

Part I

Defining a Language's Evaluation

`lambda.rhm:`

- `#lang shplait` \Rightarrow eager Moe
- `#lang shplait with ~lazy` \Rightarrow lazy Moe

`more_lazy.rhm:`

- With `#lang shplait` \Rightarrow lazy Moe
- With `#lang shplait with ~lazy` \Rightarrow lazy Moe

Let's make eager evaluation order explicit

Evaluation and “To do” Lists

```
interp(plusE(intE(1), intE(2)), mt_env)
```

```
⇒ num_plus(interp(intE(1), mt_env),  
            interp(intE(2), mt_env))
```

```
⇒ interp(intE(1), mt_env)
```

To do:

```
num_plus(●,  
          interp(intE(2), mt_env))
```

```
⇒ intV(1)
```

To do:

```
num_plus(●,  
          interp(intE(2), mt_env))
```

```
⇒ interp(intE(2), mt_env)
```

To do:

```
num_plus(intV(1),  
          ●)
```

```
⇒ intV(2)
```

To do:

```
num_plus(intV(1),  
          ●)
```

```
⇒ num_plus(intV(1), intV(2))
```

Continuations

A “to do” list is a **continuation**

```
To do:  
num_plus (●,  
          interp (intE (2), mt_env))
```

Continuations

A “to do” list is a **continuation**

```
To do:  
3 + ● * f(rest(ls))
```

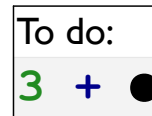
A **stack** is one way to implement continuations

```
To do:  
● * f(rest(ls))  
3 + ●
```

The terms **stack** and **continuation** are sometimes used interchangeably

Part 2

Representing Continuations



`type Cont`

`....`

Representing Continuations



```
type Cont
| doPlusK(v :: Value)
....
```

```
doPlusK(intV(3))
```


Representing Continuations

To do:
● + f(0)

```
type Cont  
| doPlusK(v :: Value)  
.....
```

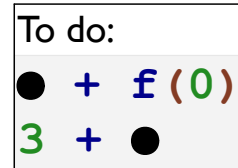
Representing Continuations

To do:
● + f(0)

```
type Cont
| plusSecondK(r :: Exp,
              e :: Env)
| doPlusK(v :: Value)
....
```

```
plusSecondK(appE(idE('#'f), intE(0)),
             mt_env)
```

Representing Continuations



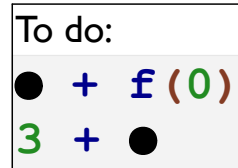
```
type Cont
| plusSecondK(r :: Exp,
              e :: Env)
| doPlusK(v :: Value)
....
```

Representing Continuations

To do:
● + f(0)
3 + ●

```
type Cont
| plusSecondK(r :: Exp,
              e :: Env,
              k :: Cont)
| doPlusK(v :: Value,
          k :: Cont)
....
```

Representing Continuations



```
type Cont
| doneK()
| plusSecondK(r :: Exp,
              e :: Env,
              k :: Cont)
| doPlusK(v :: Value,
          k :: Cont)
....
```

```
plusSecondK(appE(idE('#f'), intE(0)),
            mt_env,
            doPlusK(intV(3),
                    doneK()))
```

Part 3

interp with Continuations

```
def interp :: (Exp, Env) -> Value:
  fun (a, env):
    match a
    | ....
    | plusE(l, r): num_plus(interp(l, env),
                             interp(r, env))
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env) -> Value:
  fun (a, env):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    num_plus(●
                              interp(r, env))
    | ....
```


interp with Continuations

```
def interp :: (Exp, Env) -> Value:
  fun (a, env):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    num_plus(●
                              ,
                              interp(r, env))
    | ....
```

To do:
● + <Exp>

interp with Continuations

```
def interp :: (Exp, Env) -> Value:
  fun (a, env):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    num_plus(●,
                              interp(r, env))
    | ....
```

