

Part 0

Defining Recursion by Expansion

```
letrec name = rhs:  
  body
```

could be parsed the same as

```
let name = mk_rec(fun (name) : rhs) :  
  body
```

which is really

```
(fun (name) : body) (mk_rec(fun (name) : rhs))
```

Part I
Metacircular Recursion

Recursive Binding

```
block:  
  def x = 10  
  x + 1
```

11

Recursive Binding

```
block:  
  fun f(x) : f(x)  
  f(1)
```

infinite loop – good!

Recursive Binding

```
block:  
  def x = x  
  x
```

x: cannot use before initialization

Recursive Binding

```
block:  
  def x = [x]  
  x
```

x: cannot use before initialization

Recursive Binding

```
block:  
  def f = fun (x) : f(x)  
  f(1)
```

infinite loop – good!

Recursive Binding

```
letrec f = (fun (x) : f(x)) :  
  f(1)
```

infinite loop – good!

Recursive Binding

```
letrec f = [fun (x) : first(f) (x)]:  
          first(f) (1)
```

infinite loop – good!

Recursive Binding

```
letrec f = (fun (x) : f(x)) :  
  f(1)
```

```
| letrecE(name, rhs, body) :  
  block :  
    def val = interp(rhs,  
                      extend_env(bind(name, val),  
                                  env))  
  
  interp(body,  
          extend_env(bind(name, val),  
                      env))
```

val: cannot use before initialization

Recursive Binding

```
letrec f = (fun (x) : f(x)) :  
  f(1)
```

```
| letrecE(name, rhs, body) :  
  block:  
    def val = interp(rhs,  
                      extend_env(bind(name, fun () : val),  
                                  env))  
  
  interp(body,  
          extend_env(bind(name, fun () : val),  
                      env))
```

works!

Metacircular letrec

```
type Binding
| bind(name :: Symbol,
        val :: () -> Value)

fun lookup(n :: Symbol, env :: Env) :: Value:
  match env
  | []: error('#lookup, "free variable")
  | cons(b, rst_env): cond
                        | n == bind.name(b) :
                          bind.<val(b) ()
                        | ~else: lookup(n, rst_env)
```

Part 2

Exp Grammar

```
<Exp> ::= <Int>  
| <Exp> + <Exp>  
| <Exp> - <Exp>  
| <Symbol>  
| fun (<Symbol>) : <Exp>  
| <Exp> (<Exp>)  
| let <Symbol> = <Exp> : <Exp>  
| if <Exp> == 0 | <Exp> | <Exp>  
| letrec <Symbol> = <Exp> : <Exp>
```

NEW

NEW

Metacircular letrec

```
fun interp(a :: Exp, env :: Env) :: Value:
  match a
  | ....
  | letrecE(n, rhs, body):
      def new_env:
        extend_env(bind(n, fun (): val),
                  env)

      def val:
        interp(rhs, new_env)
        interp(body, new_env)
```


Metacircular letrec

check:

```
interp(parse('letrec fac = (fun (x):
              if x == 0
              | 1
              | x * fac(x + -1)):
              fac(5) '),
        mt_env)
~is intV(120)
```

Metacircular letrec

```
interp (parse ('letrec x = x:  
                x'),  
        mt_env)
```

val: cannot use before initialization

... a crash at the Shplait level

Part 3
Assignment-Based Recursion

Defining Recursion by Expansion

```
letrec name = rhs:  
  body
```

could be parsed the same as

```
let name = mk_rec(fun (name) : rhs) :  
  body
```

which is really

```
(fun (name) : body) (mk_rec(fun (name) : rhs))
```

Defining Recursion by Expansion

Another approach:

```
letrec fac = (fun (n) :  
    if n == 0  
    | 1  
    | n * fac(n - 1)) :  
fac(10)
```

⇒

```
let fac = 42 :  
begin :  
    fac := (fun (n) :  
        if n == 0  
        | 1  
        | n * fac(n - 1))  
fac(10)
```

Implementing Recursion

Expanding to assignment in Moe works only if Moe has state...

... but the same state idea for **letrec** can work using Shplait's state

Assignment-Based letrec

```
type Binding
| bind(name :: Symbol,
        val :: Boxof(Value))

fun lookup(n :: Symbol, env :: Env) :: Value:
  match env
  | []: error('#lookup, "free variable")
  | cons(b, rst_env): cond
                        | n == bind.name(b) :
                          unbox(bind.val(b))
                        | ~else: lookup(n, rst_env)
```

Assignment-Based letrec

```
fun interp(a :: Exp, env :: Env) :: Value:
  match a
  | ....
  | letrecE(n, rhs, body):
      let b = box(intV(42)):
          let new_env = extend_env(bind(n, b),
                                   env):
              set_box(b, interp(rhs, new_env))
              interp(body, new_env)
```


Part 4

Use Before Initialization

Use Before Initialization

```
interp(parse('letrec x = x:  
              x'),  
        mt_env)  
⇒ intV(42)
```

Use Before Initialization

```
fun interp(a :: Exp, env :: Env) :: Value:
  match a
  | ....
  | letrecE(n, rhs, body):
      let b = box(intV(42)):
          let new_env = extend_env(bind(n, b),
                                   env):
              set_box(b, interp(rhs, new_env))
              interp(body, new_env)
```

Use Before Initialization

```
type Binding
| bind(name :: Symbol,
        val :: Boxof(Optionof(Value)))

fun lookup(n :: Symbol, env :: Env) :: Value:
  match env
  | []: error(#'lookup, "free variable")
  | cons(b, rst_env):
    cond
    | n == bind.name(b):
      match unbox(bind.val(b))
      | none(): error(#'lookup, "use before initialization")
      | some(v): v
    | ~else: lookup(n, rst_env)
```

Use Before Initialization

```
fun interp(a :: Exp, env :: Env) :: Value:
  match a
  | ....
  | letrecE(n, rhs, body):
      let b = box(none()):
          let new_env = extend_env(bind(n, b),
                                   env):
              set_box(b, some(interp(rhs, new_env)))
              interp(body, new_env)
```