer( GL_ELEMENT_ARRAY_BUFFER, index_buffer );
glBufferData( GL_ELEMENT_ARRAY_BUFFER,
    sizeof( vertex_indices ),
    vertex_indices,
    GL_STATIC_DRAW );

glPatchParameters( GL_PATCH_VERTICES, 4 ); // verts per patch TCS in
glDrawElements( GL_PATCHES, 24, GL_UNSIGNED_SHORT, 0 );
    
```

```

static const GLuint vertex_indices[] =
{
    0, 1, 2, 3,
    2, 3, 4, 5,
    4, 5, 6, 7,
    6, 7, 0, 1,
    0, 2, 6, 4,
    1, 7, 3, 5
};

static const GLfloat vertex_positions[] =
{
    -0.25f, -0.25f, -0.25f,
    -0.25f, 0.25f, -0.25f,
    0.25f, -0.25f, -0.25f,
    0.25f, 0.25f, -0.25f,
    0.25f, -0.25f, 0.25f,
    -0.25f, 0.25f, 0.25f,
    -0.25f, -0.25f, 0.25f,
    0.25f, 0.25f, 0.25f
};
    
```

### TCS Inputs

- gl\_in[ ]** is an array of structures containing:
  - gl\_Position
  - gl\_PointSize
  - gl\_ClipDistance[ ]
- gl\_InvocationID** tells you which output vertex you are working on, This *must be the* index into the **gl\_out[ ]** array.
- gl\_PatchVerticesIn** is the number of vertices in each patch and the dimension of **gl\_in[ ]**
- gl\_PrimitiveID** is the number of primitives since last **glBegin( )** (the first one is #0)
- barrier( )** causes all instances of TCS's to wait here

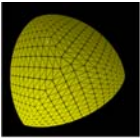
### TCS Outputs

- gl\_out[ ]** is an array of structures containing:
  - gl\_Position;
  - gl\_PointSize;
  - gl\_ClipDistance[ ];
- All invocations of the TCS have read-only access to all the output information. **barrier( )** causes all instances of TCS's to wait here
