



# Lighting




# Objectives

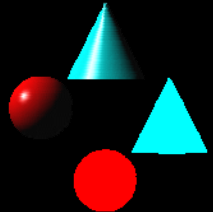


- Learn to shade objects so their images appear three-dimensional
- Introduce the types of light-material interactions
- Build a simple reflection model---the Phong model--- that can be used with real time graphics hardware

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# Lighting Principles

- Lighting simulates how objects reflect light
  - material composition of object
  - light's color and position
  - global lighting parameters
    - ambient light
    - two sided lighting
  - available in both color index and RGBA mode








# Why we need shading

- Suppose we build a model of a sphere using many polygons and color it with glColor. We get something like




- But we want



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# Shading

- Why does the image of a real sphere look like



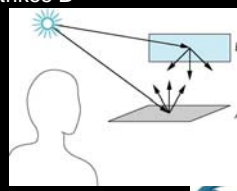


- Light-material interactions cause each point to have a different color or shade
- Need to consider
  - Light sources
  - Material properties
  - Location of viewer
  - Surface orientation

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# Scattering

- Light strikes A
  - Some scattered
  - Some absorbed
- Some of scattered light strikes B
  - Some scattered
  - Some absorbed
- Some of this scattered light strikes A and so on

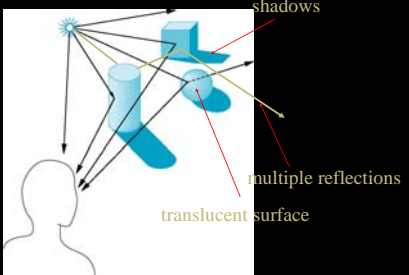
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### Rendering Equation

- The infinite scattering and absorption of light can be described by the *rendering equation*
  - Cannot be solved analytically in general
  - Ray tracing is a special case for perfectly reflecting surfaces
- Rendering equation is global and includes
  - Shadows
  - Multiple scattering from object to object

OpenGL

### Global Effects



OpenGL

### Local vs Global Rendering

- Correct shading requires a global calculation involving all objects and light sources
  - Incompatible with pipeline model which shades each polygon independently (local rendering)
- However, in computer graphics, especially real time graphics, we are happy if things “look right”
  - Exist many techniques for approximating global effects

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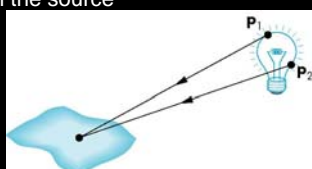
### Light-Material Interaction

- Light that strikes an object is partially absorbed and partially scattered (reflected)
- The amount reflected determines the color and brightness of the object
  - A surface appears red under white light because the red component of the light is reflected and the rest is absorbed
- The reflected light is scattered in a manner that depends on the smoothness and orientation of the surface

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### Light Sources

General light sources are difficult to work with because we must integrate light coming from all points on the source



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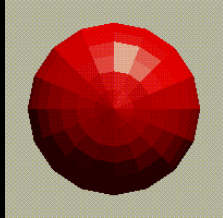
### Simple Light Sources

- Point source
  - Model with position and color
  - Distant source = infinite distance away (parallel)
- Spotlight
  - Restrict light from ideal point source
- Ambient light
  - Same amount of light everywhere in scene
  - Can model contribution of many sources and reflecting surfaces


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## Shading Schemes

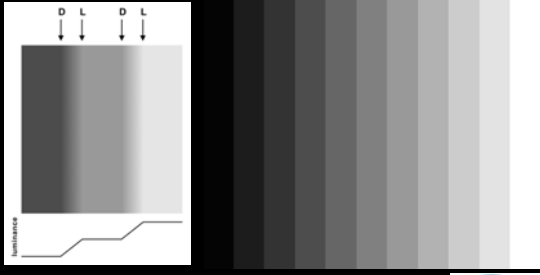
Flat Shading: same shade to entire polygon




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## Mach Band Illusion




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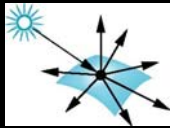


## Surface Types

- The smoother a surface, the more reflected light is concentrated in the direction a perfect mirror would reflected the light
- A very rough surface scatters light in all directions




smooth surface



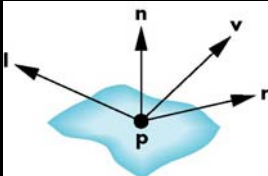
rough surface

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## Phong Model

- A simple model that can be computed rapidly
- Has three components
  - Diffuse
  - Specular
  - Ambient
- Uses four vectors
  - To source
  - To viewer
  - Normal
  - Perfect reflector

