

$$a \equiv_I b \iff a \equiv_{i,I} b \wedge a[i] \equiv b[i]$$