- layout( vertices = n ) out;** Used to specify the number of vertices output to the TPG
- Defining how many vertices this patch will output:
  - layout( vertices = 16 ) out;**
- gl\_TessLevelOuter[4]** is an array containing up to 4 edges of tessellation levels
- gl\_TessLevelInner[2]** is an array containing up to 2 edges of tessellation levels
- User-defined variables defined per-vertex are qualified as "out"
- User-defined variables defined per-patch are qualified as "patch out"

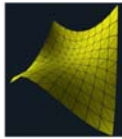
### Tessellation Primitive Generator

- Is "fixed-function", i.e., you can't change its operation except by setting parameters
- Consumes all vertices from the TCS and emits tessellated **triangles, quads, or lines**
- Outputs positions (vertices) as coordinates in barycentric (u,v,w)
- All three coordinates (u,v,w) are used for triangles
- Just (u,v) are used for quads and isolines

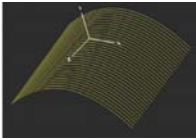
Triangle



Quad



Isolines



### TES Inputs

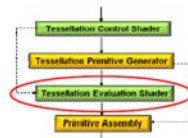
Reads one vertex of 0 <= (u,v,w) <= 1 coordinates in variable vec3 gl\_TessCoord

User-defined variables defined per-vertex are qualified as "out"  
User-defined variables defined per-patch are qualified as "patch out"

gl\_in[ ] is an array of structures coming from the TCS containing:

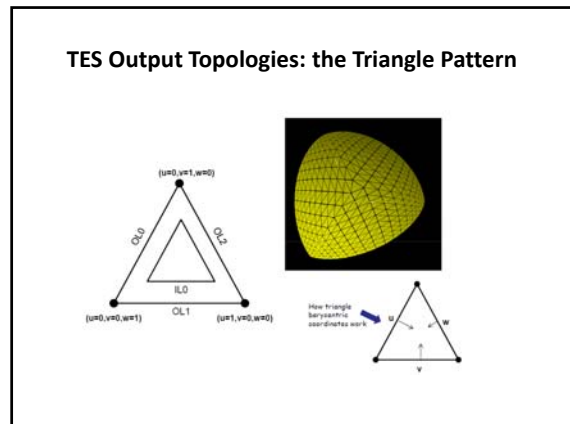
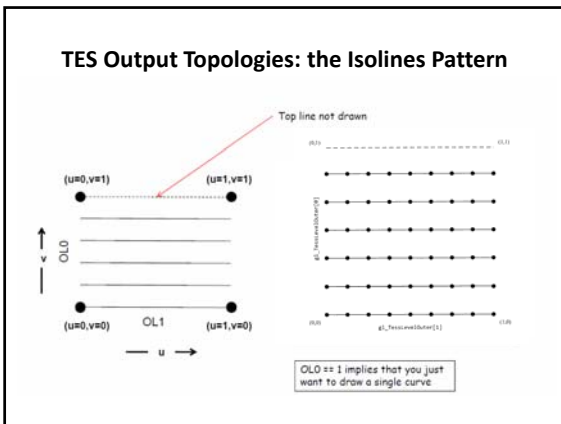
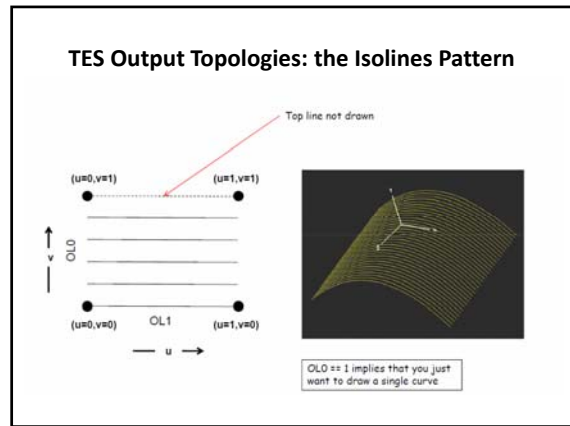
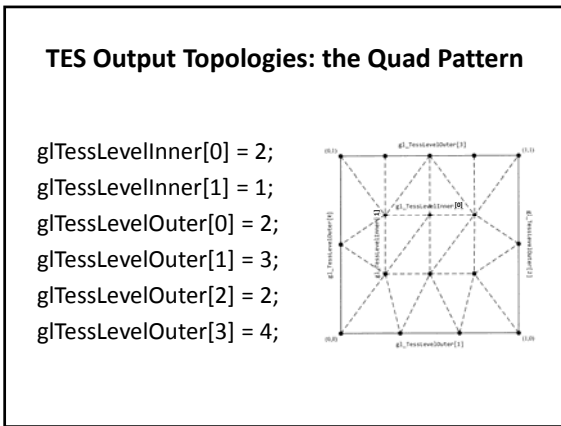
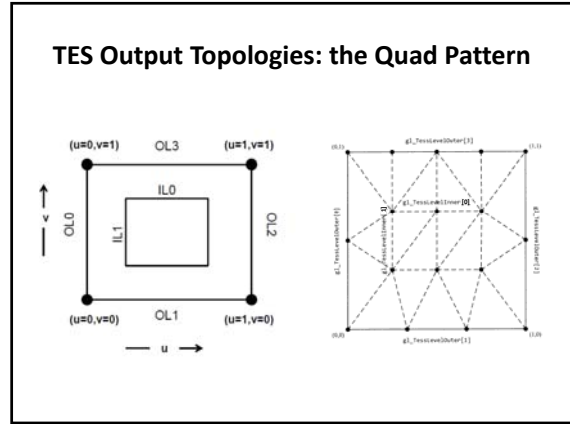
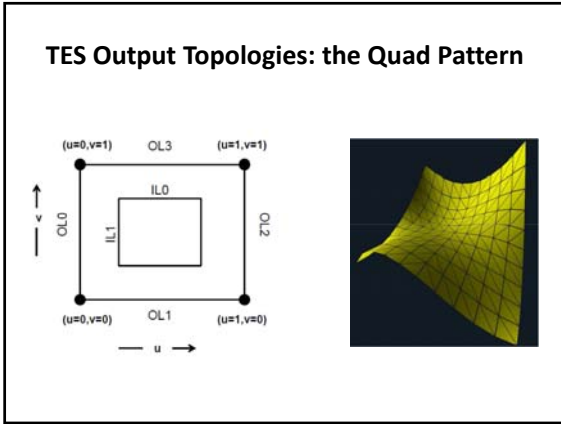
```