To do: num_plus(●, interp(r, env))
--

interp with Continuations

```
def interp :: (Exp, Env) -> Value:
  fun (a, env):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    plusSecondK(r, env)
    | ....
```

To do:

```
num_plus(●,
         interp(r, env))
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    plusSecondK(r, env, k)
    | ....
```

```
To do:
num_plus(●,
         interp(r, env))
....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | plusE(l, r): interp(l, env)
                    plusSecondK(r, env, k)
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | plusE(l, r): interp(l, env, plusSecondK(r, env, k))
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n) : intV(n)
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....
```


interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
      | ....
      | intE(n): continue(k, intV(n))
      | ....

def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
      | ....

      | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....

def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | doneK(): v
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....

def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | plusSecondK(r, env, next_k):
      interp(r, env,
            ....)
    | ....
```

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....
```

```
def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | plusSecondK(r, env, next_k):
      interp(r, env,
            ....)
    | ....
```

To do: num_plus(●, interp(r, env))

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....
```

```
def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | plusSecondK(r, env, next_k):
      interp(r, env,
            ....)
    | ....
```

To do: num_plus(v, ●)

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....
```

```
def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | plusSecondK(r, env, next_k):
      interp(r, env,
            doPlusK(v, next_k))
    | ....
```

To do: num_plus(v, ●

interp with Continuations

```
def interp :: (Exp, Env, Cont) -> Value:
  fun (a, env, k):
    match a
    | ....
    | intE(n): continue(k, intV(n))
    | ....
```

```
def continue :: (Cont, Value) -> Value:
  fun (k, v):
    match k
    | ....
    | doPlusK(v_1, next_k):
      continue(next_k,
               num_plus(v_1, v))
    | ....
```

To do: num_plus(v_1, ●

Part 4

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:  
  match a ....  
  | intE(n): continue(k, intV(n))  
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:  
  match k ....  
  | doneK(): v  
  | ....
```

```
interp(intE(5), mt_env, doneK())
```

```
⇒ continue(doneK(), intV(5))
```

```
⇒ intV(5)
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | plusE(l, r): interp(l, env, plusSecondK(r, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | plusSecondK(r, env, next_k):
    interp(r, env, doPlusK(v, next_k))
  | doPlusK(v_l, next_k):
    continue(next_k, num_plus(v_l, v))
  | ....
```

```
interp(plusE(intE(5), intE(2)), mt_env, doneK())
```

```
⇒ interp(intE(5), mt_env,
         plusSecondK(intE(2), mt_env, doneK()))
```

```
⇒ continue(plusSecondK(intE(2), mt_env, doneK()),
           intV(5))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | plusE(l, r): interp(l, env, plusSecondK(r, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | plusSecondK(r, env, next_k):
    interp(r, env, doPlusK(v, next_k))
  | doPlusK(v_l, next_k):
    continue(next_k, num_plus(v_l, v))
  | ....
```

```
⇒ continue(plusSecondK(intE(2), mt_env, doneK()),
           intV(5))
```

```
⇒ interp(intE(2), mt_env,
         doPlusK(intV(5), doneK()))
```

```
⇒ continue(doPlusK(intV(5), doneK()),
           intV(2))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | plusE(l, r): interp(l, env, plusSecondK(r, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | plusSecondK(r, env, next_k):
      interp(r, env, doPlusK(v, next_k))
  | doPlusK(v_l, next_k):
      continue(next_k, num_plus(v_l, v))
  | ....
```

```
⇒ continue(doPlusK(intV(5), doneK()),
           intV(2))
```

```
⇒ continue(doneK(),
           intV(7))
```

Part 5

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | funE(n, body):
    continue(k, closV(n, body, env))
  | ....

fun continue(k :: Cont, v :: Value) :: Value:
  match k ....

  | ....
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....

fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                               c_env),
             next_k)
    | ~else: error(....)
  | ....
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....

fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                               c_env),
              next_k)
    | ~else: error(....)
  | ....
```


interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind('#f,
                      closV('#x,
                            idE('#x),
                            mt_env)),
                  mt_env)
```