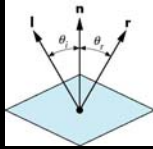


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## Ideal Reflector

- Normal is determined by local orientation
- Angle of incidence = angle of reflection
- The three vectors must be coplanar

$$r = 2(l \cdot n)n - l$$



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## Lambertian Surface

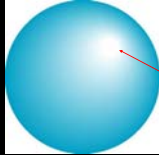
- Perfectly diffuse reflector
- Light scattered equally in all directions
- Amount of light reflected is proportional to the vertical component of incoming light
  - reflected light  $\sim \cos \theta_i$
  - $\cos \theta_i = l \cdot n$  if vectors normalized
  - There are also three coefficients,  $k_r, k_g, k_b$  that show how much of each color component is reflected

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### Specular Surfaces

- Most surfaces are neither ideal diffusers nor perfectly specular (ideal reflectors)
- Smooth surfaces show specular highlights due to incoming light being reflected in directions concentrated close to the direction of a perfect reflection



specular highlight

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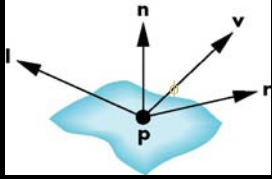
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### Modeling Specular Reflections

- Phong proposed using a term that dropped off as the angle between the viewer and the ideal reflection increased

$$I_r \sim k_s I \cos^q \phi$$

reflected intensity      shininess coef  
incoming intensity      absorption coef

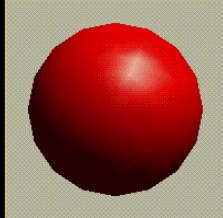


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### Shading Schemes

*Gouraud Shading:*  
smoothly blended intensity across each polygon




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### Shading Schemes

Phong Shading:  
interpolated normals to compute intensity at each point

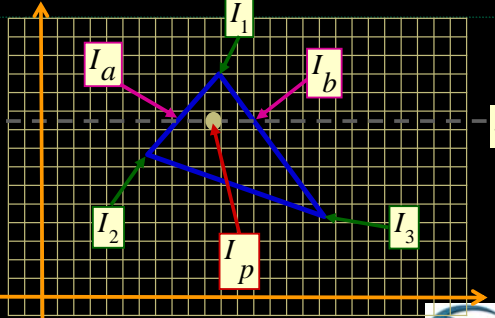


Bui Toung Phong

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### Scan Convert Polygon P

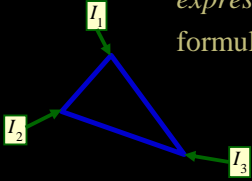


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### Intensity Interpolation

$I_1, I_2, I_3$ : Compute by direction evaluation of illumination expression, whichever formula is being used

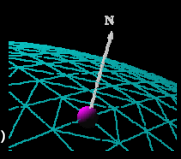


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### Surface Normals

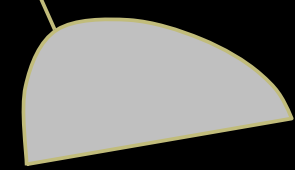
- Normals define how a surface reflects light
  - `glNormal3f( x, y, z )`
  - Current normal is used to compute vertex's color
  - Use *unit* normals for proper lighting
    - scaling affects a normal's length
    - `glEnable( GL_NORMALIZE )`
    - or
    - `glEnable( GL_RESCALE_NORMAL )`