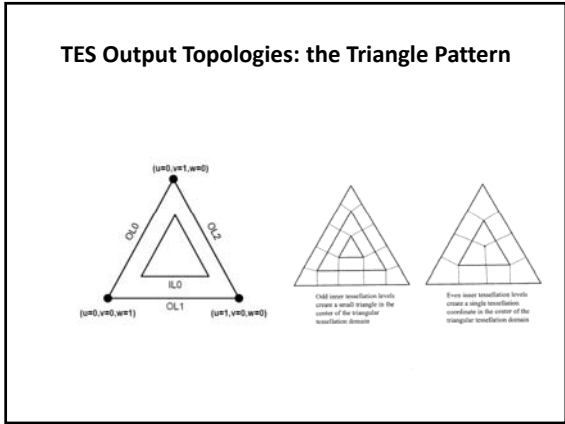
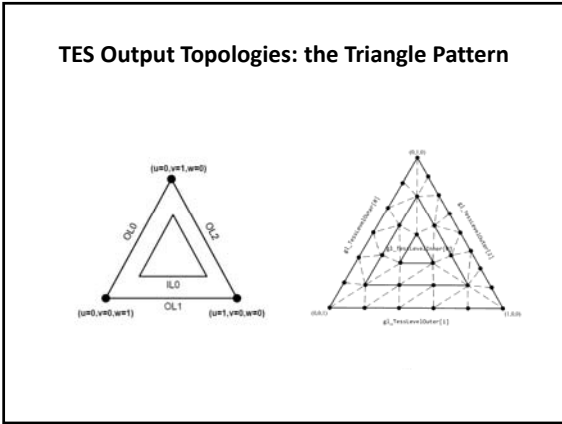
gl_Position;
gl_PointSize;
gl_ClipDistance[ ];
    
```



```

layout(
    triangles, equal_spacing,
    quads, fractional_even_spacing,
    isolines, fractional_odd_spacing
) . { ccw, cw }, point_mode ) in;
    
```

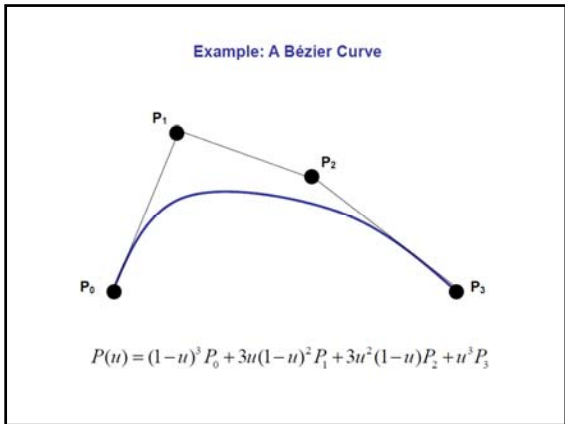




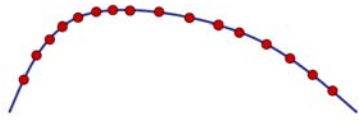
### Demo tessmodes

- ### TES subdivision
- layout(triangles, equal\_spacing, ccw) in;
  - **equal\_spacing** means that the triangle edges will be subdivided into segments with equal lengths (according to the TLs).
  - **fractional\_even\_spacing** means if there is a fractional portion based on TLs, it is evenly split between the ends.
  - **fractional\_odd\_spacing** means if there is a fractional portion based on TLs, it is not evenly split between the ends.

### Demo tesssubdivisionmodes



### Example: A Bézier Curve



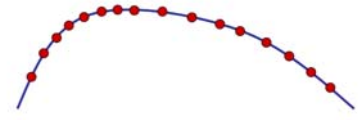
$$P(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u) P_2 + u^3 P_3$$

1. The Tessellation Control Shader figures how much to tessellate the curve based on screen area, curvature, etc.

Can tessellate non-uniformly if desired

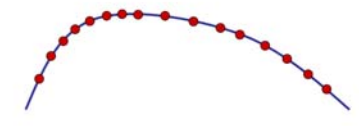
The OpenGL tessellation can also do 1D curves. Just set OLO = 1.

### Example: A Bézier Curve



2. The Tessellation Primitive Generator generates  $u[v,w]$  values for as many subdivisions as the TCS asked for.

### Example: A Bézier Curve



$$P(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u) P_2 + u^3 P_3$$

3. The Tessellation Evaluation Shader computes the  $x,y,z$  coordinates based on the TPG's  $u$  values

$$P(u) = u^3(-P_0 + 3P_1 - 3P_2 + P_3) + u^2(3P_0 - 6P_1 + 3P_2) + u(-3P_0 + 3P_1) + P_0$$

### In the OpenGL Program