```
interp(appE(idE('#f), intE(1)),
        E1,
        doneK())
```

```
⇒ interp(idE('#f),
          E1,
          appArgK(intE(1), E1, doneK()))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind('#f,
                       closV('#x,
                              idE('#x),
                              mt_env)),
                  mt_env)
```

```
⇒ interp(idE('#f),
          E1,
          appArgK(intE(1), E1, doneK()))
```

```
⇒ continue(appArgK(intE(1), E1, doneK()),
            closV('#x, idE('#x), mt_env))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind('#f,
                      closV('#x,
                            idE('#x),
                            mt_env)),
                  mt_env)
```

```
⇒ continue(appArgK(intE(1), E1, doneK()),
           closV('#x, idE('#x), mt_env))
```

```
⇒ interp(intE(1),
         E1,
         doAppK(closV('#x, idE('#x), mt_env), doneK()))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind(#'f,
                      closV(#'x,
                            idE(#'x),
                            mt_env)),
                  mt_env)
```

```
⇒ interp(intE(1),
          E1,
          doAppK(closV(#'x, idE(#'x), mt_env), doneK()))
```

```
⇒ continue(doAppK(closV(#'x, idE(#'x), mt_env), doneK()),
            intV(1))
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind('#f,
                        closV('#x,
                              idE('#x),
                              mt_env)),
                  mt_env)
```

```
⇒ continue(doAppK(closV('#x, idE('#x), mt_env), doneK()),
           intV(1))
```

```
⇒ interp(idE('#x),
         extend_env(bind('#x, intV(1)), mt_env),
         doneK())
```

interp with Continuations

```
fun interp(a :: Exp, env :: Env, k :: Cont) :: Value:
  match a ....
  | appE(fn, arg): interp(fn, env, appArgK(arg, env, k))
  | ....
```

```
fun continue(k :: Cont, v :: Value) :: Value:
  match k ....
  | appArgK(a, env, next_k):
    interp(a, env, doAppK(v, next_k))
  | doAppK(v_f, next_k):
    match v_f
    | closV(n, body, c_env):
      interp(body, extend_env(bind(n, v),
                                c_env),
              next_k)
    | ~else: error(....)
  | ....
```

```
E1 = extend_env(bind('#f,
                        closV('#x,
                              idE('#x),
                              mt_env)),
                  mt_env)
```

```
⇒ interp(idE('#x),
          extend_env(bind('#x, intV(1)), mt_env),
          doneK())
```

```
⇒ continue(doneK(),
            intV(1))
```

Part 6

Loop Syntax versus Function Calls

The Java way:

```
int sum(List<Integer> lst) {  
    int t = 0;  
    for (Integer n : lst) {  
        t = t + n;  
    }  
    return t;  
}
```

The Shplait way:

```
fun sum(lst :: Listof(Int), t :: Int):  
    match lst  
    | []: t  
    | cons(f, rst): sum(rst, f + t)
```


Infinite Loop

```
while (1) { }
```

Space-Bounded Loop

```
int f() { return f(); }
```

Moe Loop

```
let f = (fun (f) :  
          f(f)) :  
        f(f)
```

infinite or space-bounded?

Moe Loop

```
let f = (fun (f) : f(f)) :  
    f(f)
```

Moe Loop

```
let f = (fun (f) : f(f)) :  
        f(f)
```

⇒

```
(fun (f) : f(f)) (fun (f) : f(f))
```

Moe Loop

```
(fun (f) : f(f)) (fun (f) : f(f))
```

Moe Loop

```
(fun (f) : f(f)) (fun (f) : f(f))
```

⇒

```
(fun (f) : f(f)) (fun (f) : f(f))
```

Moe Loop

```
interp( (fun (f) : f(f)) (fun (f) : f(f)) ,  
        mt_env ,  
        doneK() )
```


Moe Loop

```
interp( (fun (f) : f(f)) (fun (f) : f(f)) ,  
        mt_env ,  
        doneK() )
```

need several
setup steps...

Moe Loop