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### Using Average Normals

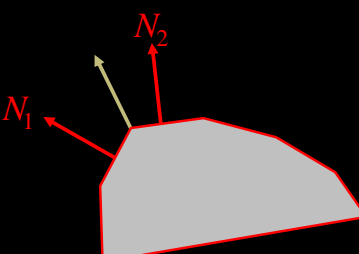
$N = \text{true (geometric) normal}$



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### Using Average Normals

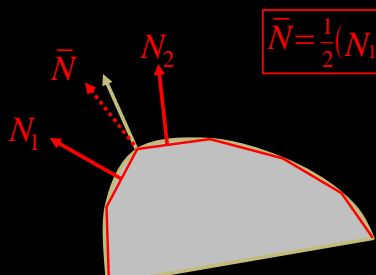


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### Using Average Normals

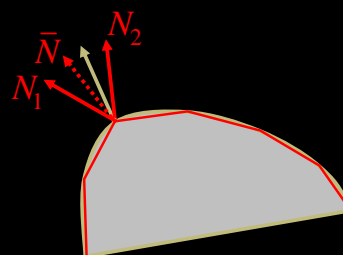
$\bar{N} = \frac{1}{2}(N_1 + N_2)$



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### Using Average Normals



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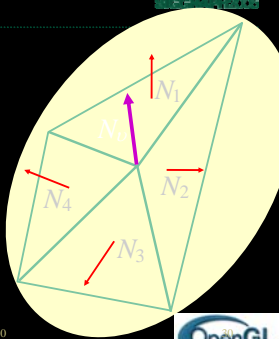
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### What should corner normals be?

$N_v = \frac{(N_1 + N_2 + N_3 + N_4)}{\|N_1 + N_2 + N_3 + N_4\|}$

More generally,

$N_v = \frac{\sum_{i=1}^n N_i}{\left\| \sum_{i=1}^n N_i \right\|}$



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### Relevant Light (unit) Vectors

Surface Normal

Point light source direction

Reflection direction

Viewpoint direction

$\theta$   $\theta$   $\alpha$

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### Flat (Cosine) Shading

- Compute constant shading function, over each polygon, based on simple cosine term
- Same normal and light vector across whole polygon
- Constant shading for polygon

$\sim N \cdot L$

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### Relevant Light (unit) Vectors

Surface Normal

Point light source direction

Reflection direction

Viewpoint direction

$\theta$   $\theta$   $\alpha$

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### Flat (Cosine) Shading

$$I = I_p k_d \cos(\theta)$$

$$= I_p k_d N \cdot L, \text{ for unit } N, L$$

Where,

$I_p =$  intensity of point light source

$k_d =$  diffuse reflection coefficient

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### Gouraud Shading

- Compute constant shading function, for each vertex, based on simple cosine term
- different normal and light vector for each vertex
- Interpolated shading for polygon

$\sim N \cdot L$

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### Intensity Interpolation (Gouraud)

$$I_a = I_1 \frac{y_s - y_2}{y_1 - y_2} + I_2 \frac{y_1 - y_s}{y_1 - y_2}$$

$$I_b = I_1 \frac{y_s - y_3}{y_1 - y_3} + I_3 \frac{y_1 - y_s}{y_1 - y_3}$$

$$I_p = I_a \frac{x_b - x_p}{x_b - x_a} + I_b \frac{x_p - x_a}{x_b - x_a}$$

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### Normal Interpolation (Phong)

$$N_a = N_1 \frac{y_3 - y_2}{y_1 - y_2} + N_2 \frac{y_1 - y_3}{y_1 - y_2}$$

$$N_b = N_1 \frac{y_3 - y_3}{y_1 - y_3} + N_3 \frac{y_1 - y_3}{y_1 - y_3}$$

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### Normal Interpolation (Phong)

$$\tilde{N}_p = \frac{N_a}{\|N_a\|} \begin{bmatrix} x_b - x_p \\ x_b - x_a \end{bmatrix} + \frac{N_b}{\|N_b\|} \begin{bmatrix} x_p - x_a \\ x_b - x_a \end{bmatrix}$$

$$N_p = \frac{\tilde{N}_p}{\|\tilde{N}_p\|}$$

Normalizing makes this a unit vector

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### Phong Illumination Formula (1/2)

$$I_\lambda = I_{a\lambda} k_{a\lambda} + f_{att} I_\lambda \left[ k_{d\lambda} (N \cdot L) + k_{s\lambda} (R \cdot V)^n \right]$$

$\cos^n(\alpha)$

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### Illumination Formula (2/2)

Where,

- $a$  denotes ambient term
- $d$  denotes diffuse term
- $s$  denotes specular term
- $k$  denotes coefficient
- $I$  denotes intensity

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### Effect of Exponent Parameter

As  $n$  increases, highlight is more concentrated, surface appears glossier

$\alpha = -\frac{\pi}{2}$     $\alpha = 0$     $\alpha = \frac{\pi}{2}$

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### How OpenGL Simulates Lights

- Phong lighting model
  - Computed at vertices
- Lighting contributors
  - Surface material properties
  - Light properties
  - Lighting model properties