```

glPatchParameteri( GL_PATCH_VERTICES, 4 );
glBegin( GL_PATCHES );
    glVertex3f( x0, y0, z0 );
    glVertex3f( x1, y1, z1 );
    glVertex3f( x2, y2, z2 );
    glVertex3f( x3, y3, z3 );
glEnd();
    
```

### In the TCS Shader

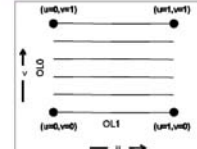
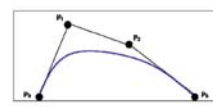
```

#version 400
#extension GL_ARB_tessellation_shader: enable

uniform int uOuter0, uOuter1;

layout( vertices = 4 ) out;

void main()
{
    gl_out[ gl_InvocationID ] gl_Position = gl_in[ gl_InvocationID ].gl_Position;
    gl_TessLevelOuter[0] = float( uOuter0 );
    gl_TessLevelOuter[1] = float( uOuter1 );
}
    
```

### In the TES Shader

```

#version 400
#extension GL_ARB_tessellation_shader: enable

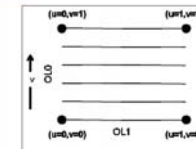
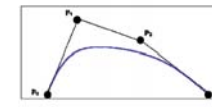
layout( isolines, equal_spacing ) in;

void main()
{
    vec4 p0 = gl_in[0].gl_Position;
    vec4 p1 = gl_in[1].gl_Position;
    vec4 p2 = gl_in[2].gl_Position;
    vec4 p3 = gl_in[3].gl_Position;

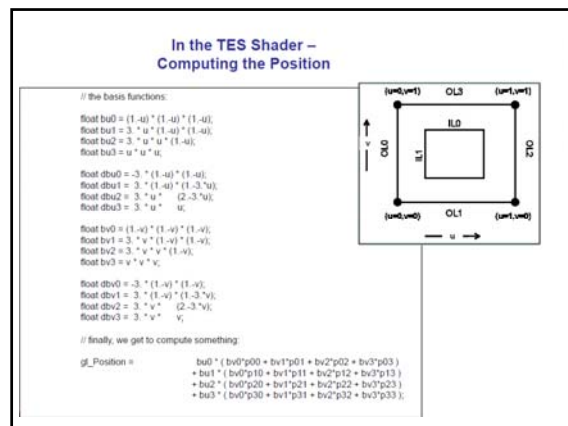
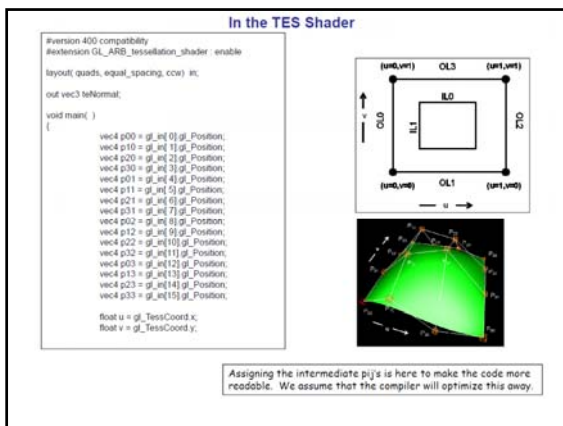
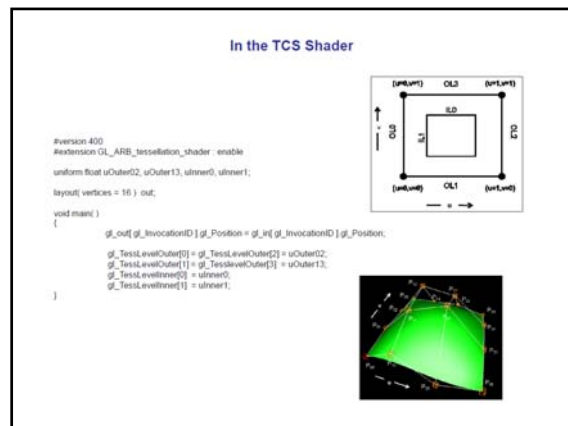
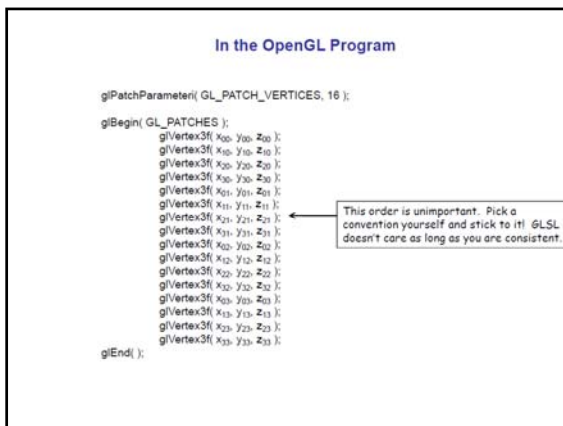
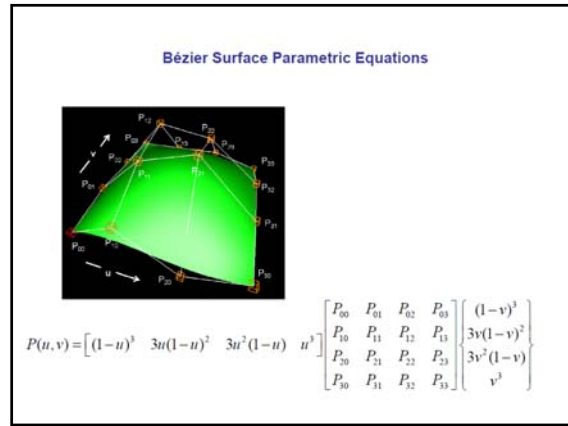
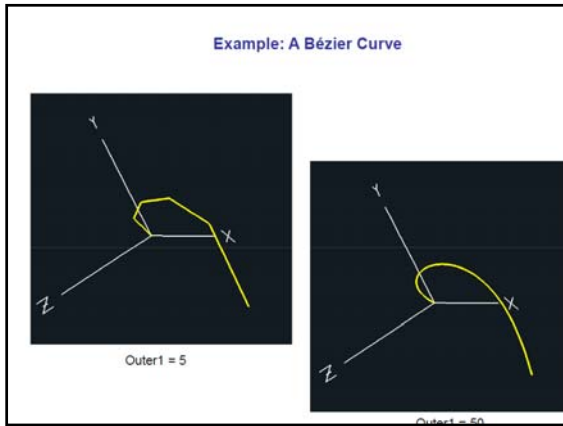
    float u = gl_TessCoord.x;