```
interp ( (fun (f) : f(f)) (fun (f) : f(f)) ) ,  
        mt_env ,  
        doneK ( ) )
```

⇒

```
interp ( fun (f) : f(f) ) ,  
        mt_env ,  
        appArgK ( fun (f) : f(f) ) ,  
                 mt_env ,  
                 doneK ( ) )
```

Moe Loop

```
interp ( fun (f) : f(f) ,  
        mt_env ,  
        appArgK ( fun (f) : f(f) ,  
                  mt_env ,  
                  doneK() ) )
```

Moe Loop

```
interp ( fun (f) : f(f) ,  
        mt_env ,  
        appArgK ( fun (f) : f(f) ,  
                  mt_env ,  
                  doneK() ) )  
⇒  
continue ( appArgK ( fun (f) : f(f) ,  
                    mt_env ,  
                    doneK() ) ,  
          closV ( #'f , f(f) , mt_env ) )
```

Moe Loop

```
continue (appArgK ( fun (f) : f(f) ,  
                    mt_env ,  
                    doneK() ) ,  
          closV (#' f , f(f) , mt_env))
```

Moe Loop

```
continue (appArgK (fun (f) : f(f) ,  
                  mt_env ,  
                  doneK ()),  
          closV (#'f, f(f) , mt_env))
```

⇒

```
interp (fun (f) : f(f) ,  
        mt_env ,  
        doAppK (closV (#'f, f(f) , mt_env) ,  
                 doneK ()))
```

Moe Loop

```
interp( fun (f): f(f) ,  
        mt_env ,  
        doAppK(closV('#' f, f(f) , mt_env) ,  
               doneK() ) )
```

Moe Loop

```
interp ( fun (f) : f(f) ,  
         mt_env ,  
         doAppK (closV (#'f, f(f) , mt_env) ,  
                   doneK() ) )
```

⇒

```
continue (doAppK (closV (#'f, f(f) , mt_env) ,  
                  doneK() ) ,  
          closV (#'f, f(f) , mt_env))
```


Moe Loop

```
continue (doAppK (closV (#'f, f(f), mt_env),  
                  doneK()),  
          closV (#'f, f(f), mt_env))
```

Moe Loop

```
continue (doAppK (closV (#'f, f(f)), mt_env),  
            doneK()),  
          closV (#'f, f(f)), mt_env))
```

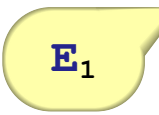
⇒

```
interp (f(f),  
        extend_env (bind (#'f, closV (#'f,  
                                     f(f),  
                                     mt_env))),  
                mt_env),  
        doneK())
```

Moe Loop

```
interp(f(f),  
      extend_env(bind(#'f, closV(#'f,  
                                f(f),  
                                mt_env))),  
      mt_env),  
doneK())
```

Moe Loop

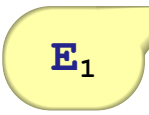
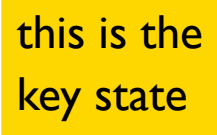
```
interp(f(f) ,  
       extend_env(bind('#'f, closV('#'f,  
                             f(f) ,  
                             mt_env)) ,  
            mt_env) ,  
      doneK())
```

Moe Loop

```
interp ( f(f) ,  
        extend_env ( bind ( #' f , closV ( #' f ,  
                                         E1 ,  
                                         f(f) ,  
                                         mt_env ) ) ,  
                    mt_env ) ,  
          doneK () )  
=  
interp ( f(f) ,  
        E1 ,  
        doneK () )
```

Moe Loop

```
interp ( f(f) ,  
        extend_env ( bind ( #'f , closV ( #'f ,  
                                        f(f) ,  
                                        mt_env ) ) ,  
                    mt_env ) ,  
        doneK () )  
=  
interp ( f(f) ,  
        E1 ,  
        doneK () )
```

Moe Loop