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## Surface Normals

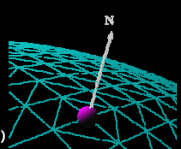

- Normals define how a surface reflects light
  - Current normal is used to compute vertex's color
  - Use *unit* normals for proper lighting
    - scaling affects a normal's length

```
glNormal3f( x, y, z )
```

```
glEnable( GL_NORMALIZE )
```

or

```
glEnable( GL_RESCALE_NORMAL )
```


## Material Properties

- Define the surface properties of a primitive
 

```
glMaterialfv( face, property, value );
```

GL_DIFFUSE	Base color
GL_SPECULAR	Highlight Color
GL_AMBIENT	Low-light Color
GL_EMISSION	Glow Color
GL_SHININESS	Surface Smoothness

  - separate materials for front and back




## Light Properties

```
glLightfv( light, property, value );
```

- light* specifies which light
  - multiple lights, starting with GL\_LIGHT0
 

```
glGetIntegerv( GL_MAX_LIGHTS, &n );
```
- properties*
  - colors
  - position and type
  - attenuation




## Light Sources (cont'd.)

- Light color properties
  - GL\_AMBIENT
  - GL\_DIFFUSE
  - GL\_SPECULAR



## Types of Lights

- OpenGL supports two types of Lights
  - Local (Point) light sources
  - Infinite (Directional) light sources
- Type of light controlled by *w* coordinate
  - $w = 0$  *Infinite Light directed along*  $(x \ y \ z)$
  - $w \neq 0$  *Local Light positioned at*  $(\frac{x}{w} \ \frac{y}{w} \ \frac{z}{w})$




## Turning on the Lights

- Flip each light's switch
 

```
glEnable( GL_LIGHTn );
```
- Turn on the power
 

```
glEnable( GL_LIGHTING );
```





### Light Material Tutorial

```

GLfloat light_pos[] = { -2.00, 2.00, 2.00, 1.00 };
GLfloat light_Ka[] = { 0.00, 0.00, 0.00, 1.00 };
GLfloat light_Kd[] = { 1.00, 1.00, 1.00, 1.00 };
GLfloat light_Ks[] = { 1.00, 1.00, 1.00, 1.00 };

glLightfv(GL_LIGHT0, GL_POSITION, light_pos);
glLightfv(GL_LIGHT0, GL_AMBIENT, light_Ka);
glLightfv(GL_LIGHT0, GL_DIFFUSE, light_Kd);
glLightfv(GL_LIGHT0, GL_SPECULAR, light_Ks);

GLfloat material_Ka[] = { 0.11, 0.00, 0.11, 1.00 };
GLfloat material_Kd[] = { 0.43, 0.47, 0.54, 1.00 };
GLfloat material_Ks[] = { 0.33, 0.33, 0.52, 1.00 };
GLfloat material_Ke[] = { 0.00, 0.00, 0.00, 0.00 };
GLfloat material_Sc = 10 ;

glMaterialfv(GL_FRONT, GL_AMBIENT, material_Ka);
glMaterialfv(GL_FRONT, GL_DIFFUSE, material_Kd);
glMaterialfv(GL_FRONT, GL_SPECULAR, material_Ks);
glMaterialfv(GL_FRONT, GL_EMISSION, material_Ke);
glMaterialf(GL_FRONT, GL_SHININESS, material_Sc);
    
```

Click on the arguments and move the mouse to modify values.

### Controlling a Light's Position

- Modelview matrix affects a light's position
  - Different effects based on when position is specified
    - eye coordinates
    - world coordinates
    - model coordinates
  - Push and pop matrices to uniquely control a light's position

### Light Position Tutorial

```

GLfloat pos[] = { 1.50, 1.00, 1.00, 0.00 };

glLookAt( 0.00, 0.00, 2.00, <- eye
          0.00, 0.00, 0.00, <- center
          0.00, 1.00, 0.00 ); <- up

glLightfv(GL_LIGHT0, GL_POSITION, pos);
    
```

Click on the arguments and move the mouse to modify values.

### Tips for Better Lighting

- Recall lighting computed only at vertices
  - model tessellation heavily affects lighting results
    - better results but more geometry to process
- Use a single infinite light for fastest lighting
  - minimal computation per vertex

### Lighting Models

	To	
From	Somewhere	Everywhere
Somewhere	Specular	Lambertian
Everywhere	Cautics	Ambient

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