    // the basis functions:
    float b0 = (1-u) * (1-u) * (1-u);
    float b1 = 3 * u * (1-u) * (1-u);
    float b2 = 3 * u * u * (1-u);
    float b3 = u * u * u;

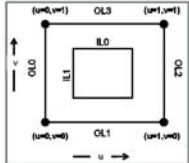
    gl_Position = b0*p0 + b1*p1 + b2*p2 + b3*p3;
}
    
```

Assigning the intermediate  $p_i$ 's is here to make the code more readable. We assume that the compiler will optimize this away.



### In the TES Shader – Computing the Normal



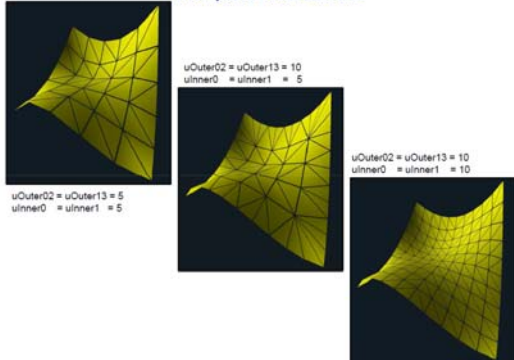
```

vec4 dpdu = dbu0 * (bv0*p00 + bv1*p01 + bv2*p02 + bv3*p03)
            + dbu1 * (bv0*p10 + bv1*p11 + bv2*p12 + bv3*p13)
            + dbu2 * (bv0*p20 + bv1*p21 + bv2*p22 + bv3*p23)
            + dbu3 * (bv0*p30 + bv1*p31 + bv2*p32 + bv3*p33);

vec4 dpdv = dbv0 * (dv0*p00 + dv1*p01 + dv2*p02 + dv3*p03)
            + dbv1 * (dv0*p10 + dv1*p11 + dv2*p12 + dv3*p13)
            + dbv2 * (dv0*p20 + dv1*p21 + dv2*p22 + dv3*p23)
            + dbv3 * (dv0*p30 + dv1*p31 + dv2*p32 + dv3*p33);