```
interp ( f (f) ,  
        E1 ,  
        doneK ( ) )
```

Moe Loop

```
interp ( f (f) ,  
        E1 ,  
        doneK ( ) )  
⇒  
interp ( f ,  
        E1 ,  
        appArgK ( f , E1 ,  
                 doneK ( ) ) )
```


Moe Loop

```
interp ( f ,  
        E1 ,  
        appArgK ( f , E1 ,  
                  doneK ( ) ) )
```

Moe Loop

```
interp ( f ,  
        E1 ,  
        appArgK ( f , E1 ,  
                  doneK ( ) ) )  
⇒  
continue ( appArgK ( f , E1 ,  
                    doneK ( ) ) ,  
          closV ( # ' f , f ( f ) , mt_env ) )
```

Moe Loop

```
continue (appArgK (f, E1,  
                  doneK()),  
          closV (#'f, f(f), mt_env))
```

Moe Loop

```
continue (appArgK (f, E1,  
                  doneK()),  
          closV (#'f, f(f), mt_env))
```

⇒

```
interp (f,  
        E1,  
        doAppK (closV (#'f, f(f), mt_env),  
                doneK()))
```

Moe Loop

```
interp ( f ,  
        E1 ,  
        doAppK ( closV ( #' f , f ( f ) , mt_env ) ,  
                 doneK ( ) ) )
```

Moe Loop

```
interp(f,  
      E1,  
      doAppK(closV(#'f, f(f), mt_env),  
             doneK()))
```

⇒

```
continue(doAppK(closV(#'f, f(f), mt_env),  
                doneK()),  
         closV(#'f, f(f), mt_env))
```

Moe Loop

```
continue (doAppK (closV (#'f, f(f), mt_env),  
                  doneK()),  
          closV (#'f, f(f), mt_env))
```

Moe Loop

```
continue (doAppK (closV (#'f, f(f), mt_env),  
                    doneK()),  
          closV (#'f, f(f), mt_env))
```

⇒

```
interp (f(f),  
        E1,  
        doneK())
```


Moe Loop

```
continue (doAppK (closV (#' f, f(f), mt_env),  
                  doneK()),  
          closV (#' f, f(f), mt_env))
```

⇒

```
interp (f(f),  
        E1,  
        doneK())
```

back to key state
⇒ loops forever

Part 7

Moe Loop?

```
let f = (fun (f) : 1 + f(f)) :  
    f(f)
```

Moe Loop?

```
let f = (fun (f) : 1 + f(f)) :  
        f(f)
```

⇒

```
(fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

Moe Loop?

```
(fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

Moe Loop?

```
(fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

⇒

```
1 + (fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

Moe Loop?

```
1 + (fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

Moe Loop?

```
1 + (fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```

⇒

```
1 + 1 + (fun (f) : 1 + f(f)) (fun (f) : 1 + f(f))
```


Tail Calls

```
fun forever(x) :  
  forever(! x)
```

Call to `forever` is a **tail call**, because there's no work to do after `forever` returns

Non-Tail Calls

```
fun run_out_of_memory(x) :  
  ! run_out_of_memory(x)
```

The call to `run_out_of_memory` is *not* a tail call,
because there's work to do after it returns

Tail Calls

```
fun forever(x) :  
  if x  
    | forever(#true)  
    | forever(#false)
```

Even though the call to `forever` is wrapped in `if`, there's no work to do after `forever` returns

The branches of `if` are in **tail position** with respect to the `if`

Non-Tail Calls

```
fun run_out_of_memory(x) :  
  if run_out_of_memory(x)  
  | #true  
  | #false
```

The call to `run_out_of_memory` is *not* a tail call,
because there's work to do after it returns

The test position `if` is *not* in tail position with respect
to the `if`

`interp` and `continue`

In `lambda_k.rhm`:

- `interp` calls `continue` only as a tail call
- `continue` calls `interp` only as a tail call
- `continue` calls `continue` only as a tail call
- `interp` calls `interp` only as a tail call
- `lookup` calls `lookup` only as a tail call
- nothing else is recursive

∴ the Shplait continuation is always small

You must maintain this property!