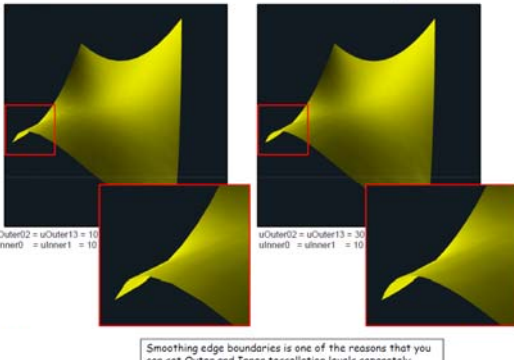
InNormal = normalize(cross( dpdu.xyz, dpdv.xyz ));
    
```

### Example: A Bézier Surface



## Bezier Patch

### Tessellation Levels and Smooth Shading



### Example: Whole-Sphere Subdivision

```

spheresubd.vert
#version 400 compatibility
out vec3 vCenter;
out float vRadius;

void main()
{
    vCenter = aVertex.xyz;
    vRadius = aVertex.w;
    gl_Position = vec4( 0, 0, 0, 1 );
}
    
```

Using the x, y, z, and w to specify the center and radius of the sphere

### Example: Whole-Sphere Subdivision

```

spheresubd.tcs
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

in float vRadius[ ];
in vec3 vCenter[ ];

patch out float trRadius;
patch out vec3 tcCenter;

uniform float uDetail;
uniform float uScale;

layout( vertices = 1 ) out;

void main()
{
    gl_out[ gl_InvocationID ] gl_Position = gl_in[ 0 ].gl_Position; // (0,0,0,1)

    tcCenter = vCenter[ 0 ];
    trRadius = vRadius[ 0 ];

    gl_TessLevelOuter[0] = 2;
    gl_TessLevelOuter[1] = uScale * trRadius * uDetail;
    gl_TessLevelOuter[2] = 2;
    gl_TessLevelOuter[3] = uScale * trRadius * uDetail;
    gl_TessLevelInner[0] = uScale * trRadius * uDetail;
    gl_TessLevelInner[1] = uScale * trRadius * uDetail;
}
    
```

Using the scale and the radius to help set the tessellation detail

Outer[0] and Outer[2] are the number of divisions at the poles. Outer[1] and Outer[3] are the number of divisions at the vertical seams. Inner[0] and Inner[1] are the inside sphere detail.



### Example: Whole-Sphere Subdivision

```

spheresubd.tes
#version 430 compatibility
#extension GL_ARB_tessellation_shader : enable

uniform float uScale;

layout( quads, equal_spacing, cwa ) in;

patch in float tRadius;
patch in vec3 tCenter;

out vec3 tNormal;

const float PI = 3.14159265;

void main()
{
    vec3 p = gl_Position.xyz;
    float u = gl_TessCoord.x;
    float v = gl_TessCoord.y;
    float w = gl_TessCoord.z;

    float phi = PI * (u - .5);
    float theta = 2 * PI * (v - .5);

    float cosphi = cos(phi);
    vec3 xyz = vec3(cosphi*cos(theta), sinphi*cos(theta),
    tNormal = xyz;

    xyz *= (uScale * tRadius);
    xyz += tCenter;

    gl_Position = uModelViewMatrix * vec4(xyz, 1.);
}
    
```

Turning u and v into spherical coordinates

$-\pi \leq \theta \leq \pi$   
 $-\pi \leq \phi \leq \pi$

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### Example: Whole-Sphere Subdivision

Detail=30, Scale=1

Detail=50, Scale=1

Detail=50, Scale=2.5

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### Making the Whole-Sphere Subdivision Adapt to Screen Coverage

```

sphereadapt.tcs.1
#version 430 compatibility
#extension GL_ARB_tessellation_shader : enable

in float vRadius;
in vec3 vCenter;

patch out float tRadius;
patch out vec3 tCenter;

uniform float uDetail;

layout( vertices = 1 ) out;

void main()
{
    gl_Out[gl_InvocationID] gl_Position = gl_In[0] gl_Position; // (0,0,0,1)
    tCenter = vCenter[0];
    tRadius = vRadius[0];

    vec4 mx = vec4(vCenter[0] - vec3(vRadius[0], 0, 0), 1.);
    vec4 px = vec4(vCenter[0] + vec3(vRadius[0], 0, 0), 1.);
    vec4 my = vec4(vCenter[0], vCenter[1] - vRadius[0], 0, 1.);
    vec4 py = vec4(vCenter[0], vCenter[1] + vRadius[0], 0, 1.);
    vec4 mz = vec4(vCenter[0], 0, vCenter[2] - vRadius[0], 1.);
    vec4 pz = vec4(vCenter[0], 0, vCenter[2] + vRadius[0], 1.);

    Extreme points of the sphere
}
    
```

Extreme points of the sphere

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### Making the Whole-Sphere Subdivision Adapt to Screen Coverage

```

sphereadapt.tcs.11
mx = uModelViewProjectionMatrix * mx;
px = uModelViewProjectionMatrix * px;
my = uModelViewProjectionMatrix * my;
py = uModelViewProjectionMatrix * py;
mz = uModelViewProjectionMatrix * mz;
pz = uModelViewProjectionMatrix * pz;

mx.xy /= mx.w;
px.xy /= px.w;
my.xy /= my.w;
py.xy /= py.w;
mz.xy /= mz.w;
pz.xy /= pz.w;

float dx = distance(mx.xy, px.xy);
float dy = distance(my.xy, py.xy);
float dz = distance(mz.xy, pz.xy);
float dmax = sqrt(dx*dx + dy*dy + dz*dz);

gl_TessLevelOuter[0] = 2.;
gl_TessLevelOuter[1] = dmax * uDetail;
gl_TessLevelOuter[2] = 2.;
gl_TessLevelInner[0] = dmax * uDetail;
gl_TessLevelInner[1] = dmax * uDetail;
gl_TessLevelInner[2] = 1.;
}
    
```

Extreme points of the sphere in Clip space

Extreme points of the sphere in NDC space

How large are the lines between the extreme points?

We no longer use uScale or tRadius. But, we do use uDetail to provide a way to convert from NDC to Screen Space or to indicate the quality you'd like (i.e., uDetail depends on how good you want the sphere to look and on how large the window is in pixels).

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### Making the Whole-Sphere Subdivision Adapt to Screen Coverage

```

sphereadapt.tes
#version 430 compatibility
#extension GL_ARB_tessellation_shader : enable

layout( quads, equal_spacing, cwa ) in;

patch in float tRadius;
patch in vec3 tCenter;

out vec3 tNormal;

const float PI = 3.14159265;

void main()
{
    vec3 p = gl_Position.xyz;
    float u = gl_TessCoord.x;
    float v = gl_TessCoord.y;
    float w = gl_TessCoord.z;

    float phi = PI * (u - .5);
    float theta = 2 * PI * (v - .5);

    float cosphi = cos(phi);
    vec3 xyz = vec3(cosphi*cos(theta), sinphi*cos(theta),
    tNormal = xyz;

    xyz *= tRadius;
    xyz += tCenter;

    gl_Position = uModelViewMatrix * vec4(xyz, 1.);
}
    
```

Spherical coordinates

No longer uses uScale

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### Making the Whole-Sphere Subdivision Adapt to Screen Coverage

Original

Triangles Shrunken

Zoomed In

Zoomed Out

Rotated

Notice that the number of triangles adapts to the screen coverage of each sphere, and that the size of the tessellated triangles stays about the same, regardless of radius or transformation

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### Example: PN Triangles

General idea: turn each triangle into a triangular Bezier patch. Create the Bezier control points by using the surface normals at the corner vertices. The Bezier patch equation can then be interpolated to any level of tessellation.

Alex Viachos, Jörg Peters, Chas Boyd, and Jason Mitchell, "Curved PN Triangles", Proceedings of the 2001 Symposium on Interactive 3D Graphics, pp. 159 – 166.

### Example: PN Triangles

```

pntriangles.vert
#version 400 compatibility
uniform float uScale;
out vec3 vNormal;

void main()
{
    vec3 xyz = aVertex.xyz;
    xyz *= uScale;
    gl_Position = aModelViewMatrix * vec4( xyz, 1. );
    vNormal = normalize( aNormalMatrix * aNormal );
}

pntriangles.tcs
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable
uniform int uOuter, uInner;
uniform float uScale;

layout( vertices = 3 ) out;
in vec3 vNormal;
out vec3 tNormal;

void main()
{
    tNormal[ gl_InnovationID ] = vNormal[ gl_InnovationID ];
    gl_InvocationID[ gl_Position = gl_InvocationID ] gl_Position;

    gl_TessLevelOuter[0] = uScale * float(uOuter);
    gl_TessLevelOuter[1] = uScale * float(uOuter);
    gl_TessLevelOuter[2] = uScale * float(uOuter);
    gl_TessLevelInner[0] = uScale * float(uInner);
}
    
```

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### Example: PN Triangles

```

pntriangles.tes, I
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable
in vec3 tNormal;
out vec3 bNormal;

layout( triangles, equal_spacing, cwi ) in;

void main()
{
    vec3 p1 = gl_in[0].gl_Position.xyz;
    vec3 p2 = gl_in[1].gl_Position.xyz;
    vec3 p3 = gl_in[2].gl_Position.xyz;

    vec3 n1 = tNormal[0];
    vec3 n2 = tNormal[1];
    vec3 n3 = tNormal[2];

    float u = gl_TessCoord.x;
    float v = gl_TessCoord.y;
    float w = gl_TessCoord.z;

    vec3 b000 = p1;
    vec3 b001 = p2;
    vec3 b002 = p3;

    float w12 = dot( p2 - p1, n1 );
    float w21 = dot( p1 - p2, n2 );
    float w13 = dot( p3 - p1, n1 );
    float w31 = dot( p1 - p3, n3 );
    float w23 = dot( p3 - p2, n2 );
    float w32 = dot( p2 - p3, n3 );
}
    
```

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### Example: PN Triangles

```

pntriangles.tes, II
vec3 b210 = ( 2 * p1 + p2 - w12 * n1 ) / 3.;
vec3 b120 = ( 2 * p2 + p1 - w21 * n2 ) / 3.;
vec3 b021 = ( 2 * p2 + p3 - w23 * n2 ) / 3.;
vec3 b012 = ( 2 * p3 + p2 - w32 * n3 ) / 3.;
vec3 b102 = ( 2 * p3 + p1 - w31 * n3 ) / 3.;
vec3 b201 = ( 2 * p1 + p3 - w13 * n1 ) / 3.;

vec3 ee = ( b210 + b120 + b021 + b012 + b201 + b102 ) / 6.;
vec3 ww = ( p1 + p2 + p3 ) / 3.;
vec3 b111 = ee + ( ee - ww ) / 2.;

vec3 xyz = 1 * b000 * w * w * w + 1 * b001 * u * u * u + 1 * b002 * v * v * v +
3 * b210 * u * w * w + 3 * b120 * u * v * v + 3 * b021 * u * v * w +
3 * b012 * u * v * w + 3 * b102 * v * w * w +
6 * b111 * u * v * w;

float v12 = 2 * dot( p2 - p1, n1 + n2 ) / dot( p2 - p1, p2 - p1 );
float v23 = 2 * dot( p3 - p2, n2 + n3 ) / dot( p3 - p2, p3 - p2 );
float v31 = 2 * dot( p1 - p3, n3 + n1 ) / dot( p1 - p3, p1 - p3 );

vec3 r000 = n1;
vec3 r001 = n2;
vec3 r002 = n3;
vec3 r110 = normalize( n1 + n2 - v12 * (p2 - p1) );
vec3 r011 = normalize( n2 + n3 - v23 * (p3 - p2) );
vec3 r101 = normalize( n3 + n1 - v31 * (p1 - p3) );

Normal = r000 * w * w + r001 * u * u + r002 * v * v +
n1 * w * u + n1 * u * v + n1 * v * w;

gl_Position = vec4( xyz, 1. );
    
```

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### Example: PN Triangles

```

pntriangles.geom
#version 400 compatibility
#extension GL_gpu_shader4 : enable
#extension GL_geometry_shader4 : enable

uniform float uScale;
in vec3 tNormal;
out float glLightIntensity;

const vec3 LIGHTPOS = vec3( 5, 10, 10 );

vec3 VTE;
vec3 CG;

void ProduceVertex( in v )
{
    glLightIntensity = abs( dot( normalize( LIGHTPOS - VTE ), normalize( bNormal[0] ) ) );
    gl_Position = aProjectionMatrix * vec4( CG + aCamera * ( VTE - CG ), 1. );
    EmitVertex();
}

void main()
{
    V[0] = gl_Position[0].xyz;
    V[1] = gl_Position[1].xyz;
    V[2] = gl_Position[2].xyz;

    CG = ( V[0] + V[1] + V[2] ) / 3.;

    ProduceVertex( 0 );
    ProduceVertex( 1 );
    ProduceVertex( 2 );
}
    
```

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### Example: PN Triangles

```

pntriangles.frag
#version 400 compatibility

in float glLightIntensity;
out vec4 fFragColor;

const vec3 COLOR = vec3( 1, 1, 0 );

void main()
{
    fFragColor = vec4( glLightIntensity * COLOR, 1 );
}
    
```

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